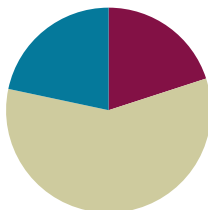


## Lesson 12

**Objective:** Solve two-step word problems, including multiplicative comparison.

### Suggested Lesson Structure

■ Fluency Practice	(12 minutes)
■ Concept Development	(35 minutes)
■ Student Debrief	(13 minutes)
<b>Total Time</b>	<b>(60 minutes)</b>



### Fluency Practice (12 minutes)

- Multiply Mentally 4.NBT.5 (4 minutes)
- Multiply in Three Different Ways 4.NBT.5 (8 minutes)

### Multiply Mentally (4 minutes)

Note: Reviewing these mental multiplication strategies provides a foundation for students to succeed during the Concept Development.

Repeat the process from Lesson 7 with the following possible sequence:  $3,421 \times 2$ ,  $2,302 \times 3$ ,  $2,112 \times 4$ , and  $2,023 \times 4$ .

### Multiply in Three Different Ways (8 minutes)

Materials: (S) Place value disks

Note: This fluency activity reviews the concepts learned in Topic C.

Repeat the fluency activity from Lesson 11, expanding to three- and four-digit numbers for the following possible sequence:  $245 \times 2$ ,  $301 \times 5$ , and  $5,241 \times 2$ .

**Concept Development (35 minutes)**

Materials: (S) Problem Set

Note: For this lesson, the Problem Set comprises word problems from the Concept Development and is therefore to be used during the lesson itself.

Students may work in pairs to solve Problems 1–4 below using the RDW approach to problem solving.

**1. Model the problem.**

Have two pairs of students who can be successful with modeling the problem work at the board while the others work independently or in pairs at their seats. Review the following questions before beginning the first problem.

- Can you draw something?
- What can you draw?
- What conclusions can you make from your drawing?

As students work, circulate. Reiterate the questions above.

After two minutes, have the two pairs of students share *only* their labeled diagrams.

For about one minute, have the demonstrating students receive and respond to feedback and questions from their peers.

**2. Calculate to solve and write a statement.**

Give everyone two minutes to finish work on that question, sharing the work and thinking with a peer. All should then write their equations and statements of the answer.

**3. Assess the solution.**

Give students one to two minutes to assess the solutions presented by their peers on the board, comparing the solutions to their own work. Highlight alternative methods to reach the correct solution.

**NOTES ON  
MULTIPLE MEANS  
OF ENGAGEMENT:**

Give everyone a fair chance to be successful by providing appropriate scaffolds. Demonstrating students may use translators, interpreters, or sentence frames to present and respond to feedback. Models shared may include concrete manipulatives. If the pace of the lesson is a consideration, prepare presenters beforehand. The first problem may be most approachable for students working below grade level.

**Problem 1**

The table shows the cost of party favors. Each party guest receives a bag with 1 balloon, 1 lollipop, and 1 bracelet. What is the total cost for 9 guests?

Item	Cost
1 balloon	26¢
1 lollipop	14¢
1 bracelet	33¢

Handwritten student work for Problem 1:

73¢

26	14	33
----	----	----

26 + 14 + 33  
40 + 33 = 73

73  
x 9  
—  
657

P = 657¢

The total cost for 9 party bags is 657¢.

This two-step problem requires students to determine the cost of party favors for one guest and then use that information to determine the total cost of party favors for 9 guests. Although RDW is reviewed prior to beginning work on this problem, because of its simplicity, many students might elect to begin solving immediately. Some students may choose to multiply each item by 9 before adding those amounts. Based on their prior experience with money, some students may represent the total amount of 657 cents as \$6.57, but they are not required to do so.

**Problem 2**

The Turner family uses 548 liters of water per day. The Hill family uses 3 times as much water per day. How much water does the Hill family use per week?

Handwritten student work for Problem 2:

548 L

548 L
-------

548  
x 3  
—  
1644

1644  
x 7  
—  
11,508

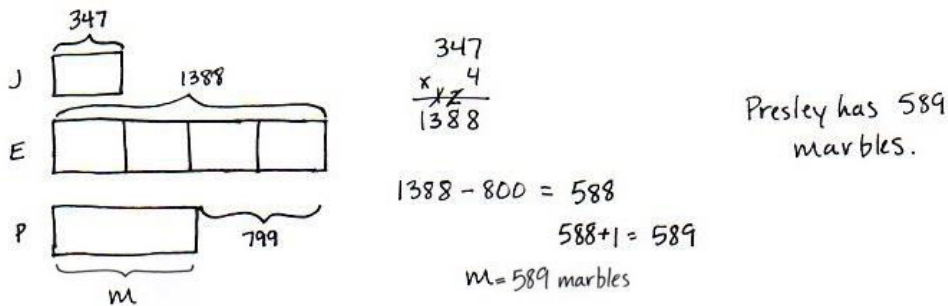
H = 11,508 L

The Hill family uses 11,508 liters of water per week.

