

Semester 2 Notes: Week 10 - Week 17 (03/15/21 - 05/07/21)

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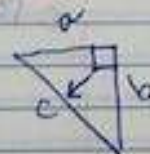
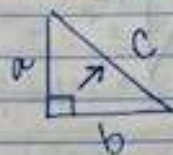
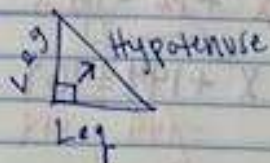
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The Pythagorean Theorem

- I can use the pythagorean theorem to find the missing length of a \triangle .



* The hypotenuse is always side c *

The pythagorean theorem : $a^2 + b^2 = c^2$

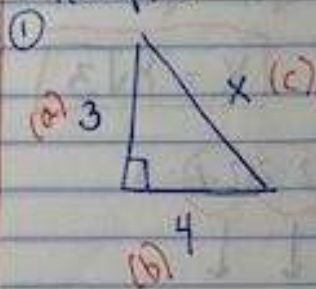
Exponent Review

$$X^2 = X \cdot X$$

$$4^2 = 4 \cdot 4 = 16$$

$$-6^2 = -6 \cdot -6 = 36$$

Examples



Find x

$2\sqrt{x}$

$$a^2 + b^2 = c^2$$

$$3^2 + 4^2 = x^2$$

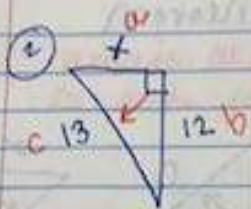
$$9 + 16 = x^2$$

$$\sqrt{25} = \sqrt{x^2}$$

$$\boxed{5 = x}$$

* opposite of x^2
is \sqrt{x} *

$$a^2 + b^2 = c^2$$



Find x

$$a^2 + b^2 = c^2$$

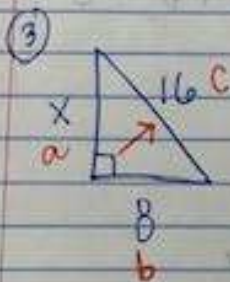
$$x^2 + 12^2 = 13^2$$

$$x^2 + 144 = 169$$

$$-144 \quad -144$$

$$\sqrt{x^2} = \sqrt{25}$$

$$x = 5$$



Find x

$$a^2 + b^2 = c^2$$

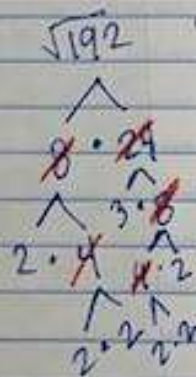
$$x^2 + 8^2 = 16^2$$

$$x^2 + 64 = 256$$

$$-64 \quad -64$$

$$\sqrt{x^2} = \sqrt{192}$$

$$x = 8\sqrt{3}$$



$$13 \cdot 546$$

$$(2 \cdot 2)(2 \cdot 2)(2 \cdot 2) \cdot 3$$

$$\downarrow \quad \downarrow \quad \downarrow$$

$$2 \cdot 2 \cdot 2 \sqrt{3}$$

$$8\sqrt{3}$$

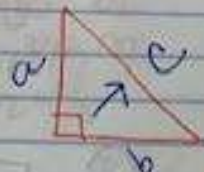
Lesson Two

04/27/2021 Pythagorean Theorem w/ Radicals
• I can use the Pythagorean theorem to solve for missing lengths.

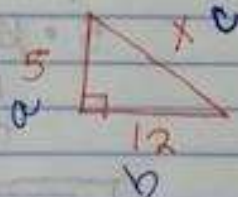
Warm-up

① What is the Pythagorean theorem?
 $a^2 + b^2 = c^2$

② Label this right triangle with sides a, b, and c.



