

# Direct Variation

Warm Up

Problem of the Day

Lesson Presentation

Lesson Quizzes

# Direct Variation

## Warm Up

**1.** Regina walked 9 miles in 3 hours. How many miles did she walk per hour?

**3 mi per hour**

**2.** To make 3 bowls of trail mix, Sandra needs 15 ounces of nuts. How many ounces of nuts does she need for 1 bowl of trail mix?

**5 oz**

# Direct Variation

## Problem of the Day

Paul has earned \$60 from his paper route. Each day he earns \$3.50 more. How many days will it take for Paul's earnings to top \$100?

**12 days**

# Direct Variation

*Learn* to identify, write, and graph an equation of direct variation.

## Vocabulary

direct variation

constant of variation

# Direct Variation

Direct variation is a linear relationship between two variables that can be written in the form  $y = kx$  or  $k = \frac{y}{x}$ , where  $k \neq 0$ . The fixed number  $k$  in a direct variation equation is the constant of variation.

# Direct Variation

## Reading Math

You can read direct variation as "*y varies directly as x*" or "*y is directly proportional to x*" or "*y varies with x.*"

# Direct Variation

## Additional Example 1A: Identifying a Direct Variation from an Equation

Tell whether each equation represents a direct variation. If so, identify the constant of variation.

$$y + 8 = x$$

$$y + 8 = x$$

$$\underline{-8} = \underline{-8}$$

$$y = x - 8$$

*Solve the equation for  $y$ .  
Subtract 8 from both sides.*

The equation is not in the form  $y = kx$ , so  $y + 8 = x$  is not a direct variation.



# Direct Variation

## Additional Example 1B: Identifying a Direct Variation from an Equation

Tell whether each equation represents a direct variation. If so, identify the constant of variation.

$$3y = 2x$$

$$\frac{3y}{3} = \frac{2x}{3}$$

$$y = \frac{2}{3}x$$

*Solve the equation for  $y$ .  
Divide both sides by 3.*

*Write  $\frac{2x}{3}$  as  $\frac{2}{3}x$ .*

The equation is in the form  $y = kx$ , so the original equation  $3y = 2x$  is a direct variation.

# Direct Variation

## Check It Out: Example 1A

Tell whether each equation represents a direct variation. If so, identify the constant of variation.

$$y + 3 = 3x$$

$$\begin{array}{r} y + 3 = 3x \\ \underline{-3} \quad \underline{-3} \end{array}$$

*Solve the equation for  $y$ .  
Subtract 3 from both sides.*

$$y = 3x - 3$$

The equation is not in the form  $y = kx$ , so  $y + 3 = 3x$  is not a direct variation.

# Direct Variation

## Check It Out: Example 1B

**Tell whether each equation represents a direct variation. If so, identify the constant of variation.**

$$4y = 3x$$

$$\frac{4y}{4} = \frac{3x}{4}$$

$$y = \frac{3}{4}x$$

*Solve the equation for  $y$ .  
Divide both sides by 4.*

*Write  $\frac{3x}{4}$  as  $\frac{3}{4}x$ .*

The equation is in the form  $y = kx$ , so the original equation  $4y = 3x$  is a direct variation.

# Direct Variation

## Additional Example 2A: Identifying a Direct Variation from a Table

Tell whether each set of data represents a direct variation. If so, identify the constant of variation and then write the direct variation equation.

Price (c)	69	99	129
Weight (oz)	2	3	4

Find  $\frac{y}{x}$  for each ordered pair.

$$\frac{y}{x} = \frac{2}{69} \quad \frac{y}{x} = \frac{3}{99} = \frac{1}{33} \quad \frac{y}{x} = \frac{4}{129}$$

$k$  is not the same for each ordered pair.

The data does not represent a direct variation.

# Direct Variation

## Helpful Hint

In a direct variation where  $k$  is positive, when  $x$  increases,  $y$  also increases; when  $x$  decreases,  $y$  also decreases.

# Direct Variation

## Additional Example 2B: Identifying a Direct Variation from a Table

Tell whether each set of data represents a direct variation. If so, identify the constant of variation and then write the direct variation equation.

Inches	1	2	5
Centimeters	2.54	5.08	12.70

Find  $\frac{y}{x}$  for each ordered pair.

$$\frac{y}{x} = \frac{2.54}{1} = 2.54 \quad \frac{y}{x} = \frac{5.08}{2} = 2.54 \quad \frac{y}{x} = \frac{12.7}{5} = 2.54$$

$k = 2.54$  for each ordered pair.

The data represent a direct variation where  $k = 2.54$ .

