

What you will learn about:
Solving Quadratics by Square Roots

$$\text{Solve: } \sqrt{x^2} = \sqrt{81}.$$

$$x = \pm 9$$

$$\text{Solve: } \sqrt{y^2} = \sqrt{121}.$$

$$y = \pm 11$$

$$\text{Solve: } x^2 - 50 = 0.$$

$$\sqrt{x^2} = \sqrt{50}$$

$$x = \pm \sqrt{50} \\ = \pm 5\sqrt{2}$$

$$\text{Solve: } y^2 - 27 = 0.$$

$$y^2 = 27$$

$$y = \pm \sqrt{27} \\ = \pm 3\sqrt{3}$$

Solve: $c^2 + 12 = 0$

$$c^2 = -12$$

$$c = \pm\sqrt{-12} \text{ No Real Solution}$$

Solve: $d^2 + 81 = 0$

$$d^2 = -81$$

$$d = \pm\sqrt{-81} \text{ No Real Solution}$$

Solve: $\frac{2x^2}{2} = \frac{98}{2}$

$$x^2 = 49$$

$$x = \pm 7$$

Solve: $\frac{3z^2}{3} = \frac{108}{3}$

$$z^2 = 36$$

$$z = \pm 6$$

Solve: $\frac{2}{3}u^2 + 5 = 17$

$$\frac{3}{2} \left(\frac{2}{3} \right) u^2 = \left(12 \right) \frac{3}{2}$$

$$u^2 = 18$$

$$u = \pm 3\sqrt{2}$$

Solve: $\frac{1}{2}x^2 + 4 = 24$

$$\frac{1}{2}x^2 = 20$$

$$x^2 = 40$$

$$x = \pm\sqrt{40} = \pm 2\sqrt{10}$$

Solve: $\frac{3}{4}y^2 - 3 = 18$

$$\frac{4}{3}\left(\frac{3}{4}\right)y^2 = (21)\frac{4}{3}$$

$$y^2 = 28$$

$$y = \pm\sqrt{28}$$

$$\pm 2\sqrt{7}$$

Solve: $5r^2 - 2 = 34$

$$5r^2 = 36$$

$$\sqrt{r^2} = \sqrt{\frac{36}{5}}$$

$$r = \pm \frac{6}{\sqrt{5}} \frac{\sqrt{5}}{\sqrt{5}}$$

$$\pm \frac{6\sqrt{5}}{5}$$

Solve: $3t^2 + 6 = 70$

$$-6 \quad -6$$

$$3t^2 = 64$$

$$t^2 = \frac{64}{3}$$

$$t = \pm \frac{8}{\sqrt{3}}$$

$$= \pm \frac{8\sqrt{3}}{3}$$

Solve: $\sqrt{(q+5)^2} = \sqrt{1}$

$$q+5 = \pm 1$$

$$q = -4, -6$$

$$-5+1$$

$$-5-1$$

Solve: $\sqrt{(r-3)^2} = \sqrt{25}$

$$r-3 = \pm 5$$

$$r = 3 \pm 5$$

$$3+5 = 8$$

$$3-5 = -2$$

$$\text{Solve: } (a - 3)^2 = 18 \quad 3 \pm 3\sqrt{2}$$

$$a - 3 = \pm\sqrt{18}$$

$$a = 3 \pm \sqrt{18}$$

$$\text{Solve: } (b + 2)^2 = 40 \quad -2 \pm 2\sqrt{10}$$

$$b + 2 = \pm\sqrt{40}$$

$$b = -2 \pm \sqrt{40}$$

$$\text{Solve: } \sqrt{\left(x - \frac{1}{2}\right)^2} = \sqrt{\frac{5}{4}}$$

$$x - \frac{1}{2} = \pm \frac{\sqrt{5}}{2}$$

$$x = \frac{1}{2} \pm \frac{\sqrt{5}}{2} \rightarrow \frac{1 \pm \sqrt{5}}{2}$$

$$\text{Solve: } \left(x - \frac{1}{3}\right)^2 = \frac{5}{9}$$

$$x - \frac{1}{3} = \pm \frac{\sqrt{5}}{3}$$

$$x = \frac{1}{3} \pm \frac{\sqrt{5}}{3}$$

$$\text{Solve: } \left(y - \frac{3}{4}\right)^2 = \frac{7}{16}$$

$$y - \frac{3}{4} = \pm \frac{\sqrt{7}}{4}$$

$$y = \frac{3}{4} \pm \frac{\sqrt{7}}{4}$$

Solve: $(x-2)^2 + 3 = 30$

$$(x-2)^2 = 27$$

$$x-2 = \pm\sqrt{27}$$

$$x = 2 \pm 3\sqrt{3}$$

Solve: $(a-5)^2 + 4 = 24$

$$(a-5)^2 = 20$$

$$a-5 = \pm\sqrt{20}$$

$$a = 5 \pm 2\sqrt{5}$$

Solve: $(b-3)^2 - 8 = 24$

$$(b-3)^2 = 32$$

$$b-3 = \pm\sqrt{32}$$

