Agenda

Homework (AP)

Pg.106-10

Homework (reg)

Pg.142 #2.29

Pg.147 #2.32, 2.33

5 min

- Warm Up
- Checkup
 - Check, copies
- Introduce z
 - Activity w/ 2 types of nonsensical tests
 - Calculate mean & s.d., come back on E.P.
- Lecture, z-score
- Whiteboards, what's my z-score
- Using z-scores to calculate percentiles
- Exit Pass
 - Update!

10 min

10 min

20 min

5 min

Warm Up

Sketch a density curve that is:

- 1. Skewed left
- 2. Skewed right
- 3. Bimodal
- 4. Uniform
- 5. Symmetric but not uniform
- 6. Skewed right with an extreme outlier

7. Johnny scores in the 65th percentile on the Unit 1 quiz. What does that mean?

Check-up time

Z-scores (super-important)

- The "z-score" of an individual is the number of standard deviations away from the mean.
- The average American male weighs 170 pounds, with a standard deviation of 30 pounds. If I weigh 155 pounds, what is my z-score?

$$z = \frac{(observation - mean)}{s.d.} \qquad z = \frac{(x - x)}{\sigma}$$

Only with symmetric distributions. Why?

Example with quiz scores (P.1)

Awesomeness			
Angie	7		
Yuki	6		
Andrew	6		
Megha	5		
Jack	5		
Michael	4		
Daniel	4		
Levani	4		
Christian	4		
Jonathan	3		
Abdullah	3		
Brian	3		
Nina	2		

Mean	4.23	
St day	1 // Q	

Mean	3.69
St.dev	1.85

IQ			
Julia	8		
Harsh	5		
Belinda	5		
Elian	5		
Koa	4		
Keren	4		
Adeel	4		
Jada	4		
Megan	3		
Dip	2		
Sid	2		
Athena	2		
Gabby H.	1		

Example with quiz scores (P.3)

Awesomeness				
Rajesh	7			
Hassan	6			
Laura	6			
Vanessa	4			
Jade	4			
Julian	4			
Hollie	3			
Carolina	3			
Dylan	3			
Eliseo	2			
Tiarra	2			
Sangeeta	2			
Alfonso	2			
Eleny	2			
Diana	1			

Mean	3.4
St.dev	1.71

Mean	3.94
St.dev	1.14

IQ			
Maribel	6		
Ikram	5		
Drew	5		
Emily	5		
Lukas	4		
Aidan	4		
Ally	4		
Adam	4		
Hannah	4		
Alicia	4		
Charmay	4		
Mahek	4		
Fatima	4		
Olivia	3		
Celia	2		
Joven	1		

Door/Window....What's my z-score?

- Tell partner:
 - "The distribution has mean ____ and standard deviation ___."
 - "I'm ____."
 - "What is my z-score?"
- Each person practice <u>five times</u>.
- Example.

Do both.

Mr. Colligan weighed 13.9 lbs at 3 months. The national average for the weight of a 3-month baby is 12.5 lbs, with standard deviation 1.5 lbs.

1. Determine the z-score of Mr. Colligan's weight.

For a 6-month-old, the national average weight is 17.25 lbs, with a standard deviation of 2.0 lbs.

2. Determine what Mr. Colligan's weight would have been at age 6 months for him to have the same *z*-score that he did at 3 months.

Door/Window

Suppose that your score on an exam has a positive z-score compared to your classmates. Explain your answers to the following:

1. Is it possible that your score is below the mean score?

Window

2. Is it possible that your score is below the median score?

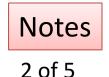
Door

3. Does this imply that your score is more than one standard deviation above the mean?

Window

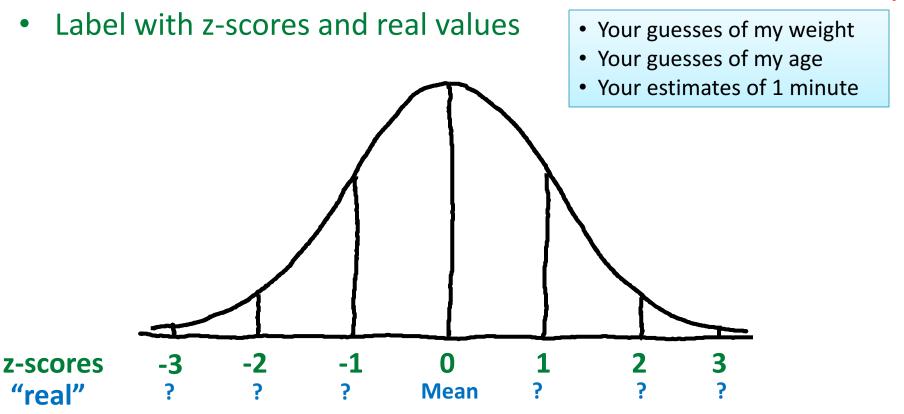
4. Is it possible that your score is the largest in the class?

