

5. $2x - 3y = -24$ solve for y

6. $x + 6y = 18$ solve for x

Warm up: Solve the given system by elimination

$$1) \quad 6x - 3y = 21$$

$$3x + 3y = -3$$

$$(2, -3)$$

$$2) \quad -3x + 4y = -4$$

$$6x - 12y = 12$$

$$(0, -1)$$

Solve Systems of Equations by Graphing

Linear Systems

Question: How can we analyze a system of Equations Graphically to determine if there is a solution?

A system of equations means: There are two or more equations sharing the same variables

Solution: Is a set of values that satisfy both equations. Graphically it is the point of intersection

Types of Systems

∞ There are 3 different types of systems of linear equations

3 Different Systems:

- 1) Infinite Solutions
- 2) No Solution
- 3) One solution

Determine a Solution to a Linear System

OPENER

Which of the following ordered pairs are solutions to the following system?

$$5x + 2y = 10$$

$$-4x + y = -8$$

1) (3,1)

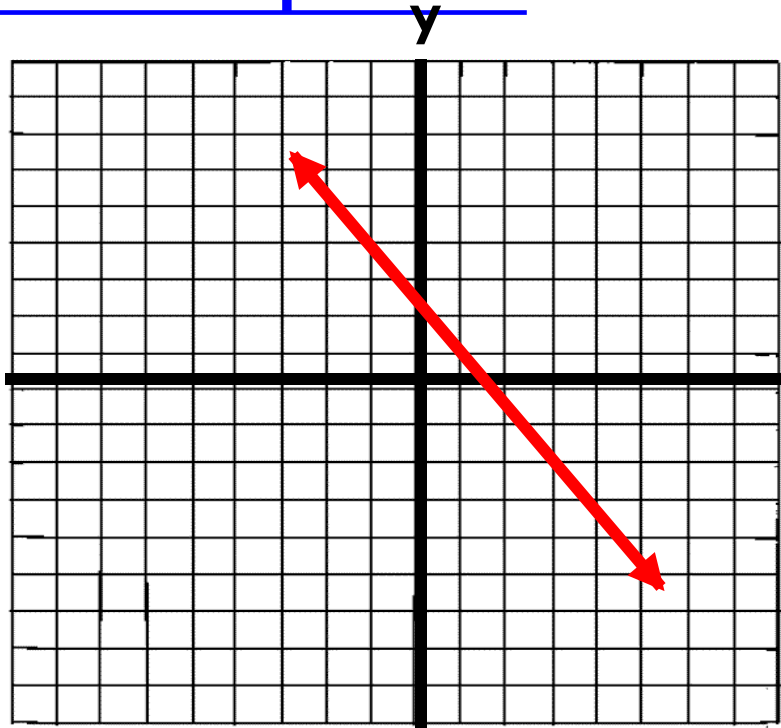


2) (2,0)

-8

Type 1: Infinite Solutions

∞ A system of linear equations having an infinite number of solutions is described as being consistent-dependent.



