

Classifying Angles

Warm Up

Draw each figure.

1. line segment



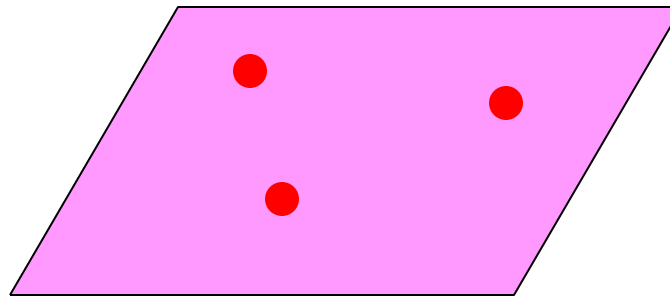
2. line



3. ray



4. plane



Classifying Angles

Module 11

Essential ?

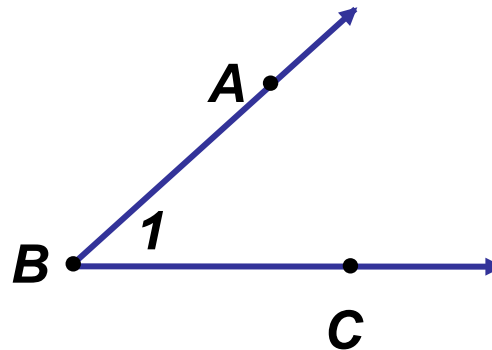
How can you use angles to identify lines, and find missing measures of angles?

Standard

MCC7.G.5: Use facts about supplementary, complementary, vertical, and adjacent angles in multi-step problem to write and solve simple equations for an unknown angle in a figure.

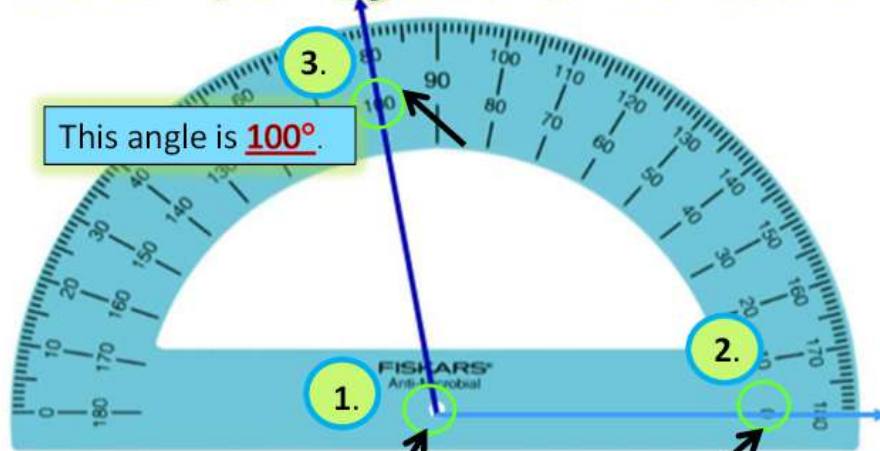
Classifying Angles

Reading Math



You can name this angle $\angle ABC$, $\angle CBA$, $\angle B$, or $\angle 1$.

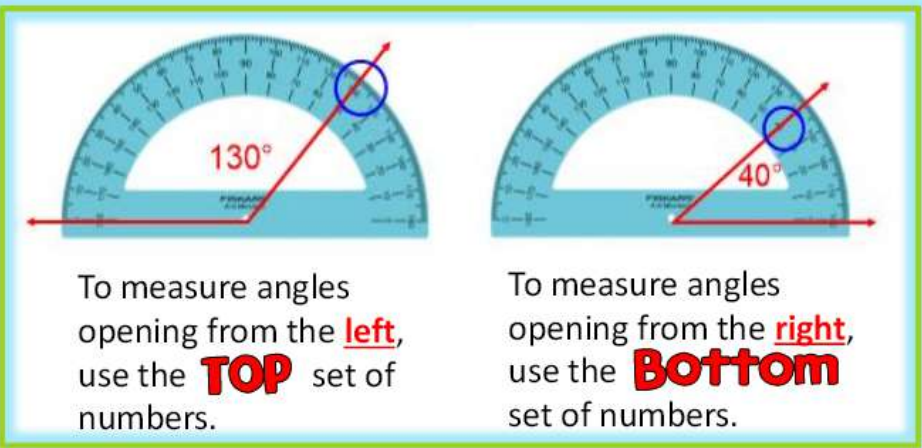
How To Use a Protractor



1. Place the center point of the protractor on the **vertex** of the angle.

2. Line up the **0 on the bottom line of the protractor** with the bottom ray of the angle.

3. To find the angle measure, **look at the number the second ray passes through.**



To measure angles opening from the **left**, use the **TOP** set of numbers.

