

$$C) \int \frac{2}{2x^2 + 3x + 1} dx = \int \frac{4}{2x+1} + \frac{-2}{x+1}$$

$$\frac{2}{(2x+1)(x+1)} = \frac{A(x+1)}{(2x+1)(x+1)} + \frac{B(2x+1)}{(x+1)(2x+1)}$$

$$2 = A(x+1) + B(2x+1)$$

$$x = -1 \quad 2 = -B \quad B = -2$$

$$x = -\frac{1}{2} \quad 2 = \frac{1}{2}A \quad A = 4$$

$$= 2 \ln|2x+1| - 2 \ln|x+1| + C$$

$$\ln \left| \frac{(2x+1)^2}{(x+1)^2} \right| + C$$

$$\ln \left(\frac{2x+1}{x+1} \right)^2 + C$$

$$D) \int \frac{x^3 - 5}{x^2 - 1} dx$$

Since the ~~power~~ ^{degree} on bottom is not bigger than the top
- start with long division

$$\begin{array}{r} x \\ x^2 - 1 \overline{) x^3 - 5} \\ \underline{-x^3 + x} \\ x - 5 \end{array}$$

$$\frac{x^3 - 5}{x^2 - 1} = x + \frac{x-5}{x^2 - 1}$$

$$\frac{x-5}{(x+1)(x-1)} = \frac{A(x-1)}{(x+1)(x-1)} + \frac{B(x+1)}{(x-1)}$$

$$x-5 = A(x-1) + B(x+1)$$

$$x = 1 \quad -4 = 2B \quad B = -2$$

$$x = -1 \quad -6 = -2A \quad A = 3$$

$$= \left\{ x + \frac{3}{x+1} - \frac{2}{x-1} \right\} + C$$

$$\frac{1}{2}x^2 + 3 \ln|x+1| - 2 \ln|x-1|$$

$$\frac{1}{2}x^2 + \ln \left| \frac{(x+1)^3}{(x-1)^2} \right| + C$$

$$E) f'(x) = \frac{2x^3}{x^3 - x}$$