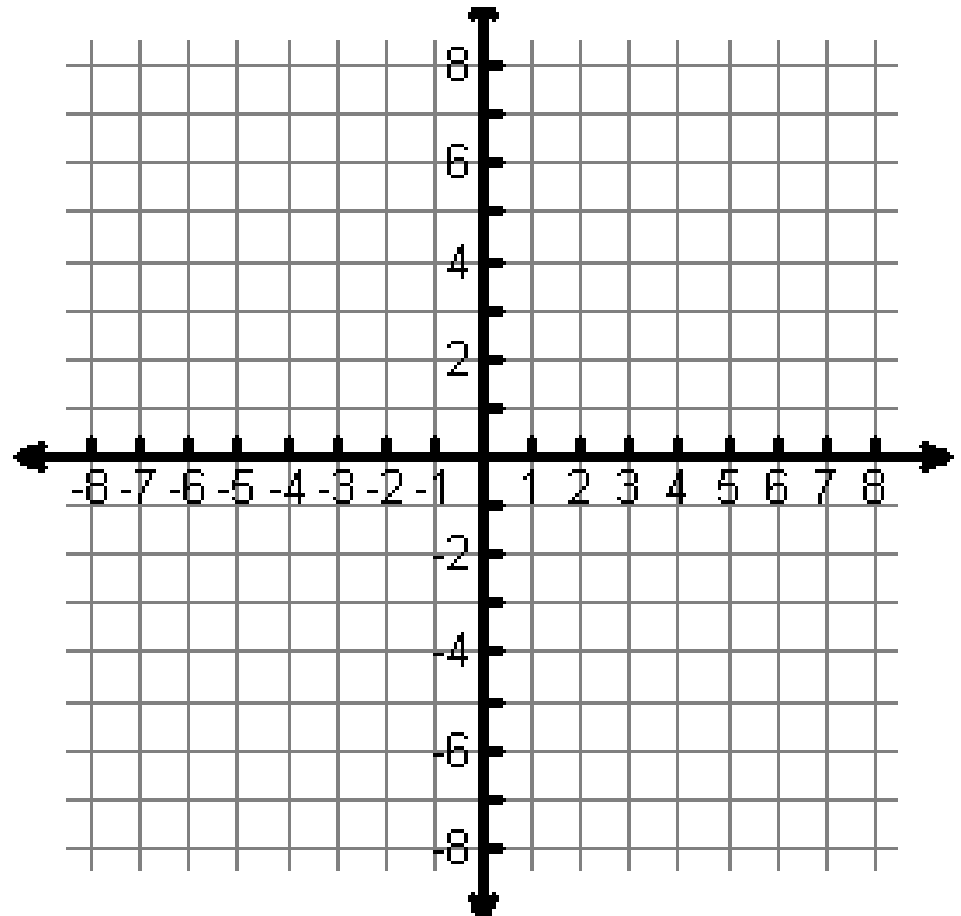
← The system has infinite solutions, the lines are **identical**

$$y = 2x + 3$$

1. Graph to find the solution.

$$y = 2x + 3$$

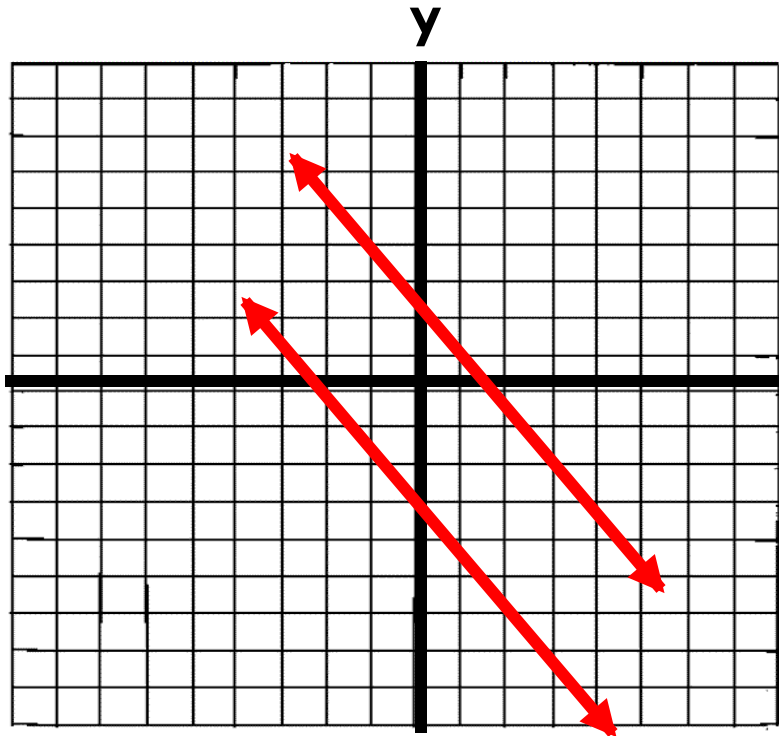
$$y = 2x + 3$$



**INFINITE
Solutions**

Type 2: No Solutions

∞ A system of linear equations having no solutions is described as being inconsistent.