In solving this problem, students use information from the problem and their knowledge of language denoting multiplicative comparison to determine their answer. They must also remember that there are 7 days in a week in order to complete the computation necessary to finish the problem. Models chosen for this problem may include tape diagrams as shown.

**Problem 3**

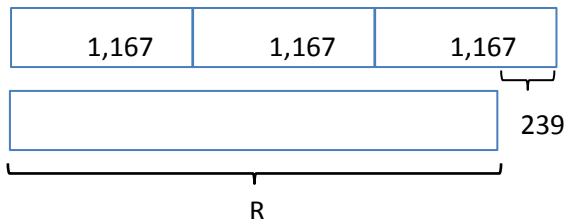
Jayden has 347 marbles. Elvis has 4 times as many as Jayden. Presley has 799 fewer than Elvis. How many marbles does Presley have?



This two-step problem affords students another opportunity to model with tape diagrams. They are required to apply what they have learned about multiplying multi-digit numbers by single digits, as well as practice their subtraction with multiple regrouping skills from Module 1. Encourage students to also practice mental math, such as when subtracting 799 from 1,388. As illustrated above, note that the diagram may or may not accurately show the relationship between 799 and the unit size, 347. Nevertheless, discuss how one might use mental math to estimate how long Presley’s bar should be.

**Problem 4**

- a. Write an equation that would allow someone to find the value of R.



$$R + 239 = 1167 \times 3$$

$$R = 3 \times 1167 - 239$$

Student equations may include one or both of the equations above. They must include the use of the R for the unknown quantity and show that R is equal to 239 less than three times 1,167.



**NOTES ON MULTIPLE MEANS OF ACTION AND EXPRESSION:**

Support English language learners as they write their own word problems. Provide sentence starters and a word bank.

Sentence starters may include:

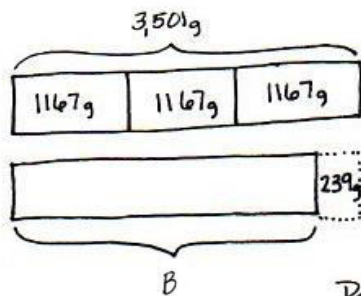
- “I had \_\_\_ (units).”
- “How many \_\_\_ in all?”

Possible words for the word bank may include:

- times as many
- fewer than
- more than
- total
- difference

b. Write your own word problem to correspond to the tape diagram, and then solve.

Patti's sandals weigh 1,167 grams. She bought 3 pairs, all different colors! All 3 pairs of sandals together weigh 239 grams more than her winter boots. What is the weight of Patti's winter boots?



**Solution A**

$$\begin{array}{r} 1167g \\ \times 3 \\ \hline 3501g \end{array}$$

$$\begin{array}{r} 4911 \\ 3501g \\ - 239g \\ \hline 3262g \end{array}$$

$B = 3,262g$

Patti's winter boots weigh 3,262 grams.

**Solution B**

$$\begin{array}{r} 1,167g \\ \times 3 \\ \hline 3,501g \end{array}$$

$$239 \xrightarrow{+61} 300 \xrightarrow{+200} 500 \xrightarrow{+3000} 3500 \xrightarrow{+1} 3501$$

$$3000 + 200 + 62 = 3,262$$

Responses will vary. Guide students with a context for creating a problem, such as the number of students who attend two schools or the weights of objects.

### Problem Set

Please note that the Problem Set for Lesson 12 comprises the problems from the Concept Development, as stated in the introduction of the lesson.

### Student Debrief (13 minutes)

**Lesson Objective:** Solve two-step word problems, including multiplicative comparison.

The Student Debrief is intended to invite reflection and active processing of the total lesson experience.

Invite students to review their solutions for the Problem Set. They should check work by comparing answers with a partner before going over answers as a class. Look for misconceptions or misunderstandings that can be addressed in the Debrief. Guide students in a conversation to debrief the problems and process the lesson.

**Problem 1:** The table shows the cost of party favors. Each party guest receives a bag with 1 balloon, 1 lollipop, and 1 bracelet. What is the total cost for 9 guests?

Item	Cost
1 balloon	26¢
1 lollipop	14¢
1 bracelet	33¢

**Student Solution:** 
$$\begin{array}{r} 264 \\ 144 \\ + 334 \\ \hline 734 \end{array}$$
 
$$\begin{array}{r} 734 \\ \times 9 \\ \hline 6606 \end{array}$$
 The total cost for 9 guests is 667¢.

**Problem 2:** The Turner family uses 548 liters of water per day. The Hill family uses 3 times as much water per day. How much water does the Hill family use per week?

**Student Solution:** 
$$\begin{array}{r} 548 \\ \times 3 \\ \hline 1644 \end{array}$$
 1,644 liters per day. 
$$\begin{array}{r} 1644 \\ \times 7 \\ \hline 11508 \end{array}$$
 The Hill family uses 11,508 liters of water per week.

**Problem 3:** Jayden has 347 marbles. Elvis has 4 times as many as Jayden. Presley has 799 fewer than Elvis. How many marbles does Presley have?