The equation is  $y = 2.54x$

# Direct Variation

## Check It Out: Example 2A

Tell whether each set of data represents a direct variation. If so, identify the constant of variation and then write the direct variation equation.

Price (c)	5	10	15
Weight (lb)	2	3	4

Find  $\frac{y}{x}$  for each ordered pair.

$$\frac{y}{x} = \frac{2}{5}$$

$$\frac{y}{x} = \frac{3}{10}$$

$$\frac{y}{x} = \frac{4}{15}$$

$k$  is not the same for each ordered pair.

The data does not represent a direct variation.

# Direct Variation

## Check It Out: Example 2B

Tell whether each set of data represents a direct variation. If so, identify the constant of variation and then write the direct variation equation.

Meters	3	4	5
Miles	9	12	15

Find  $\frac{y}{x}$  for each ordered pair.

$$\frac{y}{x} = \frac{9}{3} = 3$$

$$\frac{y}{x} = \frac{12}{4} = 3$$

$$\frac{y}{x} = \frac{15}{5} = 3$$

$k = 3$  for each ordered pair.

The data represent a direct variation where  $k = 3$ .

The equation is  $y = 3x$

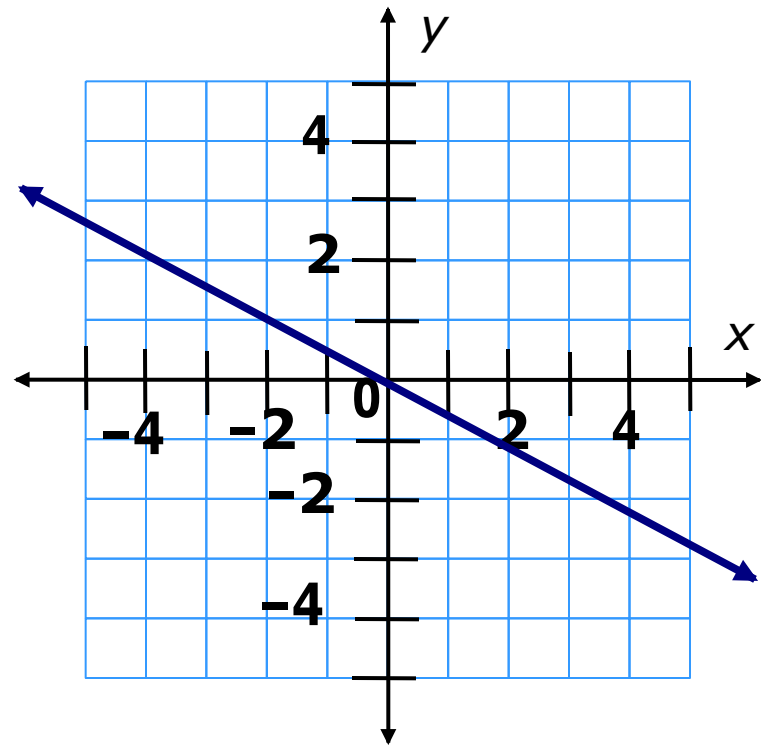


# Direct Variation

## Additional Example 3: Identifying a Direct Variation from a Graph

**Tell whether each graph represents a direct variation. If so, identify the constant of variation and then write the direct variation equation.**

The graph is a line through  $(0, 0)$ . This is a direct variation. The Slope of the line is  $\frac{1}{2}$ , so  $k = \frac{1}{2}$ . The equation is  $y = \frac{1}{2}x$ .



# Direct Variation

## Helpful Hint

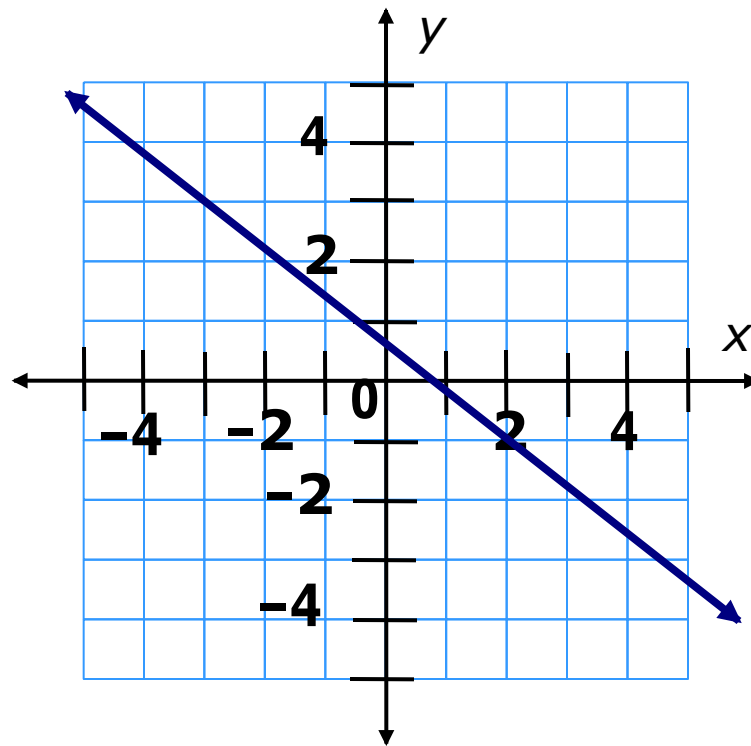
In a direct variation, the slope,  $k$ , represents a constant rate of change.

