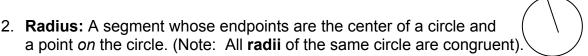
CIRCLES

Terms and Vocabulary:

1. **Circle:** The set of all points in a plane that are equidistant from a fixed point called the **center.**

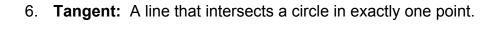


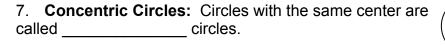
3. **Chord:** A segment whose endpoints are 2 points *on* a circle.



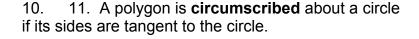


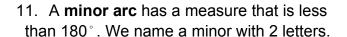
5. **Diameter:** A chord that passes through the center of a Circle.





- 8. Congruent Circles: have congruent radii.
- 9. A polygon is **inscribed** in a circle if its sides are chords of the circle.

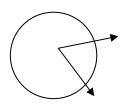




- 12. A **major arc** arc has a measure that is greater than 180°. We name a major arc with 3 letters.
- 13. A **semicircle** is an arc whose endpoints are the endpoints of a diameter. It has a measure of 180°. We name a semicircle with 3 letters.

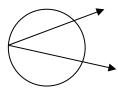
14. **Central Angle:** An angle whose vertex is the center of a circle.





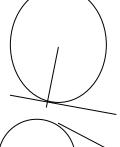
15. **Inscribed Angle:** An angle whose vertex is a point *on* a circle and whose sides contain chords.

The measure of an **inscribed angle** is **half** of the measure of its intercepted arc.



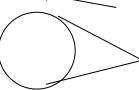
According to theorems:

16.



A radius drawn to a tangent at the point of tangency is **perpendicular** to the tangent.

17.



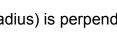
Tangent segments from an

exterior point to a circle are congruent.

- 18. In a circle, or in congruent circles, congruent central angles intercept congruent arcs.
- 19. In a circle, or in congruent circles, **congruent chords** intercept congruent arcs .



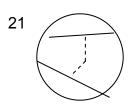
20. If a diameter (or radius) is perpendicular to chord,



then it **bisects** the chord and it **bisects** its arcs.

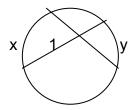


(Converse is also true).



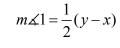
In the same circle (or congruent circles) two Chords are congruent if they are **equidistant** Form the center. (Converse is true)

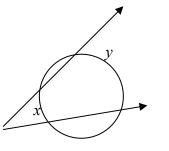
- 22. If two inscribed angles intercept the same arc, then they are congruent.
- 23. If an angle is inscribed in a **semicircle** then it is a right angle.
- 24. If a quadrilateral can be inscribed in a circle then both pairs of its opposite angles are supplementary.
- 25. The measure of an angle formed by a tangent and a chord/secant intersecting at the point of tangency is equal to **half** measure of the intercepted arc.
- 26. If 2 chords intersect in a circle, the measure of each angle is equal to $\frac{1}{2}$ the sum of the intercepted arcs made by the angle and its vertical angle.



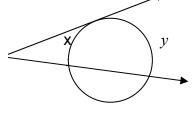
$$m \measuredangle 1 = \frac{1}{2}(x+y)$$

27. If an angle is formed such as one of the above:

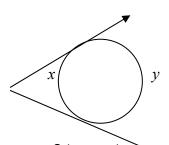




2 secants

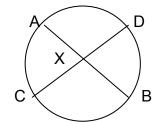


secant and tangent



2 tangents

28

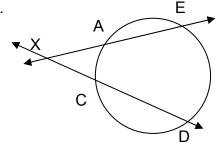


If 2 chords \overline{AB} and \overline{CD} intersect inside a Circle at point X then lengths

(lengths)
$$AX \cdot XE = CX \cdot XD$$

(Hint: It comes from similar triangles)

29.



If 2 secants intersect outside of a circle at X:

(lengths)
$$AX \cdot XE = CX \cdot XD$$

(Hint: It comes from similar triangles).