PERFORMANCE STANDARDS FOR MATH: GRADE 7

A. Mathematical Processes

Content Standard: Students in Wisconsin will draw on a broad body of mathematical knowledge and apply a variety of mathematical skills and strategies, including reasoning, oral and written communication and the use of appropriate technology, when solving mathematical, real-world* and non-routine* problems.

Rationale: In order to participate fully as a citizen and a worker in our contemporary world, a person should be mathematically powerful. Mathematical power is the ability to explore, to conjecture, to reason logically and to apply a wide repertoire of methods to solve problems. Because no one lives and works in isolation, it is also important to have the ability to communicate mathematical ideas clearly and effectively.

Performance Standard

- A.8.1 Use reasoning abilities to:
 - evaluate information
 - perceive patterns
 - identify relationships
 - formulate questions for further exploration
 - evaluate strategies
 - justify statements
 - test reasonableness of results
 - defend work

1.	Use reasoning abilities to:
	• perceive patterns (congruent, similar, divisibility, L.C.M., G.C.F., prime
	factorization, comparing and ordering, sequence, Pascal's Triangle, Fibonacci
	Sequence, probability)
	• identify relationships (ratio, proportion, congruent, arithmetic, geometric)
	• evaluate information (too much, not enough, what do you need to use)
2.	Use reasoning abilities to:
	 design questions that will help with further research
	• justify a statement using logical reasoning by explaining processes used to
	arrive at the answer
	• test reasonableness of results through estimation, sampling and substitution
	• to defend work by using the four-step process (explore, plan, solve, examine)
3.	Apply the following problem-solving strategies:
	choose an operation draw a diagram
	use manipulatives guess and check
	make a chart/table/list use estimation
	work backwards note important information
	use a calculator identify needed/extra information
	find a pattern use a graph

	A. Mathematical Processes		
	use an equation use a formula solve a simpler problem make a model classify eliminate possibilities Venn diagrams		
4.	Justify strategies and solutions through oral and written explanations		
Perfor	mance Standard		
A.8.2	Communicate logical arguments clearly to show why a result makes sense.		
7 th Grade			
	Communicate logical arguments clearly to show why a result makes sense using words, numbers, pictures, symbols, charts, graphs, tables, diagrams, models Know when to use the appropriate resource/strategy Justify logical arguments through oral and written explanation		
Perfor	mance Standard		
A.8.3	Analyze non-routine* problems by modeling*, illustrating, guessing, simplifying, generalizing, shifting to another point of view, etc.		
7 th Gra	nde		
	Analyze non-routine problems by illustrating, guessing, simplifying, relating to everyday life, modeling, acting it out, generalizing, shifting to another point of view Use mathematics as a way to understand other areas of the curriculum (e.g. measurement in science, geography skills in social studies, and Venn diagrams in language arts) See relationships between various kinds of problems and actual events		
Perfor	mance Standard		
A.8.4	 Develop effective oral and written presentations that include: appropriate use of technology the conventions of mathematical discourse (e.g., symbols, definitions, labeled drawings) mathematical language clear organization of ideas and procedures understanding of purpose and audience 		

7th Grade

1. Calculators – a learner will apply the following: scientific calculators. _____

A. Mathematical Processes

2.	Computers – a learner will apply the following: spreadsheet tool; graphing tool; geometry tool; internet access		
3.	<u> </u>		
4.	Present results of a project, written and oral, to an audience.		
Perfor	mance Standard		
A.8.5	Explain mathematical concepts, procedures, and ideas to others who may not be familiar with them.		
7 th Gra	ade		
1.	Communications – The learner will explain and demonstrate mathematical concepts, procedures and ideas to others by reading, talking about it, sharing and assisting others.		
	* think/pair/share * peer tutoring		
	* study buddies * cooperative groups		
Perfor	mance Standard		
A.8.6	A.8.6 Read and understand mathematical texts and other instructional materials and recognize mathematical ideas as they appear in other contexts.		
7 th Gra	ade		
1.	J. 6. 18 J.		
2	science; music; language arts; art; and electives Real-world connections: the learner will use real-world connections as they apply in		
۷.	daily life, careers, as consumers and in multicultural situations.		
Vocab	ulary		
7 th Gra	ade		
	congruent Pascal		
	point of view substitution generalize		

B. Number Operations and Relationships

Content Standard: Students in Wisconsin will use numbers effectively for various purposes, such as counting, measuring, estimating and problem solving.

Rationale: People use numbers to quantify, describe and label things in the world around them. It is important to know the many uses of numbers and various ways of representing them. Number sense is a matter of necessity, not only in one's occupation but also in the conduct of daily life, such as shopping, cooking, planning a budget or analyzing information reported in the media. When computing, an educated person needs to know which operations (e.g., addition, multiplication), which procedures (e.g., mental techniques, algorithms*), or which technological aids (e.g., calculator, spreadsheet) are appropriate.