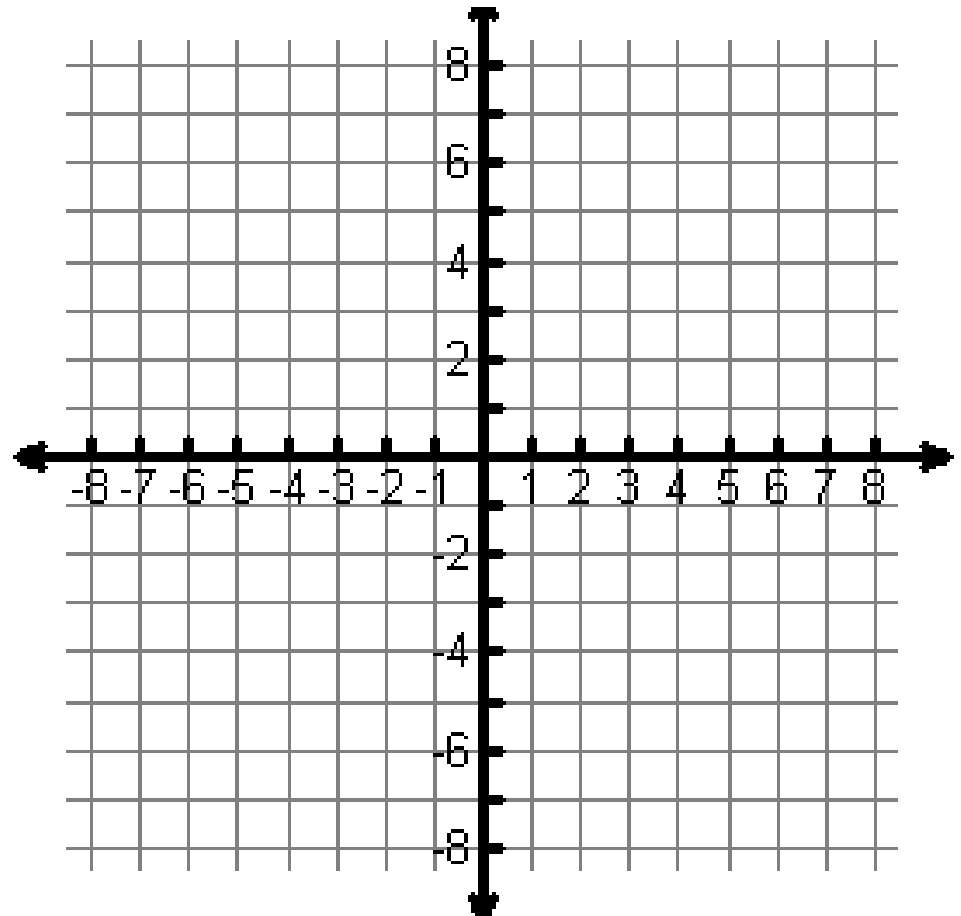
← The system has no solution, the lines are **parallel**

