

NOTE

On the test,
 $c = \lambda\nu$ $c/\lambda = \nu$
 $c/\nu = \lambda$
 will not be given – you
 have to isolate the
 variables to get these.

Equations and constants:

$E = h\nu$ and $E = hc/\lambda$ $E =$ energy of one photon with a frequency of ν
 $c = \lambda\nu$ $c/\lambda = \nu$ $c =$ speed of light = 3.0×10^8 m/s (meters per second)
 $c/\nu = \lambda$ $h =$ Planck's constant = 6.63×10^{-34} J-s
 $\lambda =$ wavelength in meters
 $\nu =$ frequency in Hz (waves/s or $1/s$ or s^{-1})

1. A photon has a frequency (ν) of 2.68×10^6 Hz. Calculate its energy. (Ans: 1.777×10^{-27} J)

2. Calculate the energy (E) and wavelength (λ) of a photon of light with a frequency (ν) of 6.165×10^{14} Hz.

$$\begin{aligned}
 E &= h\nu \\
 &= 6.63 \times 10^{-34} \text{ J-s} \times 6.165 \times 10^{14} \text{ Hz} \\
 &= 43.867395 \times 10^{-34} \times 10^{14} \text{ Js/s} \\
 &= 43.87 \times 10^{-20} \text{ J} \\
 &= 4.387 \times 10^1 \times 10^{-20} \text{ J} \\
 &= 4.387 \times 10^{-19} \text{ J}
 \end{aligned}$$

Answer: $4.387 \times 10^{-19} \text{ J}$

3. Calculate the frequency and the energy of blue light that has a wavelength of 400 nm ($h = 6.62 \times 10^{-34}$ J-s). (Ans: 7.500×10^{14} Hz)

$$\nu = c/\lambda$$

$$c = 3.000 \times 10^8$$

$$\lambda = 400 \times 10^{-9} \text{ m}$$

$$\begin{aligned}
 \nu &= 3.000 \times 10^8 / 400 \times 10^{-9} \text{ (m/s)/m} \\
 &= 3.000/4.000 \times 10^8 / 10^{-7} \text{ (m/s)/s} = /s \\
 &= 0.7500 \times 10^{15} /s \\
 &= 7.500 \times 10^{-1} \times 10^{15} /s \\
 &= 7.500 \times 10^{14} /s \text{ Note: } /s = \text{Hz}
 \end{aligned}$$

Answer: $7.500 \times 10^{14} \text{ Hz}$

4. Calculate the wavelength and energy of light that has a frequency of 1.5×10^{15} Hz.

$$\text{Ans: } \lambda = 2.0 \times 10^{-7} \text{ m} \qquad E = 9.95 \times 10^{-19} \text{ J}$$

5. A photon of light has a wavelength of 0.050 cm. Calculate its energy.

$$\text{Ans: } E = 3.978 \times 10^{-23} \text{ J}$$

6. Calculate the number of photons having a wavelength of 10.0 μm required to produce 1.0 kJ of energy.

$$\text{Ans; } 5.000 \times 10^{21} \text{ photons}$$

7. Calculate the total energy in 1.5×10^{13} photons of gamma radiation having $\lambda = 3.0 \times 10^{-12}$ m.

Part 1: Calculate the Energy of ONE Photon

Part 2: Calculate total energy of 1.5×10^{13} photons

Part 1:

$$\begin{aligned} E &= hc / \lambda \\ &= 6.63 \times 10^{-34} \text{ J-s} \times 3.000 \times 10^8 \text{ m/s} / 3.0 \times 10^{-12} \text{ m} \\ &= 6.630 \times 10^{-34} \times 10^8 \times 10^{12} \text{ Jsm/ms} \\ &= 6.630 \times 10^{-14} \text{ J} \\ &= 6.630 \times 10^1 \times 10^{-14} \text{ J} \\ &= 6.630 \times 10^{-13} \text{ J} \end{aligned}$$

Part 1 Answer: $6.630 \times 10^{-13} \text{ J}$
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Part 2:

$$\begin{aligned} 1 \text{ Photon} &= 6.630 \times 10^{-13} \text{ J} \\ 1.500 \times 10^{13} &= ? \text{ J} \\ &= (1.500 \times 10^{13} \times 1) \times 6.630 \times 10^{-13} \text{ J/J} \\ &= (1.500 \times 6.630) \times 10^{13} \times 10^{-13} \\ &= 9.945 \text{ J} \end{aligned}$$

Part 2 Answer: 9.945 J

8. Calculate the energy and frequency of red light having a wavelength of 6.80×10^{-5} cm.

Ans: $E = 2.940 \times 10^{-19}$ J $\nu = 4.4 \times 10^{12}$ Hz

9. The wavelength of green light from a traffic signal is centered at 5.20×10^{-5} cm. Calculate the frequency.

$$\lambda = c/\nu$$

$$C = 3.000 \times 10^8$$

$$\nu = 5.20 \times 10^{-5} \text{ Hz}$$

$$\lambda = 3.000 \times 10^8 / 5.200 \times 10^{-5} \text{ (m/s) Hz (remember Hz is cycles/s)}$$

$$= 15.600 \times 10^3 \text{ (m/s)s} = \text{m}$$

$$= 1.560 \times 10^1 \times 10^3 = 1.560 \times 10^4 \text{ m}$$

Answer: 1.560×10^4 m

10. Calculate the frequency of light that has a wavelength of 4.25×10^{-9} m.

Ans: $\nu = 7.059 \times 10^{16}$ Hz.