Performance Standard:

B.8.1 Read, represent and interpret various rational numbers* (whole numbers*, decimals, fractions and percents) with verbal descriptions, geometric models* and mathematical notation (e.g., expanded*, scientific*, exponential*).

7th Grade

1.	Read, write and demonstrate integers, decimals, fractions, and percents.
2.	Express numbers in scientific notation and exponential expanded form (standard
	form)
3.	Use powers and exponents in expressions
4.	Read, write, demonstrate and graph on a number line integers, decimals, fractions and
	percent.

Performance Standard:

B.8.2 Perform and explain operations on rational* numbers (add, subtract, multiply, divide, raise to a power, extract a root, take opposites and reciprocals, determine absolute value).

7th Grade

Ι.	Add, subtract, multiply and divide decimals, fractions, mixed numbers, and
	integers
2.	Solve for, as well as write, powers and positive and negative exponents in
	expressions
3.	Understand and find the square root of perfect squares
4.	Evaluate numerical and algebraic expressions using order of operations.
5.	Reinforce solving algebraic two-step equations.
6	Recall of multiplication and division facts 0-12

Performance Standard

B.8.3 Generate and explain equivalences among fractions, decimals and percents.

7 th Gra	B. Number Operations and Relationships ade
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1.	Express terminating decimals as fractions and express fractions as decimals
	Express fractions as percents and vice versa
	Express decimals as percents and vice versa
	Formulate algebraic expressions and equations from verbal phrases and sentences
5.	Express equivalent fractions in lowest terms
Perfor	mance Standard:
B.8.4	Express order relationships among rational numbers using appropriate symbols (>, <, <, >, =).
7 th Gra	ade
1.	Compare and order decimals and fractions and integers using <, >, =
	Determine whether a pair of ratios forms a proportion by using cross products
	(= or =/)
3.	Solve proportions by using cross products
Perfor	mance Standard:
B.8.5	Apply proportional thinking in a variety of problem situations that include, but are not limited to:
	 ratios and proportions (e.g., rates, scale drawings*, similarity*)
	• percents including those greater than 100 and less than one (e.g., discounts, rate of increase or decrease, sales tax)
7 th Gra	ade
1.	Express ratios as fractions and determine whether two ratios are equivalent.
	Determine unit rates (3 apples for \$.30; how much for 1 apple?).
3.	Solve proportions
4.	Solve problems involving scale drawings
	Illustrate the meaning of percent using models or symbols
6.	Express percents greater than 100 and percents less than 1 as fractions and as decimals
7	and vice versa.
	Find the percent of a number
8.	
9. 10	<u> </u>
10	. Express similarity statements
Perfor	mance Standard:

- B.8.6 Model* and solve problems involving number-theory concepts such as:prime* and composite numbers

 - divisibility and remainders
 - greatest common factors
 - least common multiples

B. Number Operations and Relationships

7 th Grade		
1.	Find the prime factorization of a composite number	
2.	Use divisibility rules of 2, 3, 4, 5, 6, 8, 9, and 10	
3.	Find the greatest common factor of two or more numbers	
4.	Find the least common multiple of two or more numbers.	
5.	Reinforce dividing whole numbers and repeating and terminating rational decimals	
Perfor	mance Standard:	
B.8.7	In problem-solving situations, select and use appropriate computational procedures with rational numbers such as:	
	• calculating mentally	
	• estimating	
	• using technology (e.g., scientific calculators, spreadsheets)	
7 th Gra	nde	
1.	Compute sums and differences using compensation	
2.	Multiply decimals mentally by powers of 10.	
3.	Estimate sums and differences using front-end estimation	
4.	Estimate quotients using compatible numbers	
5.	Problem solving strategies:	
	Classify information, guess and check, use a graph, make a table, determine reasonable answers, use a formula, solve a simpler problem, choose the method of computation, make a list, eliminate possibilities, find a pattern, use logical reasoning, draw a diagram, make a model, work backward, use an equation and not enough information is present	
6.	Estimate with decimals	
7.	Estimate the area of irregular figures	
8.	Estimate sums and differences, products and quotients of fractions and mixed	

9. Estimate by using fractions, decimals and percents interchangeably. _____

13. Compute mentally a percent of a number. _____

10. Estimate by rounding. _____

11. Estimate square roots. ____

12. Use scientific calculators in problem-solving situations to help explain algorithms. _____

B. Number Operations and Relationships

Vocabulary			
7 th Grade	7 th Grade		
absolute value common denominator divisible irregular figures percent perfect square rate similar figures standard form corresponding sides and	additive inverse denominator equivalent lowest terms proportion population density scale factor square unit price	clustering fraction unit rate numerator percentage radical sign scientific notation square root	

C. Geometry

Content Standard: Students in Wisconsin will be able to use geometric concepts, relationships and procedures to interpret, represent and solve problems.

Rationale: Geometry and its study of shapes and relationships is an effort to understand the nature and beauty of the world. While the need to understand our environment is still with us, the rapid advance of technology has created another need: to understand ideas communicated visually through electronic media. For these reasons, educated people in the 21st century need a well-developed sense of spatial order to visualize and model real world* problem situations.