× Remember, parallel lines have the same slope

2. Graph to find the solution.

$$y = -2x + 5$$

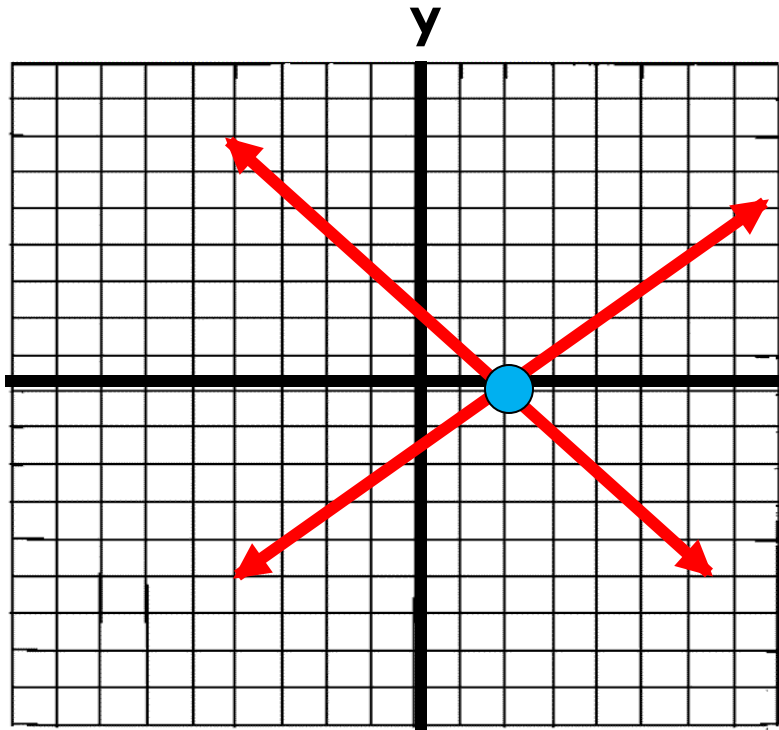
$$y = -2x + 1$$



**No
Solution**

Type 3: One solution

∞ A system of linear equations having exactly one solution is described as being one solution.



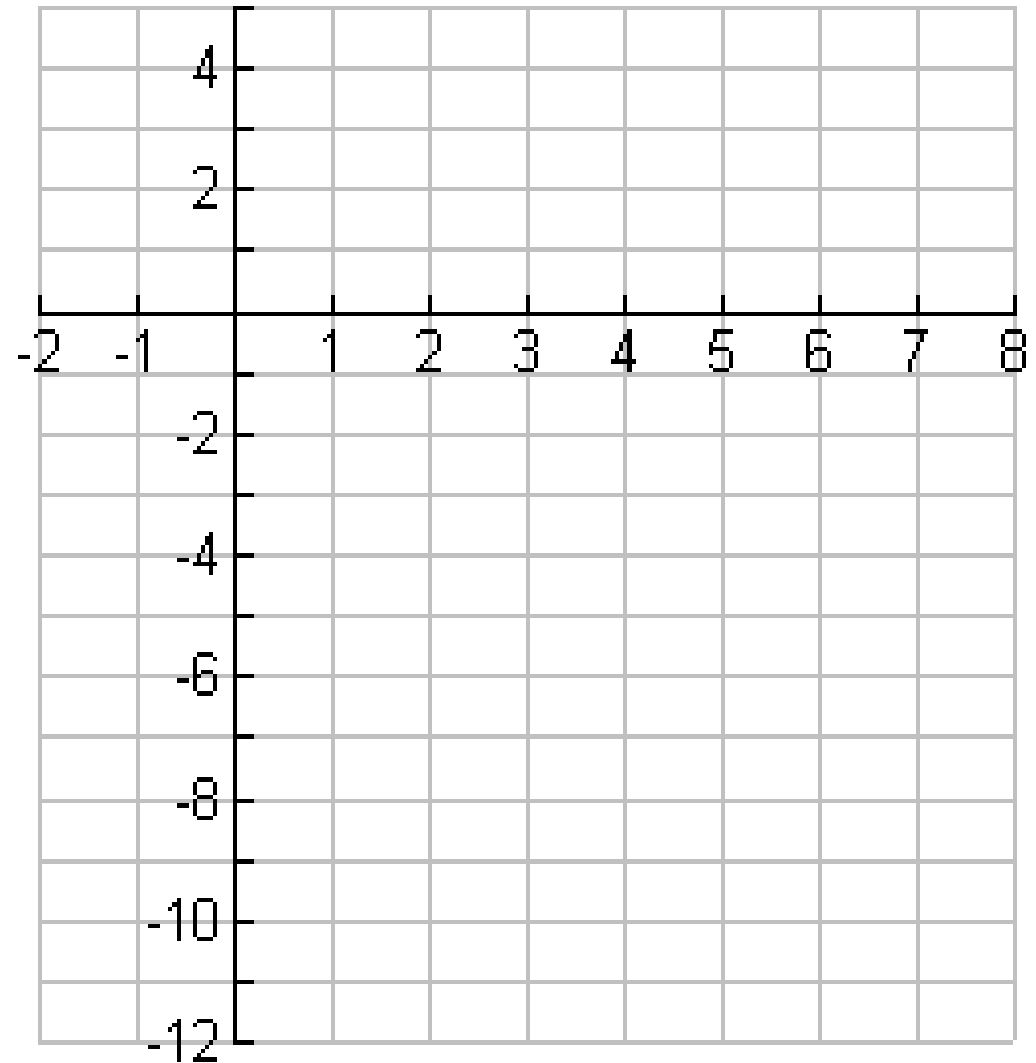
← The system has exactly one solution at the *point of intersection*