To measure angles opening from the **right**, use the **BOTTOM** set of numbers.

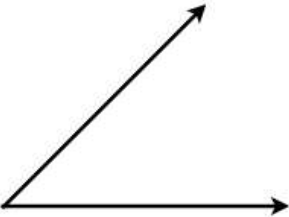
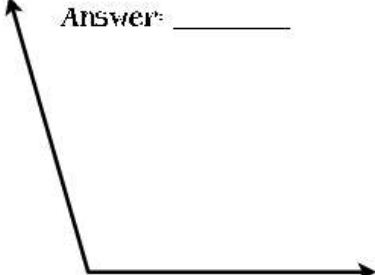
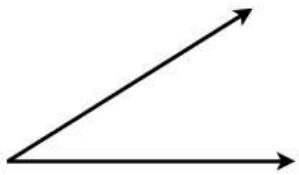
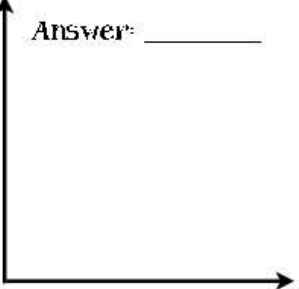
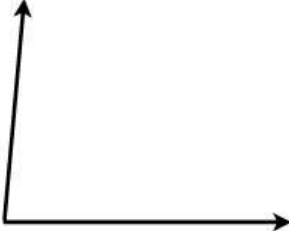

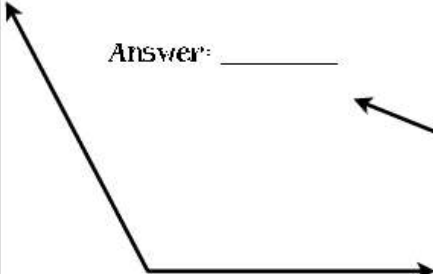

Glue in notebook.





Protractor Practice



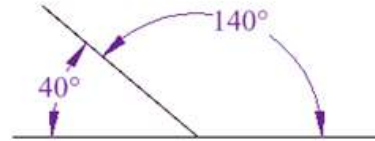
 <p>Answer: _____</p>	 <p>Answer: _____</p>
 <p>Answer: _____</p>	 <p>Answer: _____</p>
 <p>Answer: _____</p>	 <p>Answer: _____</p>
 <p>Answer: _____</p>	 <p>Answer: _____</p>

Supplementary Angles:

Two Angles are _____ if they **add up to** _____ **degrees**.

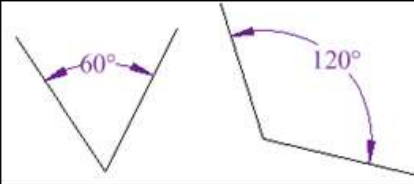
These two angles (140° and 40°) are Supplementary Angles, because they add up to **180°** .

Notice that together they make a straight angle, or straight line which is 180 degrees.



But the angles don't have to be together.

These two are supplementary because **$60^\circ + 120^\circ = 180^\circ$**



FUN TRICK TO REMEMBER:
"S" for Supplementary.... "S" makes 180!

S

PRACTICE PROBLEMS:

Two angles are supplementary and one of them is 31°
What is the size of the other angle?

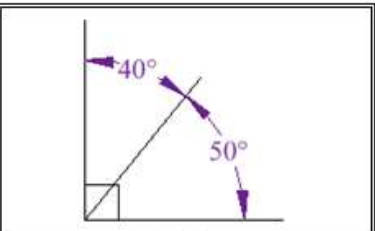
Two angles are supplementary and one of them is 127°
What is the size of the other angle?

Complementary Angles:

Two Angles are _____ if they **add up to** _____ **degrees** (Right Angle).

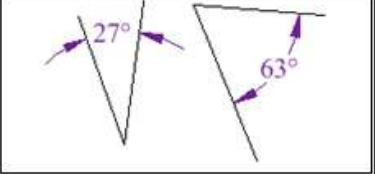
These two angles (40° and 50°) are **Complementary Angles**, because they add up to 90° .