$$b = 3 \pm 4\sqrt{2}$$

Solve: $(3r+4)^2 = -8$

$$3r+4 = \pm\sqrt{-8}$$

No Real Solution

$$p^2 - 10p + 25 = 18$$

Solve: $p^2 - 10p + 25 = 18$

$$(p-5)^2 = 18$$

$$p-5 = \pm\sqrt{18}$$

$$p = 5 \pm 3\sqrt{2}$$

Solve: $x^2 - 6x + 9 = 12$

$$(x-3)^2 = 12$$

$$x-3 = \pm\sqrt{12}$$

$$x = 3 \pm 2\sqrt{3}$$

Solve: $y^2 + 12y + 36 = 32$

$$(y+6)^2 = 32$$

$$y+6 = \pm\sqrt{32}$$

$$y = -6 \pm 4\sqrt{2}$$

Solve: $y^2 + 12y + 36 = 32$

What you will learn about:
Solving Quadratics by Completing the Square

$$ax^2 + bx + c$$

Complete the square

1) $a = 1$

2) b -value and divide by 2

3) Square answer in step # 2

$$\frac{9}{2}$$

Complete the square to make it a perfect square trinomial. Write as a binomial squared.

$$x^2 + 14x + 49$$

$$\downarrow$$

$$(x + 7)^2$$

$$y^2 + 12y + 36$$

$$(y + 6)^2$$

$$a^2 - 20a + 100$$

$$\downarrow$$

$$(a - 10)^2$$

$$b^2 - 4b + 4$$

$$(b - 2)^2$$

$$u^2 - 9u + \frac{81}{4}$$

$$\left(u - \frac{9}{2}\right)^2$$

$$m^2 - 5m + \frac{25}{4}$$

$$\left(m - \frac{5}{2}\right)^2$$

$$p^2 + \frac{1}{2}p + \frac{1}{16}$$

$$\left(p + \frac{1}{4}\right)^2$$

$$q^2 - \frac{2}{3}q + \frac{1}{9}$$

$$\left(q - \frac{1}{3}\right)^2$$

a = 1

Solve by Completing the Square

Solve $x^2 + 8x = 48$ by completing the square.

$$x^2 + 8x + 16 = 48 + 16$$

$$\sqrt{(x+4)^2} = \sqrt{64} \quad \begin{array}{l} -4+8 \\ 4 \end{array} \quad \begin{array}{l} -4-8 \\ -12 \end{array}$$

$$x+4 = \pm 8$$

$$x = -4 \pm 8$$

Solve $d^2 + 10d = -9$ by completing the square.

$$d^2 + 10d + 25 = -9 + 25 \quad \begin{array}{l} -5+4 \\ -1 \end{array} \quad \begin{array}{l} -5-4 \\ -9 \end{array}$$

$$(d+5)^2 = 16$$

$$d+5 = \pm 4$$

$$d = -5 \pm 4$$

Solve $y^2 - 6y = 16$ by completing the square.

$$y^2 - 6y + 9 = 16 + 9$$

$$(y-3)^2 = 25 \quad \begin{array}{l} 3+5=8 \\ 3-5=-2 \end{array}$$

$$y-3 = \pm 5$$

$$y = 3 \pm 5$$

Solve $r^2 - 4r = 12$ by completing the square.

$$r^2 - 4r + 4 = 12 + 4$$

$$(r - 2)^2 = 16$$

$$r - 2 = \pm 4 \quad r = 6, -2$$

$$r = 2 \pm 4$$

Solve $x^2 + 4x = -21$ by completing the square.

$$x^2 + 4x + 4 = -21 + 4$$

$$(x + 2)^2 = -17$$

No Real Solution

Solve $x^2 + 10x + 4 = 15$ by completing the square.

$$x^2 + 10x + 25 = 11 + 25 \quad x = -5 \pm 6$$

$$(x + 5)^2 = 36$$

$$x = 1, -11$$

$$x + 5 = \pm 6$$

$$11 + \frac{9}{4}$$

$$\frac{44}{4} + \frac{9}{4} = \frac{53}{4}$$

Solve $n^2 = 3n + 11$ by completing the square.

$$n^2 - 3n + \frac{9}{4} = 11 + \frac{9}{4}$$

$$n = \frac{3}{2} \pm \frac{\sqrt{53}}{2}$$

$$\left(n - \frac{3}{2}\right)^2 = \frac{53}{4}$$

$$n - \frac{3}{2} = \pm \frac{\sqrt{53}}{2}$$