3. Graph to find the solution.

$$y = 3x - 12$$

$$y = -2x + 3$$

Solution:
(3, -3)



Steps

- 1. Make sure each equation is in slope-intercept form: $y = mx + b$.**
- 2. Graph each equation on the same graph paper.**
- 3. The point where the lines intersect is the solution.** *If they don't intersect then there's no solution.*
- 4. Check your solution algebraically.**

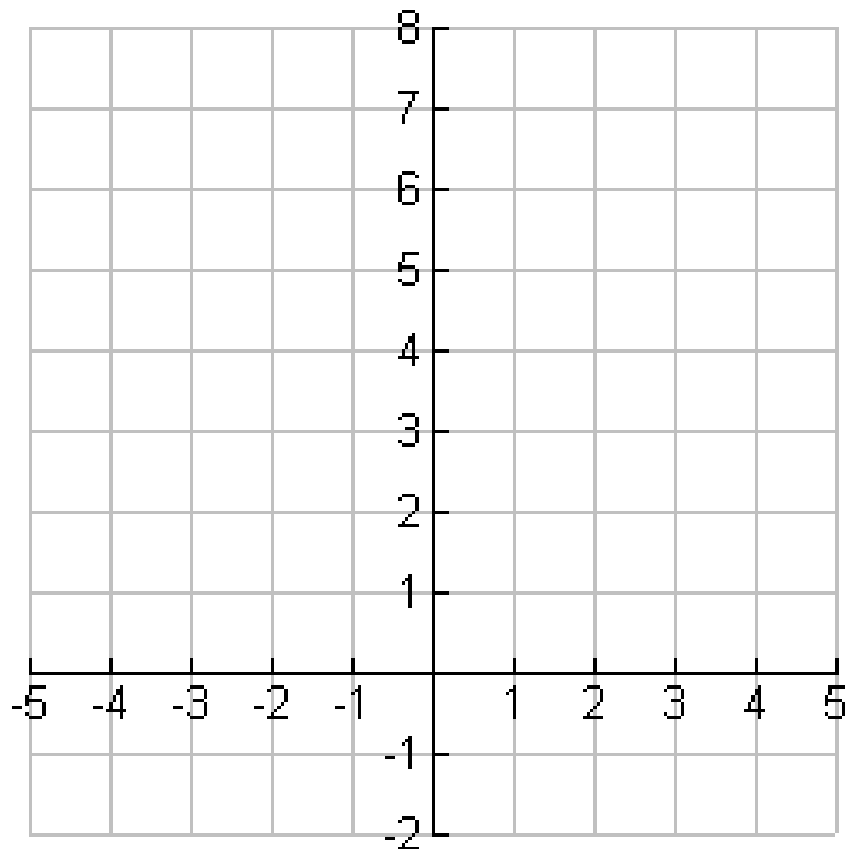
1. Graph to find the solution.

$$2x - 2y = -8$$

$$2x + 2y = 4$$

Solution:

