

So far, we have added, subtracted, and multiplied complex numbers. Can we divide them? A division problem between two complex numbers would look like this:

$$\frac{4 + 6i}{3 - 2i}$$

We want the answer to be in the form $a + bi$. Right now, the problem doesn't look like that because of the i in the denominator. Hopefully we can get rid of that problem by multiplying the whole fraction by a clever form of 1. (So that would be a fraction with the same thing on top as on the bottom.) What clever form of 1 could we multiply the fraction by to get a real number in the denominator?

1. Divide $(4 + 6i) \div (3 - 2i)$.
2. Divide $(a + bi) \div (c + di)$.

Will the answers to these division problems also be complex numbers?

$$1) \frac{4+6i}{3-2i} \cdot \frac{3+2i}{3+2i} = \frac{12+8i+18i+12i^2}{3^2-(2i)^2} = \frac{26i}{13} = 2i$$

$$2) \frac{a+bi}{c+di} \cdot \frac{c-di}{c-di} = \frac{ac + -adi + bci - bdi^2}{c^2 - (di)^2} = \frac{(ac+bd)}{c^2+d^2} + \frac{(-ad+bc)}{c^2+d^2} i$$