Notice that together they make a right angle.



But the angles don't have to be together.

These two are complementary because $27^\circ + 63^\circ = 90^\circ$



FUN TRICK TO REMEMBER:
 "C" for Complementary.... "C" makes 90!
C

PRACTICE:

If two angles are complementary and one of them is 77° , what is the size of the other angle?

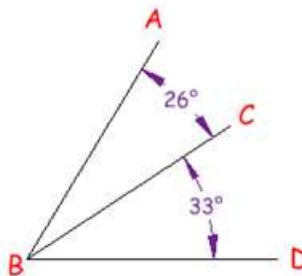
If two angles are complementary and one of them is 34° , what is the size of the other angle?

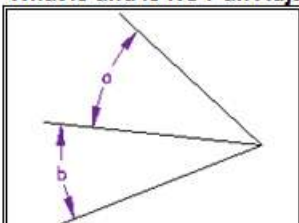
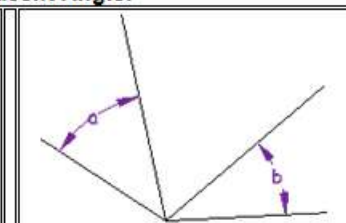
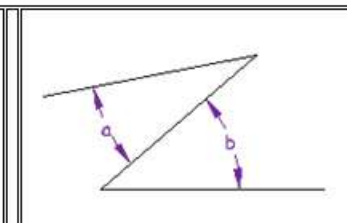
SOL 8.6 Notes – Adjacent Angles**Adjacent Angles:**

Two angles are _____ if they have a common side, a common vertex (corner point) and do not overlap.

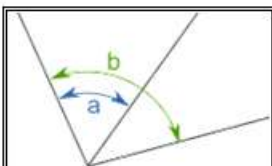
Angle ABC is adjacent to angle CBD because:

- they have a common side (line CB)
- they have a common vertex (point B)

**What Is and Is NOT an Adjacent Angle:**

		
These ARE Adjacent Angles	NOT Adjacent Angles	NOT Adjacent Angles
They share a vertex <i>and</i> a side	they only share a vertex, <i>not</i> a side	they only share a side, <i>not</i> a vertex

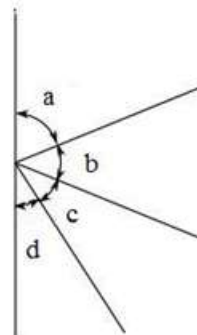
Don't Overlap!
The angles must not overlap.



NOT Adjacent Angles
angles a and b overlap

PRACTICE:

Which of the following pairs of angles are NOT adjacent?



Name: _____

Date: _____

NOTES – SOL 8.6 – Vertical Angles

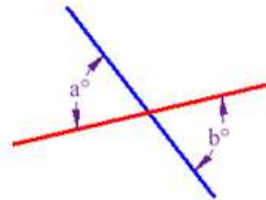
_____ are the angles opposite each other when two lines cross.

"Vertical" in this case means they **share the same Vertex** (or corner point), not the usual meaning of up-down.

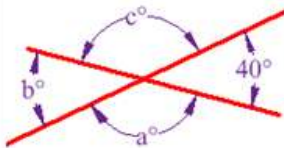
In this example, a° and b° are vertical angles.

Vertical angles are ALWAYS _____.

$$a^\circ = b^\circ$$



EXAMPLE: Find angles a° , b° and c° below:



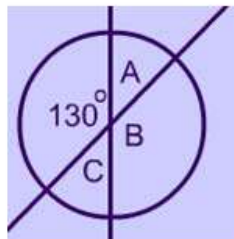
Because b° is opposite 40° , it must also be _____.

A full circle is _____ $^\circ$, so that leaves $360^\circ - 2 \times 40^\circ = 280^\circ$

Angles a° and c° are also vertical angles, so must be equal, which means they are 140° each.

Answer: $a = 140^\circ$, $b = 40^\circ$ and $c = 140^\circ$.