Door



"Normal" Distribution (use with z)

- Symmetric, single-peaked, bell-shaped
 - Sometimes called "bell curve"
- Important because it describes lots of real-world situations
- BUT.....non-Normal data are common. Don't assume Normality.



Notes 3 of 5

Is it Normal?

- Option 1
 - It says so in the problem. Done.
- Option 2
 - Construct a normal quantile/prob. plot (graph type #6)

 $x axis \rightarrow x$ $y axis \rightarrow z$

Linear = Normal

- Option 3
 - Compare to Empirical rule

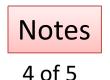
41	120
76	55
-10	7
-61	20
-13	95
22	-44
-16	1
-17	-37
8	-27
-50	-94
33	-57
-125	8
93	45
-84	-31
-10	69

n=17

Try it!

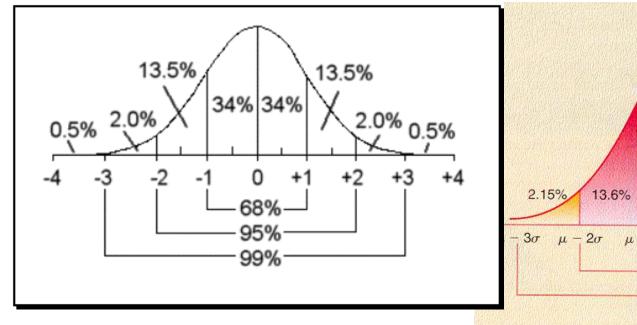
 Construct a normal quantile plot for the heights of my students.

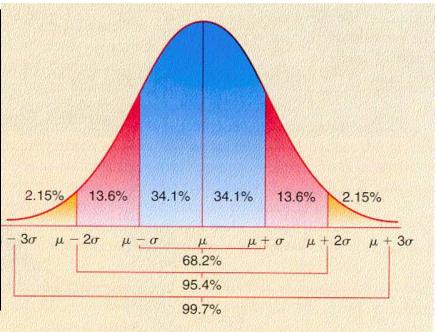
63.5



Empirical Rule (68-95-99)

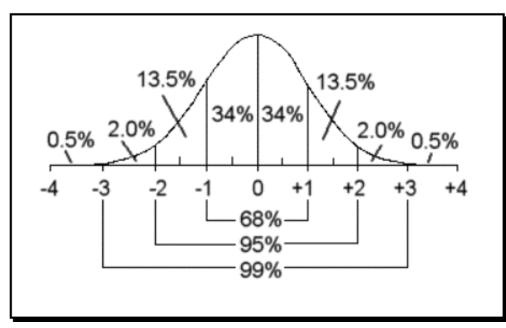
- In a Normal distribution with mean μ and standard deviation σ
 - A fair amount of data (68%) fall within one σ of μ
 - Lots of data (95%) fall within two σ of μ
 - Most data (99%) fall within three σ of μ





Using z-scores to get proportions

- Each SAT section is curved so μ =500 and σ =100 (which is awesome for AP Statistics teachers)
- I earn 600 on the Math portion. What is the z-score?
 - What is the *probability* of earning at least 600 on the Math section of the SAT?
- What is the probability of earning at least 625?



Using z-scores to get proportions

- A chart of standard Normal probabilities will tell you the area below any z-score
- Area = proportion = probability = percentile

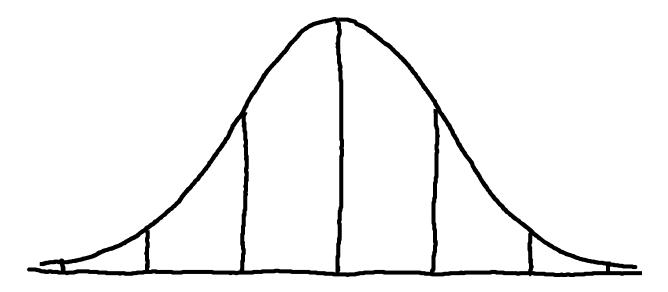


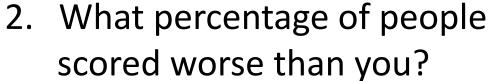
Table C (z-chart)

