# The Pythagorean Theorem

### Pythagoras

- Lived in southern Italy during the sixth century B.C.
- Considered the first true mathematician
- Used mathematics as a means to understand the natural world
- First to teach that the earth was a sphere that revolves around the sun



## Right Triangles

Longest side is the hypotenuse, side c (opposite the 90° angle)
The other two sides are the legs, sides a and b
Pythagoras developed a formula for finding the length of the sides of any *right* triangle



## The Pythagorean Theorem

"For any right triangle, the sum of the areas of the two small squares is equal to the area of the larger."

 $a^2 + b^2 = c$ 

b а







### Solve for x.



## abe =

 $6^{2} + 8^{2} = x^{2}$  $36 + 64 = x^{2}$  $100 = x^{2}$  $\sqrt{100} = \sqrt{x^{2}}$ 

### Solve for y.



#### Solve for t.

6

abel=  $t^{2} + 6^{2} = 15^{2}$   $t^{2} + 36 = 225$ -36 - 36

 $t^{2} = 189$   $\sqrt{t^{2}} = \sqrt{189}$   $t = \sqrt{189}$   $t \approx 13.7$ 

To the nearest tenth of a foot, find the length of the diagonal of a rectangle with a width of 4 feet and a length of 10 feet.



abc = $4^2 + 10^2 = x^2$  $16 + 100 = x^2$  $116 = x^2$  $\sqrt{116} = \sqrt{x^2}$  $x = \sqrt{116}$ 

(x ≈ 10.8)

A car drives 20 miles due east and then 45 miles due south. To the nearest hundredth of a mile, how far is the car from its starting point?



- Applications The Pythagorean theorem has far-reaching ramifications in other fields (such as the arts), as well as practical applications.
- The theorem is invaluable when computing distances between two points, such as in navigation and land surveying.
  - Another important application is in the design of ramps. Ramp designs for handicap-accessible sites and for skateboard parks are very much in demand.

A baseball "diamond" is really a square.

You can use the Pythagorean theorem to find distances around a baseball diamond.

### **Baseball Problem**

The distance between consecutive bases is 90 feet. How far does a catcher have to throw the ball from home plate to second base?



## **Baseball Problem**

To use the Pythagorean theorem to solve for x, find the right angle. Which side is the hypotenuse? Which sides are the legs? Now use:  $a^2 + b^2 = c^2$ 



### Baseball Problem Solution

The hypotenuse is the distance from home to second, or side x in the picture.

The legs are from home to first and from first to second.

Solution:

 $x^2 = 90^2 + 90^2 = 16,200$ x = 127.28 ft



## Ladder Problem

A ladder leans against a second-story window of a house. If the ladder is 25 meters long, and the base of the ladder is 7 meters from the house, how high is the window?



#### Ladder Problem Solution

First draw a diagram that shows the sides of the right triangle.

- Label the sides:
  - Ladder is 25 m
  - Distance from house is 7 m
- Use  $a^2 + b^2 = c^2$  to solve for the missing side.

Distance from house: 7 meters

voler. States

### Ladder Problem Solution

1. 25 1

A = 7 m

B

11

24

E

 $7^{2} + b^{2} = 25^{2}$   $49 + b^{2} = 625$   $b^{2} = 576$ b = 24 m

How did you do?

### Sources

Great info on the Pythagorean theorem, Pythagoras, and other math-related topics:

- The Baseball Problem
- Pythagoras of Samos
- Pythagoras Playground
- Microsoft Encarta 2000