# Direct Variation

## Check It Out: Example 3

Tell whether each graph represents a direct variation. If so, identify the constant of variation and then write the direct variation equation.

The line does not pass through  $(0, 0)$ . This is not a direct variation.



# Direct Variation

## Additional Example 4A: *Application*

A truck travels at a speed of 55 miles per hour.

Write a direct variation equation for the distance  $y$  the truck travels in  $x$  hours.

distance = 55 miles per hour times number of hours

*Use the formula  $y = kx$ .  $k = 55$*

$$y = 55 \cdot x$$

$$y = 55x$$

# Direct Variation

## Additional Example 4B: *Application*

**A truck travels at a speed of 55 miles per hour.**

**Graph the data.**

Make a table. Since time cannot be negative, use nonnegative number for  $x$ .

$x$	$y = 55x$	$y$	$(x, y)$
0	$y = 55(0)$	0	(0, 0)
1	$y = 55(1)$	55	(1, 55)
2	$y = 55(2)$	110	(2, 110)

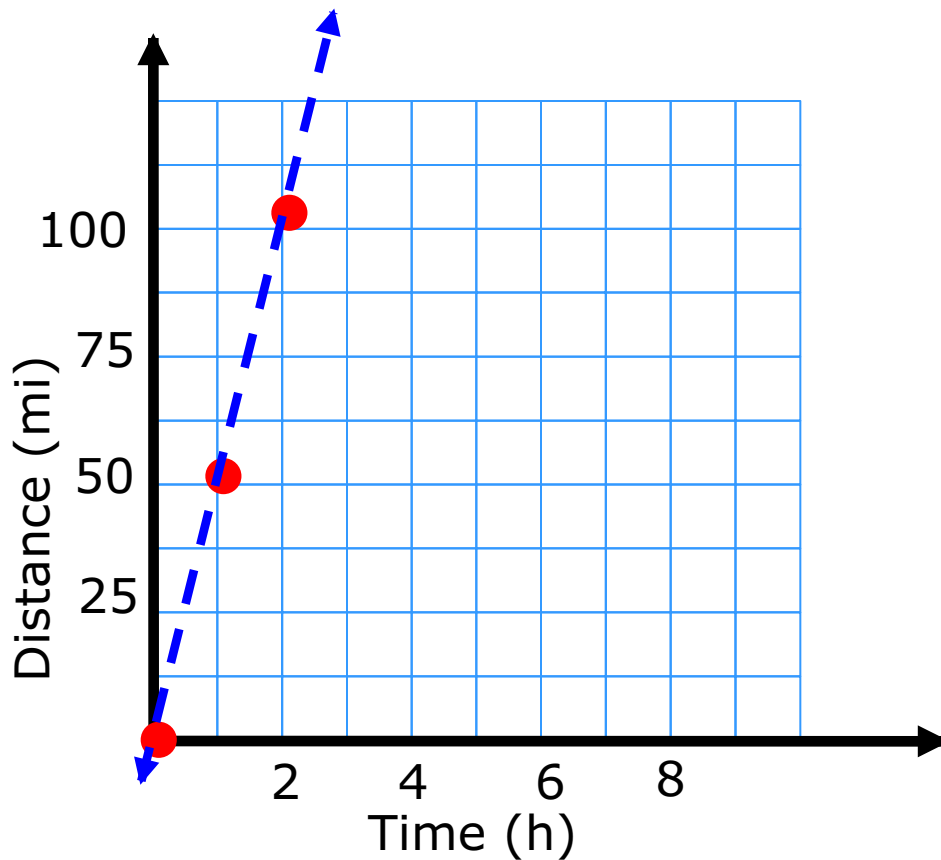
# Direct Variation

## Additional Example 4 Continued

Use the ordered pairs to plot the points on a coordinate plane. Connect the points in a straight line. Label the axes.