2						
12 6.	0	0.01	0.02	(0.03)	0.04	0.05
0	0.5	0.50399	0.50798	0.51197	0.51595	0.51994
0.1	0.53983	0.5438	0.54776	0.55172	0.55567	0.55962
0.2	0.57926	0.58317	0.58706	0.59095	0.59483	0.59871
0.3	0.61791	0.62172	0.62552	0.6293	0.63307	0.63683
0.4	0.65542	0.6591	0.66276	0.6664	0.67003	0.67364
0.5	0.69146	0.69497	0.69847	0.70194	0.7054	0.70884
0.6	0.72575	0.72907	0.73237	0.73565	0.73891	0.74215
0.7	0.75804	0.76115	0.76424	0.7673	0.77035	0.77337
.0.8	0.78814	0.79103	0.79389	0.79673	0.79955	0.80234
0.9	0.81594	0.81859	0.82121	0,82381	0.82639	0,82894
_1	0.84134	0.84375	0.84614	0.84849	0.85083	0.85314
1.1	0.86433	0.8665	0.86864	0.87076	0.87286	0.87493
1.2	0.88493	0.88686	0.88877	0,89065	0.89251	0.89435
1.3	0.9032	0.9049	0.90658	0.90824	0.90988	0.91149
1.4	0.91924	0.92073	0.9222	0.92364	0.92507	0.92647
1.5	0.93319	0.93448	0.93574	0.93699	0.93822	0.93943

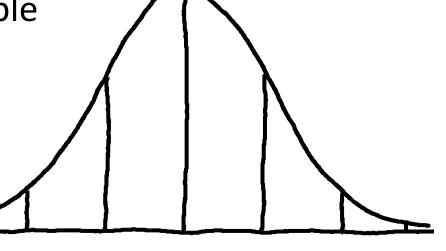
Using z-scores (example)

Each SAT test is curved so the mean 500 with σ =100. Let's say you score 625 on the SAT Math.

1. What is my z-score?
$$\frac{625-500}{100} = 1.25$$

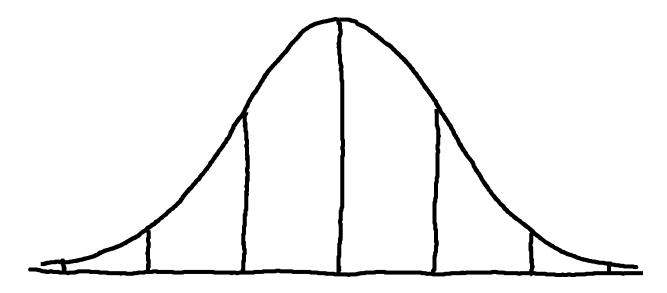


3. What is the probability of doing better than 625?



More examples

- 1. $z \le 1.5$
- 2. $z \ge 1.5$
- 3. $-1.5 \le z \le 1.5$
- 4. $-0.7 \le z \le 1.5$



Door/Window

- Door: Say any two z-scores between -3 and 3
- Door/Window: Find the probability of falling within those two z-scores.
- Door/Window: Compare answers.
- Window: Say two new z-scores between -3 and 3.
- Four times total.

Example of test problem

The heights of American men are approximately normally distributed, with a mean of μ =70 inches and a standard deviation of σ =3 inches. What percentage of American men are at least as tall as Mr. Colligan, who is 75 inches tall?

$$z = \frac{75-70}{3} = 1.67$$

Area under $1.67 \rightarrow .9525$ Area above $1.67 \rightarrow 1 - .9525 = .0475$

About 4.75% of American men are at least as tall as Mr. Colligan.

You try

The level of cholesterol in the blood is important because high cholesterol levels may increase the risk of heart disease. The distribution of blood cholesterol levels in a large population of people of the same age and sex is roughly Normal. For 14-year-old boys, the mean is μ =170 milligrams of cholesterol per deciliter of blood (mg/dl) and the standard deviation is σ =30 mg/dl. Levels above 240 mg/dl may require medical attention. What percent of 14-year-old boys have more than 240 mg/dl of cholesterol?

- 1. Draw and label a Normal curve.
- 2. Use the table to calculate the z-score and associated percentile.
- 3. State your conclusion in context.

Door/Window Competition

- Each of you writes a z-score on your whiteboard
- Show each other
- Calculate the area between those z-scores.
- Winner

 First with the correct answer written on their whiteboard.
- 3 rounds

Exit Pass (P.1)

Homework (AP) Pg.106-108 #11, 17, 25, 26

- 1. What is the standardized (z) score you earned on your quiz from the beginning of class? Also state which quiz you took, "IQ" or "Awesome".
- 2. What would you have to score to earn a z-score of 0 on your quiz?
- 3. What would you have to score to earn a z-score of 2 on your quiz?

Awesomeness		
Mean	5.15	
St.dev	1.79	

IQ			
Mean	4.67		
St.dev 1.45			

Awesomeness	
Imiich	7
Dimitry	6
Abbie L.	6
Gaby	6
Elena	6
Abby M.	6
Emmanuil	5
Maria	5
Rachel	4
Miranda	4
Carlos	4
Drew	3
Bella	3
Melody	3
Kaylee	2

IQ	
Manpreet	7
Jon	7
Julie	7
Daniel	7
Jusiah	6
Jenna	6
Reese	6
Itzel	5
Isaac	5
Maya	4
Shiyi	3
Kevin	2
Wendy	2