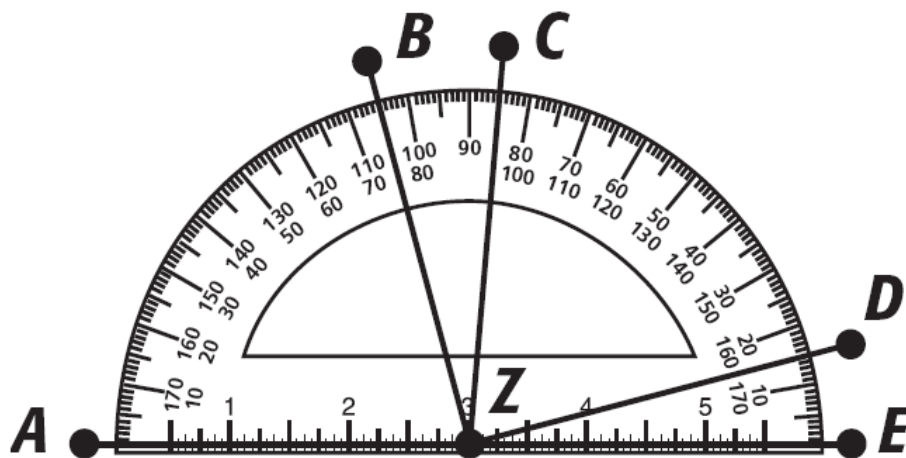
PRACTICE PROBLEM: What is the measure of angles a° , b° and c° below?



Classifying Angles

Lesson Quiz: Part II

Use the diagram to tell whether the angles are complementary, supplementary, or neither.



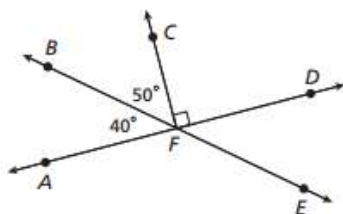
- $\angle AZB$ and $\angle BZC$ **neither**
- $\angle BZC$ and $\angle CZD$ **complementary**
- Angles M and N are supplementary. If $m\angle M$ is 117° , what is $m\angle N$? **63°**

are supplementary.

MCC7.G.5

2 EXAMPLE Identifying Angles and Angle Pairs

Use the diagram below.



- A** Name a right angle. _____
- B** Name a pair of adjacent angles. _____
- C** Name a pair of complementary angles. _____
- D** Name an angle that is supplementary to $\angle CFE$. _____
- E** Name an angle that is supplementary to $\angle BFD$. _____
- F** Name an angle that is supplementary to $\angle CFD$. _____
- G** Name a pair of non-adjacent angles that are complementary. _____

REFLECT

2a. What is the measure of $\angle DFE$? Explain how you found the measure.

2b. Are $\angle CFB$ and $\angle DFE$ adjacent angles? Why or why not?

2c. Are $\angle BFD$ and $\angle AFE$ adjacent angles? Why or why not?

Classifying Angles

Additional Example 3: Finding Angle Measures

Angles A and B are complementary. If $m\angle A$ is 56° , what is the $m\angle B$?

Since $\angle A$ and $\angle B$ are complementary, $m\angle A + m\angle B = 90^\circ$.

$$m\angle A + m\angle B = 90^\circ$$

$$56^\circ + m\angle B = 90^\circ$$

$$\begin{array}{r} - 56^\circ \\ \hline \end{array}$$

$$m\angle B = 34^\circ$$

Substitute 56° for $m\angle A$.

Subtract 56° from both sides.

The measure of $\angle B = 34^\circ$.

Classifying Angles

Check It Out: Example 3

Angles P and Q are supplementary. If $m\angle P$ is 32° , what is the $m\angle Q$?

Since $\angle P$ and $\angle Q$ are supplementary, $m\angle P + m\angle Q = 180^\circ$.

$$m\angle P + m\angle Q = 180^\circ$$

$$32^\circ + m\angle Q = 180^\circ$$

$$\begin{array}{r} 32^\circ + m\angle Q = 180^\circ \\ - 32^\circ \quad \quad - 32^\circ \\ \hline \end{array}$$

$$m\angle Q = 148^\circ$$

The measure of $\angle Q = 148^\circ$.

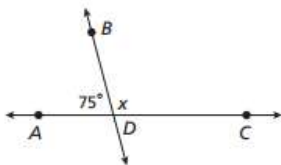
Substitute 32° for $m\angle P$.

Subtract 32° from both sides..

3 EXAMPLE Finding Angle Measures

Find the measure of each angle.

A $\angle BDC$



$\angle BDC$ and _____ are _____ angles.

The sum of their measures is _____.