### Check

$y = 55x$  is in slope-intercept form with  $m = 55$  and  $b = 0$ . The graph shows a slope of 55 and a  $y$ -intercept of 0.



# Direct Variation

## Additional Example 4 Continued

**C.** How long does it take the truck to travel 660 miles?

Find the value of  $x$  when  $y = 660$

$$y = 55x$$

*Write the equation for the direct variation.*

$$\frac{660}{55} = \frac{55x}{55}$$

*Substitute 660 for  $y$ .*

*Divide both sides by 660.*

$$12 = x$$

It will take the truck 12 hours to travel 660 miles.

# Direct Variation

## Check It Out: Example 4A

A bicycle travels at a speed of 12 miles per hour.

Write a direct variation equation for the distance  $y$  the bike travels in  $x$  hours.

distance = 12 miles per hour times number of hours

*Use the formula  $y = kx$ .  $k = 12$*

$$y = 12 \cdot x$$

$$y = 12x$$



# Direct Variation

## Check It Out: Example 4B

**A bicycle travels at a speed of 12 miles per hour.**

**Graph the data.**

Make a table. Since time cannot be negative, use nonnegative number for  $x$ .

$x$	$y = 12x$	$y$	$(x, y)$
0	$y = 12(0)$	0	(0, 0)
1	$y = 12(1)$	12	(1, 12)
2	$y = 12(2)$	24	(2, 24)

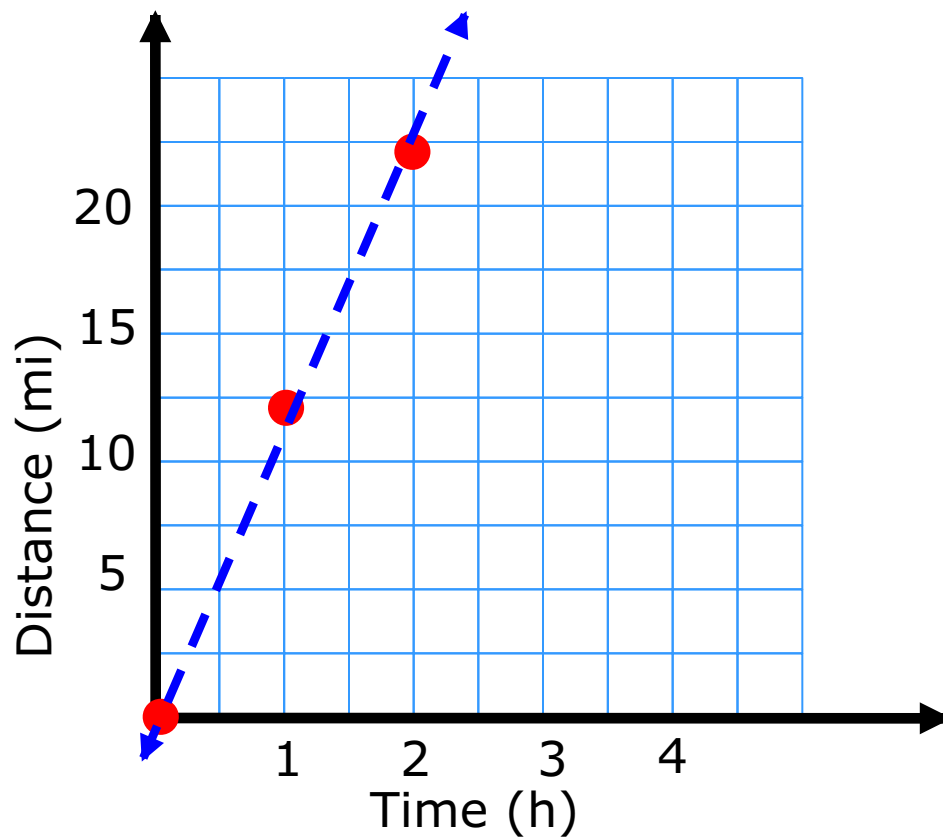
# Direct Variation

## Check It Out: Example 4 Continued

Use the ordered pairs to plot the points on a coordinate plane. Connect the points in a straight line. Label the axes.

### Check

$y = 12x$  is in slope-intercept form with  $m = 12$  and  $b = 0$ . The graph shows a slope of 12 and a  $y$ -intercept of 0.



