The 70 most common math skills from the last 10 SATs

Some things show up all the time on the SAT. Other things don't. I need to know this information in order to make the questions and question-selection algorithms for <u>Mathchops</u>. So I went through every question from the last 10 released SATs and figured out which skills showed up. Then one of my partners helped me make a Python script and we did a bunch of data analysis. What follows is a list of the most common types. The number in parentheses refers to how many times it showed up (out of 580 questions).

Slope (65 times) – Use the slope formula. Go back and forth from equation to graph. Find the equation when given two points. Find the slope based on a word problem.

System of equations (50) – Substitution, elimination, multiply then eliminate.

Y-intercept (49) – Usually either asking you to plug in 0 for x or figure it out based on the wordy description.

Plug in (46) – You have a value or a point that needs to be plugged into an equation or function.

Algebra translation (46) – Convert a word problem into an equation.

Ratio (33) – Part:part, part:whole.

Percent (32) – All variations: basic, increase/decrease, markup, discount.

Functions (31) – The basic f(x) notation is used extensively.

Tables (30) – Other question types (slope, probability) are presented in table form.

Combine like terms (29) – Frequently included in other question types.

Read the graph (27) – Many are quite basic questions, like finding the highest point on a line graph.

Distribute (25) – As in 3(x + 2) = 3x + 6.

Fractions (24) – Evenly split between calculator and non-calculator, but usually a part of something else. You would not be directly tested on something like 3/4 + 5/7.

Exponential growth (21) – Be comfortable with this: Final = Initial(1+/- rate)[^]time. Sometimes there are fractional exponents.

Factoring (20) – The basics, plus zero product property, difference of two squares, perfect square trinomials, factor by grouping, u-substitution.

Radicals (20) – Arithmetic operation, translate to fractional power, solve as part of an equation. **Median (20)** – Presented lots of ways: word problem, table, box and whisker plot, value/frequency histogram.

Slope formula (19) – Find the slope when given two points.

Meaning of a constant (18) – Usually a slope or y-intercept in a word problem.

Line of best fit (18) – These are usually just slope questions. Sometimes they ask about specific points.

Answer is not x (18) – You might solve for x but then be asked, "What is 2x - 3?"

Pick numbers (15) – This is never required but is often helpful.

Probability (14) – Almost all probability questions are in the form of table data. The key is to identify the numerator and the denominator: "What is the probability of selecting a female from the group of left-handed students?"

Isolate variable (13) – These usually require several algebraic moves (+/- from both sides, factor something out).

FOIL (13) – Usually just the basics, as in (x+3)(x-4).

Questions about a study (13) – Often something about margin of error or the setup of the study.

Substitution (systems) (12) – If y = 3x + 2 and 3x + 4y = 10, what is the value of x? **Conversion (12)** – They give you the conversion but you have to execute it correctly (oz/pounds, \$5/pound, etc.)

Exponents (11) – All basic operations, fractional, negative.

Negatives (11) – Arithmetic, distributing the negative over a parenthesis. Like fractions, they aren't directly tested.

Similar triangles (11) – Set up a proportion based on similar triangles.

Average (11) – Arithmetic mean. Mostly basic but a few advanced ones, like the average sum trick.

Elimination (systems) (11) – If 2x + y = 10 and 2x - 3y = 2, what is the value of y? **Function shifts (11)** – Mostly parabolas. Sometimes helpful to know -b/2a.

Plug in zero for intercept (11) – If 3x + 4y = 24, what is the x-intercept? Equations and word problems.

Fractional exponent (10) – Rewrite radicals as fractional exponents and vice versa.

Plug in answers (10) – Like picking numbers, it's not required but it's often helpful.

Inequality (9) – Usually something like 2x + 8 < 12, although you sometimes have to graph a system of linear inequalities.

Angle chasing (9) – 180 in a line, 180 in a triangle, corresponding angles, vertical angles. **Square both sides (8)** – It's often better to plug in the answers but sometimes you have to square both sides to get rid of the radical.

Match constants (8) – If 3x + 4y = ax + by, what is a + b?

Given graph, find equation (7) – Usually a linear equation, testing your knowledge of slope and y-intercept.

Rectangle area (7) – Basic or part of an algebraic word problem, sometimes quadratic.

Algebra LCD (7) – Something like x/(x+2) + 2x/(x+3).

Distribute negative (6) – A common trap in equations.

No solution (6) – If ax + 4 = 5x + 8, what value of 'a' would result in zero solutions? **Box and whisker plot (6)** – Usually asks for the median or range. The toughest one asks you

to identify the correct plot based on the data.

Quadratic and linear system (6) – These almost always require the substitution method and sometimes involve other skills, like factoring.

Perpendicular (6) – Know that perpendicular lines have negative, reciprocal slopes.

30:60:90 (6) – Know the side/angle relationships for 30_60_90 triangles.

U-substitution (6) – An advanced factoring technique.

Infinite solutions (6) – If ax + 4 = 5x + 4, what value of 'a' would result in infinite solutions? **Standard deviation (6)** – Just know that S.D. is related to how spread out the data points are. **Factor out constant (6)** – As in converting 3x + 6 into 3(x+2). Usually part of the factoring process.

SOHCAHTOA (5) – Set up the basic ratios. Know that similar triangles have the same trig ratios. Sometimes combined with the Pythagorean Theorem.

Range (5) – Table, box and whisker plot, list of numbers.

Difference of two squares (5) – This has to be automatic – often part of something else.

Percent increase (5) - The price was \$20. Now it's \$28. What's the percent increase?

Value/frequency (5) – Bar graph or table. Usually part of a median or arithmetic mean question.

Percent decrease (5) – The price was \$80. Now it's \$60. What's the percent decrease?

Pythagorean theorem (5) – Often combined with SOHCAHTOA or similar triangles.

-b/2a (5) – Use this to find the x-coordinate of the vertex.

Perfect square trinomial (5) – Useful for completing the square. Sometimes required as part of a multistep solution.

Scales don't match (5) – The origin won't be included, or the scales increase at different rates. **Circle equation (5)** – Know horizontal and vertical shifts, how to find the radius. You sometimes need to complete the square.

Margin of error (5) – You just have to be familiar with the concept. You don't have to calculate it.

c = product of roots, **b** = -sum (4) – Use when in $x^2 + bx + c$ form. Usually not required but often helpful.

What happens when you add a number? (4) – Know how outliers affect the mean and median.

Imaginary numbers (4) – Usually i² = -1 or combining like terms.

X minus root is a factor (4) – If 3 is a root of a polynomial, then (x-3) is a factor of the polynomial.