③ Find X



$$a^2 + b^2 = c^2$$

$$5^2 + 12^2 = X^2$$

$$25 + 144 = X^2$$

$$\sqrt{169} = \sqrt{X^2}$$

$$13 = X$$

Radical Review

$$\begin{array}{c} \sqrt{45} \\ \wedge \\ 5 \cdot 9 \\ \wedge \\ 3 \cdot 3 \\ \downarrow \\ \boxed{3\sqrt{5}} \end{array}$$

- ① Find multiples
- ② Cross out the numbers you simplify.
- ③ circle any pairs.
- ④ write your pair as one number on the outside

Examples

①

$$\begin{array}{c} \sqrt{32} \\ \wedge \\ 4 \cdot 8 \\ \wedge \\ 2 \cdot 2 \quad \times \cdot 2 \\ \wedge \\ 2 \cdot 2 \\ \downarrow \quad \downarrow \\ 2 \cdot 2 \sqrt{2} \\ \boxed{4\sqrt{2}} \end{array}$$

②

$$\begin{array}{c} \sqrt{30} \\ \wedge \\ 5 \cdot 6 \\ \wedge \\ 2 \cdot 3 \\ \downarrow \\ \boxed{\sqrt{30}} \end{array}$$

4/28/21 Types of Triangles

• I can determine if a triangle is acute, right, or obtuse.

*Formulas:

$$a^2 + b^2 > c^2 \rightarrow \text{Acute } \Delta$$

$$a^2 + b^2 = c^2 \rightarrow \text{Right } \Delta$$

$$a^2 + b^2 < c^2 \rightarrow \text{Obtuse } \Delta$$

* c is always your longest side *

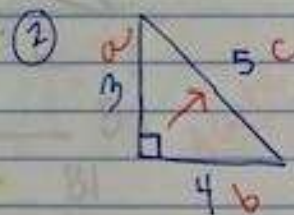
①

7	8	9
a	b	c

$$\begin{array}{r} a^2 + b^2 \\ 7^2 + 8^2 \end{array} \quad \begin{array}{r} c^2 \\ 9^2 \end{array}$$

$$49 + 64 \quad 81$$

△ $113 > 81$ Acute



$$\begin{array}{r} a^2 + b^2 \\ 3^2 + 4^2 \end{array} \quad \begin{array}{r} c^2 \\ 5^2 \end{array}$$

$$9 + 16 \quad 25$$

$$25 = 25$$

Right

#5 (3) Example



$$a^2 + b^2 = c^2$$

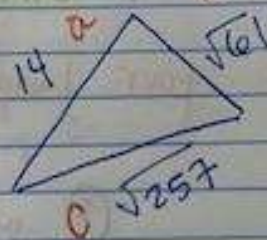
$$(2\sqrt{14})^2 + 12^2 = 15^2$$

$$(2 \times 14) + 144 = 225$$

$$28 + 144 = 225$$

Δ triangle Obtuse $172 < 225$

#6 (4)



$$a^2 + b^2 = c^2$$

$$14^2 + \sqrt{61}^2 = \sqrt{257}^2$$

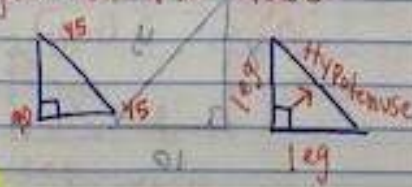
$$196 + 61 = 257$$

Right $257 = 257$

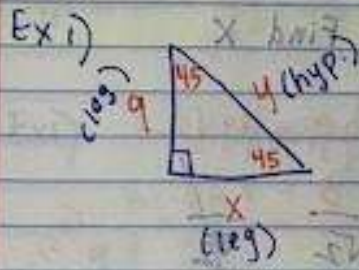
5/3/21 Special Right Triangles

- I can use special right triangle rules to find lengths of the sides.