# Direct Variation

## Check It Out: Example 4 Continued

**C.** How long does it take the bicycle to travel 96 miles?

Find the value of  $x$  when  $y = 96$

$$y = 12x$$

*Write the equation for the direct variation.*

$$\frac{96}{12} = \frac{12x}{12}$$

*Substitute 96 for  $x$ .*

*Divide both sides by 12.*

$$8 = x$$

It will take the bicycle 8 hours to travel 96 miles.

## Lesson Quizzes

Standard Lesson Quiz

Lesson Quiz for Student Response Systems

# Direct Variation

## Lesson Quiz: Part I

Tell whether each of the following represents a direct variation. If so, identify the constant of variation.

1.  $12y = 6x$      *yes;  $k = \frac{1}{2}$*

2.

Speed (mi/h)	40	50	60
Time (h)	7.5	6	5

*no*

# Direct Variation

## Lesson Quiz: Part II

3. A cheetah runs at a speed of 0.75 miles per minute.

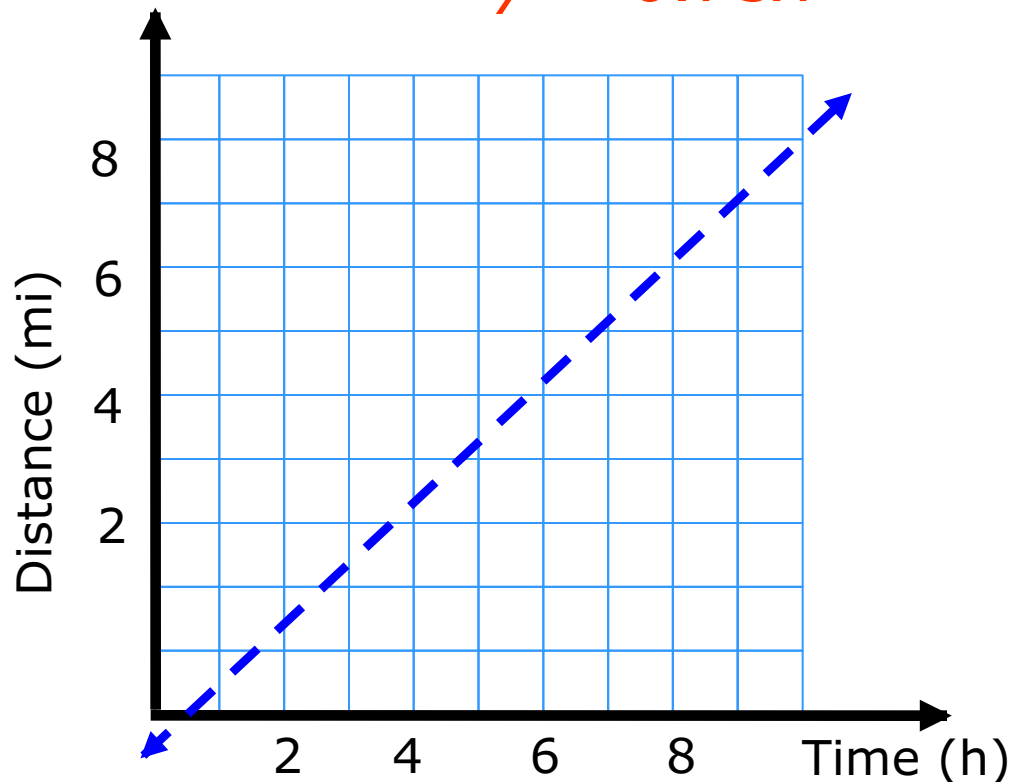
a. Write a direct variation equation for the distance  $y$  the cheetah runs in  $x$  minutes.

$$y = 0.75x$$

b. Graph the data.

c. How far does the cheetah run in 5 minutes?

3.75 miles



# Direct Variation

## Lesson Quiz for Student Response Systems

1. Tell whether the equation represents a direct variation. If so, identify the constant of variation.

$$y = 1.5x$$

A. yes;  $k = 0$

B. yes;  $k = 1$

C. yes;  $k = 1.5$

D. no

# Direct Variation

## Lesson Quiz for Student Response Systems

2. Tell whether the data set represents a direct variation. If so, identify the constant of variation.

Time (hr)	0	2	3	5
Distance (mi)	0	10	18	40

A. yes;  $k = 10$

B. yes;  $k = 5$

C. yes;  $k = 0$

**D.** no



# Direct Variation

## Lesson Quiz for Student Response Systems

3. An employee's pay is \$8.50 per number of hours worked. Write a direct variation equation for the amount  $y$  the employee gets in  $x$  number of hours. Graph the data. How much does the employee get in 8 hours?

A.  $y = 8.5x$ ; \$52 B.  $y = 8.5x$ ; \$68

