

Polynomial Synthetic Division

Synthetic Division can be used to factor or divide polynomials when the _____ is a _____ $(x - k)$.

A Divide: $5x^3 + 17x^2 + 7x + 3$ by $(x+3)$	STEPS: <i>in your own words</i>
$(x + 3) = (x - (-3))$	①
$\begin{array}{r} \underline{-3} \quad 5 \quad 17 \quad 7 \quad 3 \\ \hline \end{array}$	②
$\begin{array}{r} \underline{-3} \quad 5 \quad 17 \quad 7 \quad 3 \\ \quad \downarrow \quad -15 \\ \hline 5 \end{array}$	③
$\begin{array}{r} \underline{-3} \quad 5 \quad 17 \quad 7 \quad 3 \\ \quad \quad -15 \quad -6 \\ \hline 5 \quad 2 \end{array}$	④
$\begin{array}{r} \underline{-3} \quad 5 \quad 17 \quad 7 \quad 3 \\ \quad \quad -15 \quad -6 \quad -3 \\ \hline 5 \quad 2 \quad 1 \end{array}$	⑤
$\begin{array}{r} \underline{-3} \quad 5 \quad 17 \quad 7 \quad 3 \\ \quad \quad -15 \quad -6 \quad -3 \\ \hline 5 \quad 2 \quad 1 \quad \underline{0} \end{array}$	⑥
$\begin{array}{r} \underline{-3} \quad 5 \quad 17 \quad 7 \quad 3 \\ \quad \quad -15 \quad -6 \quad -3 \\ \hline 5 \quad 2 \quad 1 \quad \underline{0} \\ \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \\ 5x^2 + 2x + 1 \quad R0 \end{array}$	⑦ Write the quotient. Begin writing the quotient with a power of x that is one less than the greatest power of x in the dividend. The last number represents the remainder.
$(5x^3 + 17x^2 + 7x + 3) \div (x + 3) =$	

NOTES – POLYNOMIAL FUNCTIONS

B	Divide: $(-10x^3 + 83x^2 - 26x + 6) \div (x - 8)$		
Quotient:		Remainder:	

Quotient Notations with Remainders	
Remainder Notation	$(-10x^2 + 3x - 2), R - 10$
Polynomial Notation	$\left(-10x^2 + 3x - 2 - \frac{10}{x-8}\right)$ <div style="display: flex; justify-content: space-between; margin-top: 5px;"> ← Remainder ← Divisor </div>

C $(6x^3 + 12x^2 + 9) \div (x + 2)$ Missing a term	D $(6x^3 - 15x^2 + 60x - 22) \div (2x - 1)$ Divisor not in form $(x - k)$
$\begin{array}{r} \underline{-2} \\ 6 \\ 12 \\ 0 \\ 9 \\ \hline \end{array}$	$\begin{array}{r} \underline{\frac{1}{2}} \\ 6 \\ -15 \\ 60 \\ -22 \\ \hline \end{array}$

- | Remember the following when dividing polynomials using synthetic division: |
|---|
| <ol style="list-style-type: none"> ① Polynomials must be in _____ form (decreasing degree). ② All terms must be included, so if you have an x^4, then you must have an x^3. If there isn't an x^3 term, write ___ for the missing term. ③ Repeat the process of multiply and add until you determine the remainder. ④ Write the quotient with a power of x that is ___ less than the greatest power of x in the dividend. ⑤ The last number represents the remainder. If the remainder is 0, then the divisor is a _____ of the dividend. |