$45^\circ - 45^\circ - 90^\circ$

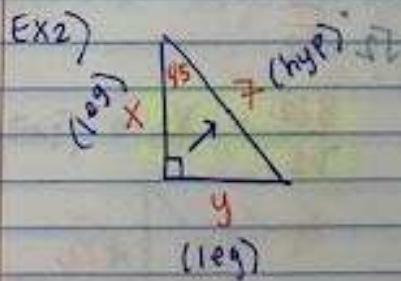


leg = leg
 Hypotenuse = leg $\cdot \sqrt{2}$



leg = leg
 $X = 9$

hyp = leg $\cdot \sqrt{2}$
 $Y = 9 \cdot \sqrt{2}$
 $Y = 9\sqrt{2}$



hyp = leg $\cdot \sqrt{2}$
 $7 = X \cdot \sqrt{2}$

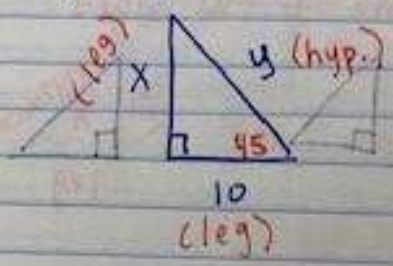
$\sqrt{2} \cdot \frac{7}{\sqrt{2}} = X$
 $\sqrt{2} \cdot \sqrt{2}$

leg = leg
 $Y = \frac{7\sqrt{2}}{2}$

$\frac{7\sqrt{2}}{2} = X$

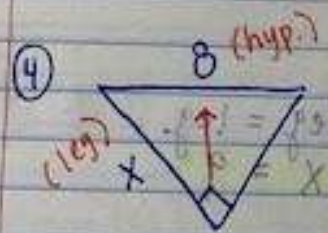
Special Right Triangles

③ leg = leg hyp = leg · √2



leg = leg
 $x = 10$

hyp = leg · √2
 $y = 10\sqrt{2}$



Find x

hyp = leg · √2
 $8 = x\sqrt{2}$
 $\frac{8}{\sqrt{2}} = \frac{x\sqrt{2}}{\sqrt{2}}$

$\sqrt{2} \cdot \frac{8}{\sqrt{2}} = x$

$\frac{8\sqrt{2}}{2} = x$

$\sqrt{2} \cdot \frac{8}{\sqrt{2}} = 8$
 $\sqrt{2} \cdot x = 8$

$x = \frac{8}{\sqrt{2}}$

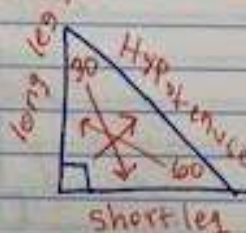
$x = \frac{8\sqrt{2}}{2}$

leg = leg
 $x = 8$

05/04/21 Special Right Triangles Continued

I can use special right Δ rules to find missing lengths.

$30^\circ - 60^\circ - 90^\circ$



* Short leg: across from 30°

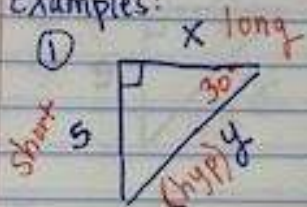
* Long leg: across from 60°

Formulas:

$hyp = short\ leg \cdot 2$

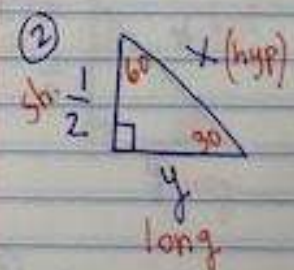
$Long\ leg = short\ leg \cdot \sqrt{3}$

Examples:



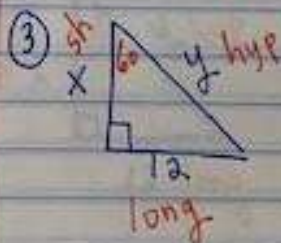
$hyp = sh \cdot 2$
 $y = 5 \cdot 2$
 $y = 10$

$long = sh \cdot \sqrt{3}$
 $x = 5 \cdot \sqrt{3}$
 $x = 5\sqrt{3}$



$hyp = sh \cdot 2$
 $x = \frac{1}{2} \cdot 2$
 $x = 1$

$long = sh \cdot \sqrt{3}$
 $y = \frac{1}{2} \cdot \sqrt{3}$
 $y = \frac{\sqrt{3}}{2}$



$hyp = sh \cdot 2$
 $y = 2x$
 $y = \frac{12\sqrt{3}}{3} \cdot \frac{2}{1}$
 $y = \frac{24\sqrt{3}}{3}$

$long = sh \cdot \sqrt{3}$
 $\sqrt{3} \cdot \frac{12}{\sqrt{3}} = \frac{x \cdot \sqrt{3}}{\sqrt{3}}$
 $12\sqrt{3} = x$