### LESSON 4.1 Assignment

Name \_

Date \_\_\_

#### Shape and Structure Forms of Quadratic Functions

- **1.** Analyze the graph of the quadratic function.
  - **a.** The standard form of a quadratic function is  $f(x) = ax^2 + bx + c$ . What possible values can *a* and *c* have for the given quadratic function? Explain your reasoning.
- **b.** The vertex form of a quadratic function is  $f(x) = a(x h)^2 + k$ . What possible values can *a*, *h*, and *k* have for the given quadratic function? Explain your reasoning.

**c.** The factored form of a quadratic function is  $f(x) = a(x - r_1)(x - r_2)$ . What possible values can a,  $r_1$ , and  $r_2$  have? Explain your reasoning.

**2.** Write a quadratic function for the parabola that passes through the point (2, -3) with roots (-6, 0) and (4, 0).

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- **3.** Mitzu shoots an arrow from an initial height of 2 meters. The arrow reaches its maximum height of 20 meters after it has flown a distance of 60 meters.
  - **a.** Write a quadratic function to represent the height of the arrow as a function of its distance.

b. Determine the height of the arrow after it has flown a distance of 100 meters.

- **4.** Charlie kicks a soccer ball from the ground through a hoop that is 80 feet away at a height of 20 feet. The ball hits the ground 100 feet from where Charlie kicked it.
  - a. Write a quadratic function to represent the height of the ball as a function of its distance.

b. Determine the maximum height of the ball during its flight.

# LESSON 4.2 Assignment

Name \_\_\_\_

\_ Date \_\_\_\_\_

### Function Sense Translating Functions

**1.** Graph  $d(x) = (x + 3)^2 - 1$  without a calculator. Explain each of your steps.



**2.** Graph  $g(x) = (x - 5)^2 - 4$  without a calculator. Explain each of your steps.



**3.** The function h(x) is shown. If  $f(x) = x^2$ , write h(x) in terms of f(x).



**4.** The function p(x) is shown. If  $f(x) = x^2$ , write p(x) in terms of f(x).



**5.** The function t(x) is a translation of  $f(x) = x^2$ , and t(x) has a vertex at (25, -9). Write the function t(x). Explain your reasoning.

## LESSON 4.3 Assignment

Name \_\_\_

Date \_\_\_\_\_

### Up and Down Vertical Dilations of Quadratic Functions

**1.** Graph  $d(x) = -\frac{1}{2}(x + 5)^2 - 3$  without a calculator. Explain each of your steps.



**2.** Graph  $g(x) = 3(x - 2)^2 - 6$  without a calculator. Explain each of your steps.



**3.** Write the function h(x) that represents the given graph. Explain your reasoning.



**4.** Write the function p(x) that represents the given graph. Explain your reasoning.



**5.** The function t(x) is a transformation of  $f(x) = x^2$ . The function t(x) has a vertex at (-12, 15) and has been vertically compressed by a factor of  $\frac{1}{4}$ . Write the function t(x). Explain your reasoning.

### **LESSON** 4.4 Assignment

Name \_\_\_

Date \_\_\_\_\_

#### Side to Side Horizontal Dilations of Quadratic Functions

**1.** Graph  $m(x) = \left(\frac{1}{2}x + 3\right)^2 + 2$  without a calculator. Explain each of your steps.



**2.** Write the function p(x) that represents the given graph. Explain your reasoning.



**3.** Graph  $g(x) = (2x - 8)^2 - 4$  without a calculator. Explain each of your steps.



**4.** The graph of the quadratic function t(x) is shown. If  $f(x) = x^2$ , write t(x) in terms of f(x). Explain your reasoning.



### LESSON 4.5 Assignment

Name \_\_\_\_

\_ Date \_\_\_

### What's the Point? Deriving Quadratic Functions

**1.** Use your knowledge of reference points to write an equation for the quadratic function that has *x*-intercepts at (-1, 0) and (1, 0) and a *y*-intercept at (0, -3).

**2.** Use your knowledge of reference points to write an equation for the quadratic function that has a vertex at (4, -3) and passes through (6, -1).

**3.** Use your knowledge of reference points to write an equation for the quadratic function that has one *x*-intercept at (-7, 0) and passes through (-4, -18).

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**4.** Create a system of equations and use algebra to write a quadratic function that passes through the points (-2, 8), (1, 14), and (0, 10).

- **5.** Victoria competes in a discus throwing competition. She needs to throw her discus at least 200 feet to win the event. The discus has an initial height of 5 feet when she releases it. The discus reaches a height of 25 feet after traveling 75 feet and a height of 20 feet after traveling 150 feet.
  - **a.** Write a quadratic function to model the height of the discus as a function of the distance traveled.
  - b. Does Victoria win the competition? Explain your reasoning.
  - c. What was the maximum height of the discus?

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Name \_\_\_\_

\_ Date \_\_\_\_

### Now It's Getting Complex . . . But It's Really Not Difficult! Complex Number Operations

**1.** Calculate each power of *i*.

**a.** *i*<sup>44</sup>

**b.** *i*<sup>4003</sup>

**c.** *i*<sup>730</sup>

**d.** *i*<sup>-20</sup>

- 2. Simplify each expression. Identify the real and imaginary parts of your answer.
  - **a.** √−18

**b.** 
$$\frac{\sqrt{-72}-2}{6}$$

**a.** -7 + 3i + x = 10 - 2i

**b.** 
$$\frac{x}{5+4i} = -2 - i$$

**4.** Multiply each number by its complex conjugate. Identify the real and imaginary parts of your answer. **a.** 4 - 6i

**5.** Simplify the expression (3 + i)(2 + 4i)(3 - i)(2 - 4i). Identify the real and imaginary parts of your answer.

### **LESSON** 4.7 Assignment

Name \_\_\_\_

Date \_

#### You Can't Spell "Fundamental Theorem of Algebra" without F-U-N! Quadratics and Complex Numbers

- **1.** The Internet Bargains Company models their profit during different 20-day periods throughout the year. The function p(x) represents the daily profit (in thousands of dollars) on the *x*th day of each period. When p(x) > 0, the company has a daily profit. When p(x) < 0, the company has a daily loss.
  - **a.** The model for one 20-day period is  $p(x) = 0.04(x 10)^2 + 2$ . Determine which of the days in the 20-day period the company made a profit without using a calculator. Explain your reasoning.

**b.** The model for one 20-day period is p(x) = -0.1(x - 3)(x - 15). Determine which of the days in the 20-day period the company made a profit without using a calculator. Explain your reasoning.

**c.** The model for one 20-day period is  $p(x) = -0.06(x - 9)^2$ . Determine which of the days in the 20-day period the company made a profit without using a calculator. Explain your reasoning.

2. Determine the number of roots for each given equation and whether the roots are real or imaginary. a.  $0 = 9x^2 - 6x + 1$  **b.**  $0 = 2x^2 + 9x + 10$ 

**c.**  $0 = x^2 - 3x + 5$ 

- $\ensuremath{\textbf{3.}}$  Write a quadratic equation in standard form with the given roots.
  - **a.** Write a quadratic equation with a double root of -5.

**b.** Write a quadratic equation with a root of -3 + 2i.