**Student Solution:** 
$$\begin{array}{r} 347 \\ \times 4 \\ \hline 1388 \end{array}$$
 
$$\begin{array}{r} 1388 \\ - 799 \\ \hline 589 \end{array}$$
 Presley has 589 marbles.

Any combination of the questions below may be used to lead the discussion.

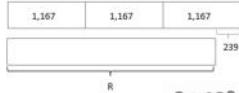
- How was Problem 1 similar to the other problems we did today? How was it different?
- How was setting up Problem 2 similar to setting up Problem 3? At what point did the two problems become quite different?
- What piece of information did you need to know to solve Problem 2 that was not given to you in the problem?
- Share the word problem you created for Problem 4(b) with your partner. Solve your partner’s problem. Explain the strategy you used to solve it.

**Exit Ticket (3 minutes)**

After the Student Debrief, instruct students to complete the Exit Ticket. A review of their work will help with assessing students’ understanding of the concepts that were presented in today’s lesson and planning more effectively for future lessons. The questions may be read aloud to the students.

NYS COMMON CORE MATHEMATICS CURRICULUM Lesson 12 Problem Set 4•3

4. Write an equation that would allow someone to find the value of R.

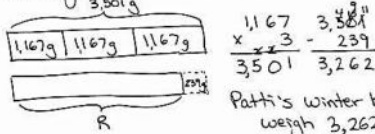


$$R + 239 = 3 \times 1,167$$

$$R = 3 \times 1,167 - 239$$

b. Write your own word problem to correspond to the tape diagram, and then solve.

Patti's sandals weigh 1,167 grams. She bought 3 pairs, all different colors. All 3 pairs of sandals weigh 239 grams more than her winter boots. What is the weight of Patti's winter boots?



Patti's winter boots weigh 3,262 grams.

COMMON CORE Lesson 12: Solve two-step word problems, including multiplicative comparison. engage<sup>ny</sup> 3.D.10

Name \_\_\_\_\_

Date \_\_\_\_\_

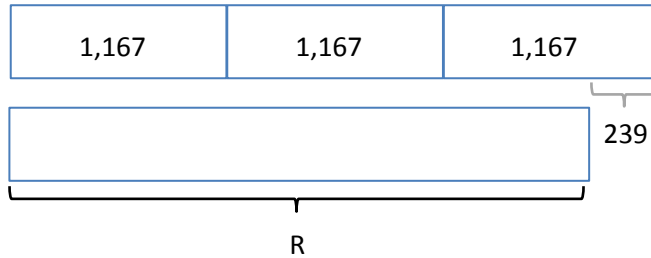
Use the RDW process to solve the following problems.

1. The table shows the cost of party favors. Each party guest receives a bag with 1 balloon, 1 lollipop, and 1 bracelet. What is the total cost for 9 guests?

Item	Cost
1 balloon	26¢
1 lollipop	14¢
1 bracelet	33¢

2. The Turner family uses 548 liters of water per day. The Hill family uses 3 times as much water per day. How much water does the Hill family use per week?
3. Jayden has 347 marbles. Elvis has 4 times as many as Jayden. Presley has 799 fewer than Elvis. How many marbles does Presley have?

4. a. Write an equation that would allow someone to find the value of R.



- b. Write your own word problem to correspond to the tape diagram, and then solve.



Name \_\_\_\_\_

Date \_\_\_\_\_

Use the RDW process to solve the following problem.

Jennifer has 256 beads. Stella has 3 times as many beads as Jennifer. Tiah has 104 more beads than Stella. How many beads does Tiah have?

Name \_\_\_\_\_

Date \_\_\_\_\_

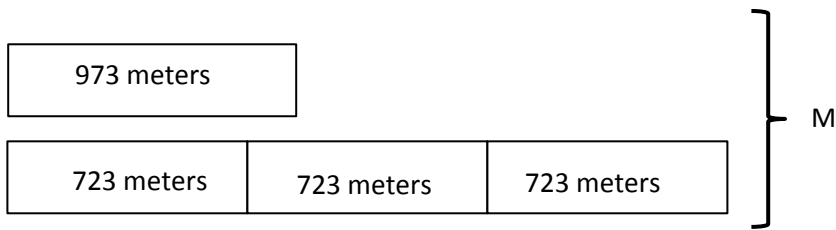
Use the RDW process to solve the following problems.

1. The table shows the number of stickers of various types in Chrissy's new sticker book. Chrissy's six friends each own the same sticker book. How many stickers do Chrissy and her six friends have altogether?

Type of Sticker	Number of Stickers
flowers	32
smiley faces	21
hearts	39

2. The small copier makes 437 copies each day. The large copier makes 4 times as many copies each day. How many copies does the large copier make each week?
3. Jared sold 194 Boy Scout chocolate bars. Matthew sold three times as many as Jared. Gary sold 297 fewer than Matthew. How many bars did Gary sell?

4. a. Write an equation that would allow someone to find the value of  $M$ .



- b. Write your own word problem to correspond to the tape diagram, and then solve.