

Name _____

Solutions to Pre-AP Algebra II Summer Reading

Solutions to Quiz #1 - Summer Reading Packet

Upcoming MTA2W/T classes

1. Find the slope of the line which goes through the points $(2, -6)$ and $(-7, -12)$.

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{(-12) + (-6)}{(-7) - (2)} = \frac{-18}{-9} = \boxed{\frac{2}{3}}$$

2. What is the equation of a line, in point-slope form, that goes through the point $(3, -12)$ and has the slope $-\frac{2}{3}$.

$$y - y_1 = m(x - x_1) \quad \therefore \quad y - (-12) = -\frac{2}{3}(x - 3)$$

$$\boxed{y + 12 = -\frac{2}{3}(x - 3)}$$

3. Simplify:

$$x^4 \cdot x^7 = x^{4+7} = \boxed{x^{11}}$$

$$(3xy)^4 = 3^4 x^4 y^4 = \boxed{81x^4 y^4}$$

$$(2x^3)^4 = 2^4 \cdot x^{12} = \boxed{16x^{12}}$$

4. Simplify:

$$\frac{7x^8}{14x^9} = \boxed{\frac{1}{2x^3}}$$

$$\left(\frac{x^3}{2y}\right)^5 = \boxed{\frac{x^{15}}{32y^5}}$$

5. Simplify

$$(4x^9 y^3)^2 = \boxed{16y^6}$$

$$\frac{x^{-4}}{x^5} = \frac{1}{x^{5+4}} = \boxed{\frac{1}{x^9}}$$

$$\frac{x^{12}}{x^{-4}} = x^{12+4} = \boxed{x^{16}}$$

6. Factor

$$\cancel{64x^2 - 9y^2} \quad \begin{array}{c} \\ \swarrow \\ (8x + 3y)(8x - 3y) \end{array} \quad \begin{array}{c} x^2 - 6x - 7 \\ \begin{array}{c} \swarrow \\ (x-7)(x+1) \end{array} \end{array} \quad \begin{array}{c} 49x^2 + 28x + 4 \\ \begin{array}{c} \swarrow \\ (7x + 2)^2 \end{array} \end{array}$$

7. Solve using the Quadratic Formula.

$$5x^2 - 4x - 3 = 0$$

$$x = \frac{-(-4) \pm \sqrt{(-4)^2 - 4(5)(-3)}}{2(5)}$$

$$= \frac{4 \pm \sqrt{16 + 60}}{10} = \frac{4 \pm \sqrt{76}}{10}$$

$$= \frac{4 \pm 2\sqrt{19}}{10} = \boxed{\frac{2 \pm \sqrt{19}}{5}}$$

8. Find the distance between the following points:

$(2, -6)$ and $(-7, -12)$

$$D = \sqrt{(2 - (-7))^2 + (-6 - (-12))^2}$$

$$= \sqrt{9^2 + 6^2}$$

$$= \sqrt{81 + 36}$$

$$= \sqrt{117} = \boxed{3\sqrt{13}}$$

9. Find the Midpoint of the following points:

$$(2, -6) \text{ and } (-7, -12) \quad \left(\frac{2+(-7)}{2}, \frac{(-6)+(-12)}{2} \right) = \boxed{\left(-\frac{5}{2}, -9 \right)}$$

10. What is the discriminant of the following equation?

$$5x^2 - 4x - 3 = 0 \quad b^2 - 4ac \\ = (-4)^2 - 4(5)(-3) = 16 + 60 = \boxed{76}$$

11. Determine the harmonic mean of 12 and 15.

$$\frac{2(12)(15)}{12+15} = \frac{2 \cdot 12 \cdot 15}{27} = \boxed{\frac{40}{3}}$$

12. Using the formula from the packet, find the sum of the first 100 numbers $(1+2+3+\dots+100)$.

$$\frac{100(100+1)}{2} = \boxed{5050}$$

13. Using the formula from the packet, find the sum of the first 20 squares $(1^2 + 2^2 + 3^2 + \dots + 20^2)$.

$$\frac{20(20+1)(2 \cdot 20 + 1)}{6} = \frac{20 \cdot 21 \cdot 41}{6} = \boxed{2870}$$

14. Using the formula from the packet, find the sum of the first 15 cubes $(1^3 + 2^3 + 3^3 + \dots + 15^3)$.

$$\frac{15^2(15+1)^2}{4} = \frac{225(256)}{4} = \boxed{14400}$$

15. What is the law of sines you would use if you knew $\angle A$, $\angle C$, and side c ?

$$\frac{\sin A}{a} = \frac{\sin C}{c}$$

16. What is the law of cosines you would use if you wanted to solve for $\angle B$?

$$b^2 = a^2 + c^2 - 2ac \cdot \cos B$$

17. Simplify:

$$\frac{x}{r} = \cos \theta$$

$$\frac{y}{x} = \tan \theta$$

$$\frac{r}{y} = \csc \theta$$

$$\frac{1}{\csc \theta} = \sin \theta$$

$$\frac{1}{\cos \theta} = \sec \theta$$

$$\frac{1}{\sin \theta} = \csc \theta$$

$$\frac{\sin \theta}{\cos \theta} = \tan \theta$$

$$\frac{\cos \theta}{\sin \theta} = \cot \theta$$

18. Given the following polynomial, $f(x) = 5x^5 - 3x^4 + 2x^3 + 4x^2 - 7x + 12$, find the ...

Sum of the roots:

$$-\frac{b}{a} = -\frac{(-3)}{5}$$

$$= \boxed{\frac{3}{5}}$$

Product of the roots: *odd power*

$$-\frac{1 \text{ last}}{\text{first}} = -\frac{12}{5}$$

Sum of the squares of the roots:

$$\frac{b^2 - 2ac}{a^2} = \frac{(-3)^2 - 2(5)(2)}{5^2}$$

$$= \frac{9 - 20}{25} = \boxed{-\frac{11}{25}}$$

19. Given the following polynomial, $f(x) = 2x^8 - 5x^7 + 3x^3 + 7x^2 - 6x + 13$, find the ...

Sum of the roots:

$$-\frac{b}{a} = -\frac{(-5)}{2}$$

$$= \boxed{\frac{5}{2}}$$

Product of the roots: *even power*

$$+\frac{1 \text{ last}}{\text{first}} = \frac{13}{2}$$

Sum of the squares of the roots:

$$\begin{aligned} &\text{Since there is no "x"}^6 \text{ term,} \\ &\text{there is no "c" coefficient.} \\ \therefore \frac{b^2 - 2ac}{a^2} &= \frac{(-5)^2 - 2(2)(0)}{2^2} \\ &= \boxed{\frac{25}{4}} \end{aligned}$$

20. Find the sum of the measures of interior angles of a polygon with 12 sides:

$$\begin{aligned} (n-2)180^\circ &= (12-2)180^\circ \\ &= \boxed{1800^\circ} \end{aligned}$$

21. From the number 2520, find the ...

...number of positive integral factors.

$$\begin{aligned} 2^3 \cdot 3^2 \cdot 5^1 \cdot 7^1 &\therefore 4 \cdot 3 \cdot 2 \cdot 2 \\ &= \boxed{48} \end{aligned}$$

... number of integral factors. \therefore positive & negative

$$\begin{aligned} \therefore 48 \times 2 & \\ &= \boxed{96} \end{aligned}$$

...sum of the positive integral factors.

$$\begin{aligned} (2^3+2^2+2^1+2^0)(3^2+3^1+3^0)(5^1+5^0)(7^1+7^0) \\ (2^3+2^2+2^1+1)(3^2+3^1+1)(5+1)(7+1) \\ 15 \cdot 13 \cdot 6 \cdot 8 = \boxed{9360} \end{aligned}$$

...sum of the integral factors.

$$\begin{aligned} \text{positives} + \text{negatives} &= 0 \\ \therefore 9360 + (-9360) &= \boxed{0} \end{aligned}$$

22. Determine the number of diagonals of a convex polygon with 20 sides.

$$\frac{n}{2}(n-3) \quad \therefore \quad \frac{20}{2}(20-3) = 10 \cdot 17 = \boxed{170}$$

23. Determine the sum of the terms in the 12 row of Pascal's triangle.

$$\begin{array}{ccccccc} & & 1 & & 1 & & \\ & & 1 & 2 & 1 & & \\ & & 1 & 3 & 3 & 1 & \\ & & 1 & 4 & 6 & 4 & 1 \\ & & 1 & 5 & 10 & 10 & 5 & 1 \\ & & 1 & 6 & 15 & 20 & 15 & 6 & 1 \\ & & 1 & 7 & 21 & 35 & 35 & 21 & 7 & 1 \\ & & 1 & 8 & 28 & 56 & 70 & 56 & 28 & 8 & 1 \\ & & 1 & 9 & 36 & 84 & 126 & 126 & 84 & 36 & 9 & 1 \\ & & 1 & 10 & 45 & 120 & 210 & 210 & 120 & 45 & 10 & 1 \\ & & 1 & 11 & 55 & 165 & 330 & 462 & 462 & 330 & 165 & 55 & 11 & 1 \\ & & 1 & 12 & 66 & 220 & 495 & 792 & 924 & 792 & 495 & 220 & 66 & 12 & 1 \end{array}$$

$\therefore 2^{12} = \boxed{4096}$

"12 row"

24. Find the sum of the coefficients (and constants) in the expansion of $(3x^3 - 4y^2 + 5z - 2)^8$

$$(3-4+5-2)^8 = 2^8 = \boxed{256}$$

25. What are the first 4 perfect numbers?

$$6, 28, 496, 8128$$

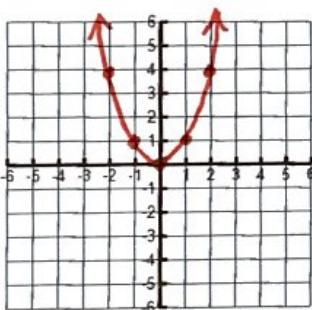
26. Write the following repeating decimal as a fraction in simplest terms.

$$5.\overline{1234}$$

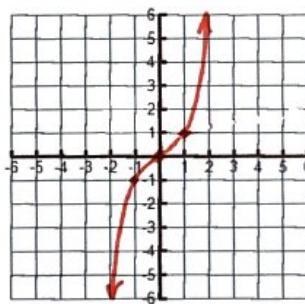
$$\frac{51234 - 512}{9900} = \frac{50722}{9900} = \boxed{\frac{25361}{4950}}$$

Graph the following:

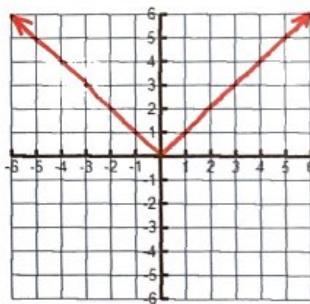
27. $y = x^2$



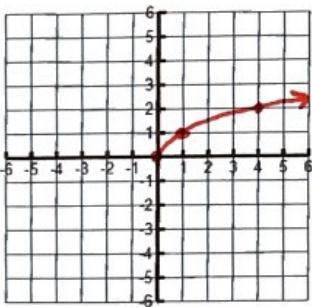
28. $y = x^3$



29. $y = |x|$



30. $y = \sqrt{x}$



31. $y = 2^x$