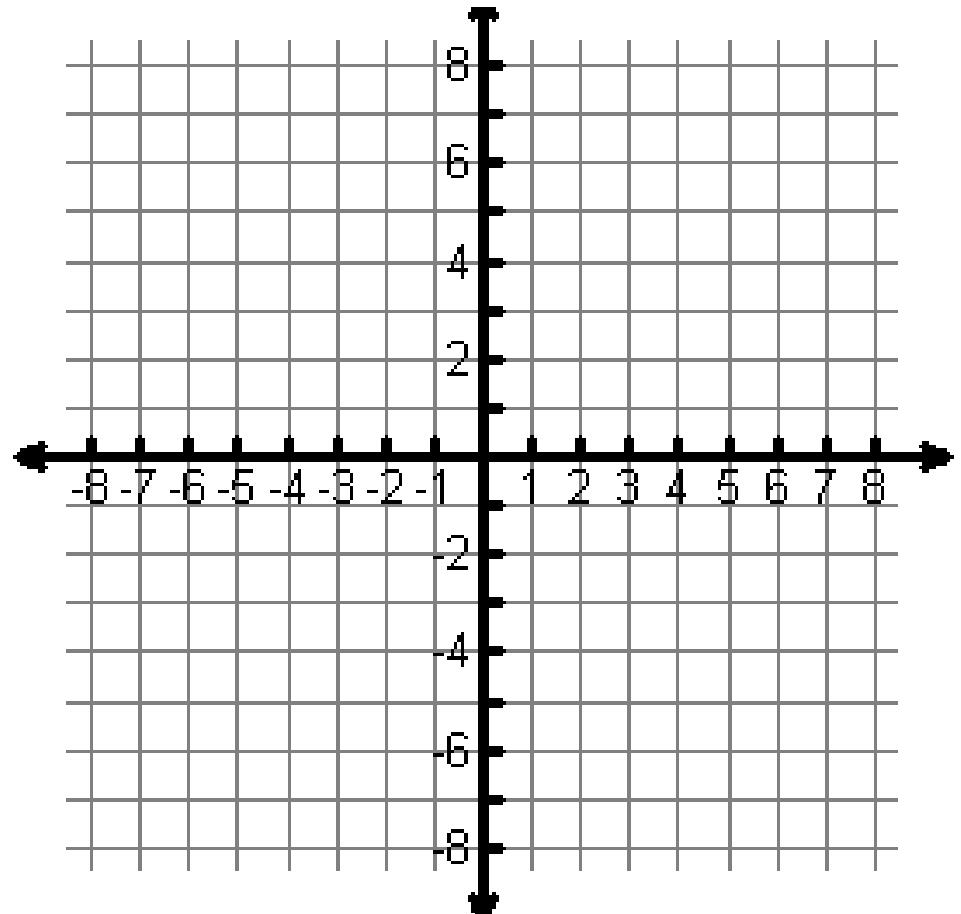
$(-1, 3)$



3. Graph to find the solution.

$$x + y = -2$$

$$2x - 3y = -9$$



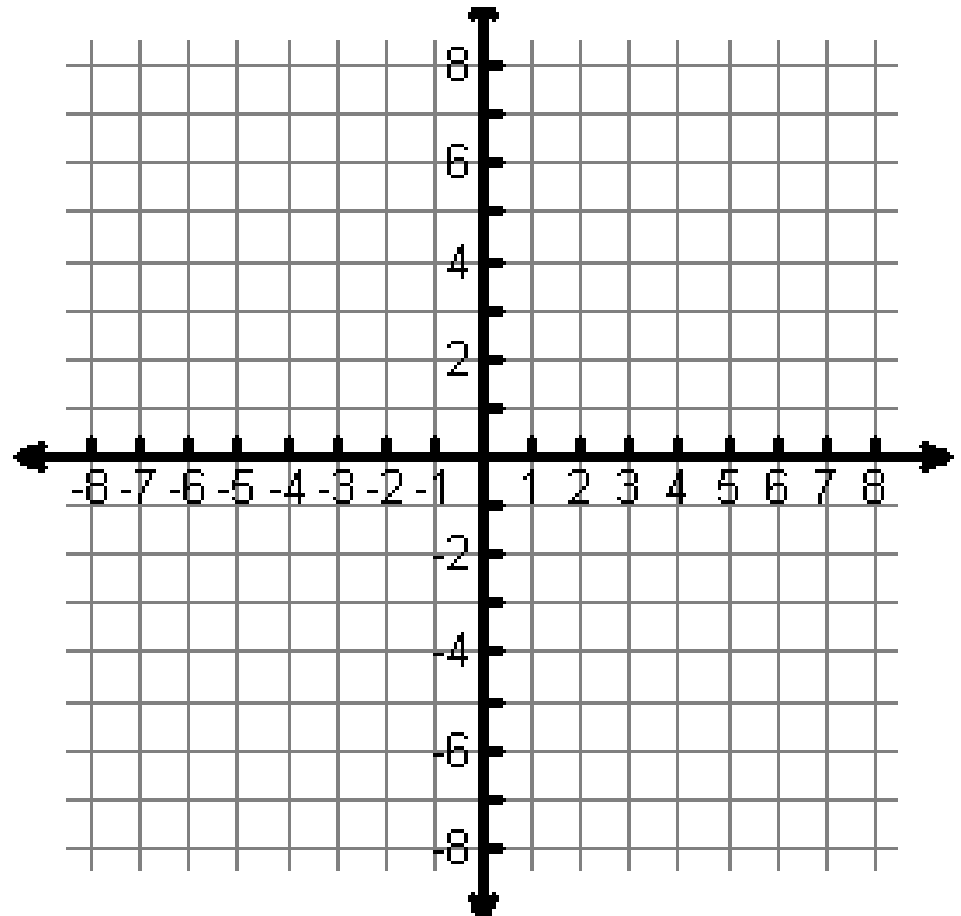
Solution:

$(-3, 1)$

4. Graph to find the solution.

$$y = 5$$

$$2x + y = 1$$



Solution:

$(-2, 5)$

Types of Systems

∞ There are 3 different types of systems of linear equations

3 Different Systems:

- 1) Infinite Solutions
- 2) No Solution
- 3) One solution

So basically....

∞ If the lines have the same y -intercept b , and the same slope m , then the system has **Infinite Solutions.**