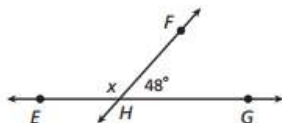
Write an equation to help you find the measure of $\angle BDC$.

$75 + x =$ _____

In the box, solve the equation for x .

$m\angle BDC =$ _____.

B $\angle EHF$



$\angle EHF$ and _____ are _____ angles.

The sum of their measures is _____.

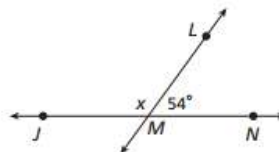
In the box, write and solve an equation to help you find $m\angle EHF$.

$m\angle EHF =$ _____.

TRY THIS!

3a. Find the value of x , and $m\angle JML$.

$m\angle JML = x =$ _____.



PRACTICE

For 1–5, use the figure.

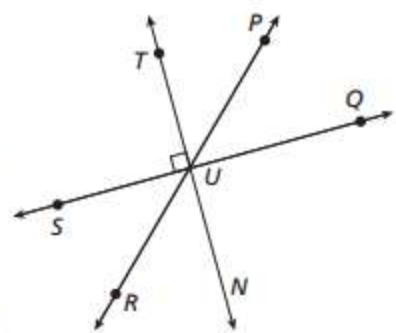
1. $m\angle QUP + m\angle PUT =$ _____

2. Name a pair of supplementary angles.

3. Name a pair of complimentary angles.

4. Name a pair of adjacent angles.

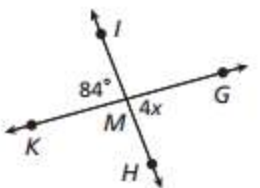
5. What is the measure of $\angle QUN$? Explain your answer.



Solve for the indicated angle measure or variable.

6. $m\angle YLA =$ _____

7. $x =$ _____



8. The railroad tracks meet the road as shown. The town will allow a parking lot to be built on the side of the road that is perpendicular to the railroad tracks.



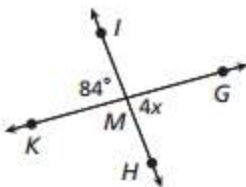
5. What is the measure of $\angle QUN$? Explain your answer.

Solve for the indicated angle measure or variable.

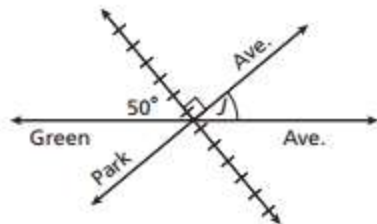
6. $m \angle YLA =$ _____



7. $x =$ _____

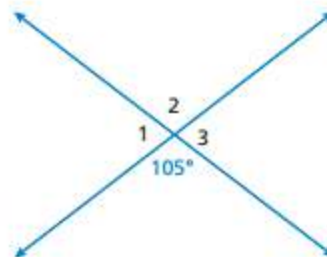


8. The railroad tracks meet the road as shown. The town will allow a parking lot at angle J if the measure of angle J is greater than 38° . Can a parking lot be built at angle J ? Why or why not?



9. **Error Analysis** A student states that when the sum of two angle measures equals 180° , the two angles are complementary. Explain why the student is incorrect.

The figure is formed by a pair of intersecting lines.
Use the figure for each problem.



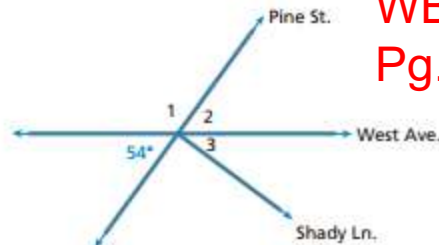
1. Use a protractor to find the measures of $\angle 1$, $\angle 2$, and $\angle 3$.

$m\angle 1 =$ _____, $m\angle 2 =$ _____, and $m\angle 3 =$ _____

2. Explain how you could find the measure of $\angle 1$ without using a protractor.

3. Explain how you could find the measure of $\angle 2$ without using a protractor.

The figure shows the intersection of Pine Street, West Avenue, and Shady Lane. Use the figure for each problem.



4. Write and solve an equation to find the measure of $\angle 1$.

5. What is the measure of $\angle 2$? Justify your answer without using a protractor.

6. $\angle 2$ and $\angle 3$ are complementary angles. Write and solve an equation to find the measure of $\angle 3$.

Homework:
WB Pg. 275 Even
Pg. 279 All