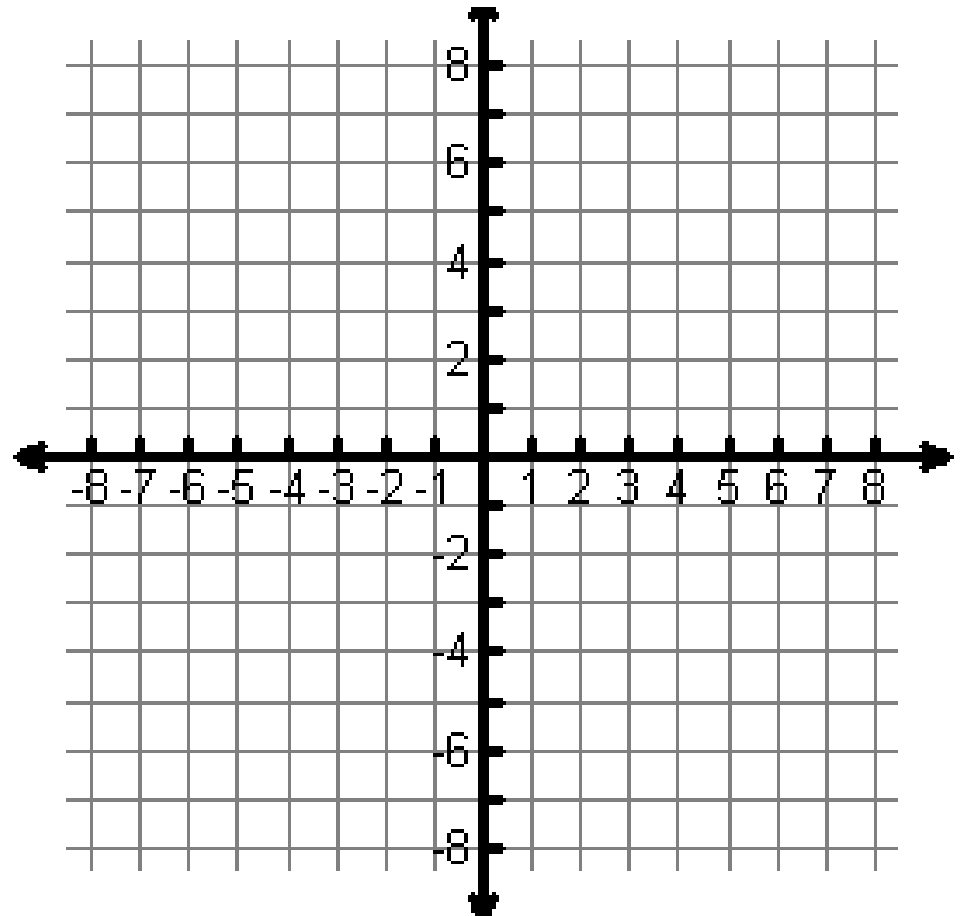
∞ If the lines have the same slope m , but different y -intercepts b , the system has **No Solution.**

∞ If the lines have different slopes m , the system has **One Solution.**

4. Graph to find the solution.

$$y = 5$$

$$2x + y = 1$$



Solution:

$(-2, 5)$

Opener

Finish Graphing to Perfection

Solve Systems of Equations by Substitution

Steps

1. One equation will have either x or y by itself, or can be solved for x or y easily.
2. Substitute the expression from Step 1 into the other equation and solve for the other variable.
3. Substitute the value from Step 2 into the equation from Step 1 and solve.
4. Your solution is the ordered pair formed by x & y .
5. Check the solution in each of the original equations.

Solve by Substitution

1. $x = -4$

$$3x + 2y = 20$$

1. $(-4, 16)$

Solve by Substitution

$$2. \quad y = x - 1$$

$$x + y = 3$$

$$2. \quad (2, 1)$$

Solve by Substitution

$$3. \quad 3x + 2y = -12$$

$$y = x - 1$$

$$3. \quad (-2, -3)$$

Solve by Substitution

$$4. \quad x = \frac{1}{2}y - 3$$

$$4x - y = 10$$

$$4. \quad (8, 22)$$

Solve by Substitution

$$5. \quad x = -5y + 4$$

$$3x + 15y = -1$$

5. No solution

Solve by Substitution

$$6. \quad 2x - 5y = 29$$

$$x = -4y + 8$$

$$6. \quad (12, -1)$$

Solve by Substitution

$$7. \quad x = 5y + 10$$

$$2x - 10y = 20$$

7. Many solutions

Solve by Substitution

8. $2x - 3y = -24$

$$x + 6y = 18$$

9. $(-6, 4)$

CW/HW

$$\begin{aligned} 1. \quad & y = 6x - 11 \\ & -2x - 3y = -7 \end{aligned}$$

$$\begin{aligned} 2. \quad & 2x - 3y = -1 \\ & y = x - 1 \end{aligned}$$

$$\begin{aligned} 3. \quad & y = -3x + 5 \\ & 5x - 4y = -3 \end{aligned}$$

$$\begin{aligned} 4. \quad & -3x - 3y = 3 \\ & y = -5x - 17 \end{aligned}$$

$$\begin{aligned} 5. \quad & y = -2 \\ & 4x - 3y = 18 \end{aligned}$$

$$\begin{aligned} 6. \quad & y = 5x - 7 \\ & -3x - 2y = -12 \end{aligned}$$

HW



Graphing and Substitution WS