Performance Standard

- C.8.1 Describe special and complex two- and three-dimensional figures (e.g., rhombus, polyhedron, cylinder) and their component parts (e.g., base, altitude and slant height) by:
 - naming, defining and giving examples
 - comparing, sorting and classifying them
 - identifying and contrasting their properties (e.g., symmetrical, isosceles, regular)
 - drawing and constructing physical models to specifications
 - explaining how these figures are related to objects in the environment

7th Grade

1.	Identify and draw points, line segments, line rays, transversal lines, perpendicular lines,
	parallel lines, and intersecting lines
2.	Draw and construct physical models to specifications by using a compass, protractor, and
	straight edge
3.	Describe and classify angles (alternate interior, corresponding, vertical, complementary
	and supplementary, right, obtuse, acute, straight) and triangles (equilateral, isosceles,
	scalene, acute, obtuse and right)
4.	Construct angles and triangles (congruent and bisected)
5.	Calculate the sum of the angles of a polygon
6.	Identify, classify, and construct regular and irregular polygons (three-sided through
	n-sided)
7.	Identify and construct congruent, similar and symmetrical figures
8.	Construct and identify the parts of a circle including diameter and radius.
9.	Analyze three-dimensional objects by applying the knowledge of faces, edges, vertices,
	and comparison of line segments within the figure
10.	Analyze, select and present examples of three-dimensional figures in real-life
	settings
-	manas Standards

Performance Standard:

C.8.2 Identify and use relationships among the component parts of special and complex 2-and 3-dimensional figures (e.g., parallel sides, congruent* faces).

C. Geometry

7 th Gra	7 th Grade		
2. 3.	Predict a pattern for the number of diagonals in a polygon Illustrate perpendicular and parallel lines; congruent and similar figures Determine and calculate correspondence in similar figures and find missing measures Analyze three-dimensional objects by applying the knowledge of faces, edges, vertices,		
	and comparison of line segments within the figure		
Perfor	mance Standard:		
C.8.3	Identify 3-dimensional shapes from 2-dimensional perspectives and draw 2-dimensional sketches of 3-dimensional objects preserving their significant features.		
7 th Gra	ade		
1.	Plan and construct physical models to specifications		
Perfor	mance Standard:		
C.8.4	Perform transformations* on 2-dimensional figures and describe and analyze the effects of the transformations on the figures.		
7 th Gra	ade		
1.	Translate, rotate and reflect figures on the coordinate plane Design tessellations		
	Compose and diagram dilations		
Perfor	mance Standard:		
C.8.5	Locate objects using the rectangular coordinate system*.		
	• Employ technology to demonstrate the rectangular coordinate system when grade appropriate.		
7 th Gra	ade		
1. 2.	Identify ordered pairs using the rectangular coordinate system Identify and graph the transformations or movements of geometric figures shown on a coordinate grid		
3. 4.	Translate, rotate, and reflect figures on the coordinate plane Locate and examine points on earth by using the rectangular coordinate system		

C. Geometry

Vocabulary			
7 th Grade			
adjacent angle bisects congruent angle corresponding angle midpoint segment bisector vertical angle	alternate interior angle complementary angle congruent lines dilation perpendicular bisector supplementary angle	angle bisector diagonal congruent segments irregular polygon rotation transversal	

D. Measurement

Content Standard: Students in Wisconsin will select and use appropriate tools (including technology) and techniques to measure things to a specified degree of accuracy. They will use measurements in problem-solving situations.

Rationale: Measurement is the foundation upon which much technological, scientific, economic and social inquiry rests. Before things can be analyzed and subjected to scientific investigation, or mathematical modeling*, they must first be quantified by appropriate measurement principles. Measurable attributes* include such diverse concepts as voting preferences, consumer price indices, speed and acceleration, length, monetary value, duration of an Olympic race, or probability of contracting a fatal disease.

Performance Standard:

D.8.1 Identify and describe attributes* in situations where they are not directly* or easily measurable (e.g., distance, area of an irregular figure, likelihood of occurrence).

7th Grade

1.	Find irregular figures located in the nome and estimate area of each.
2.	Determine appropriate tools and accurately measure length, mass and volume.
3.	Use procedures for basic indirect measurement to find area of irregular figures.

4. Summarize the process and results of steps 2 and 3 to the class using graphics or other technologies.

Performance Standard

- D.8.2 Demonstrate understanding of basic measurement facts, principles and techniques including the following:
 - approximate comparisons between metric and US customary units (e.g., a liter and a quart are about the same; a kilometer is about six-tenths of a mile.)
 - knowledge that direct measurement* produces approximate, not exact, measures.
 - the use of smaller units to produce more precise measures.
 - employment of appropriate grade level technology.

1.	Compare and contrast metric and customary units of measure
2.	Demonstrate that each unit of measurement is part of another either smaller or larger
	unit
3.	Distinguish when it is necessary to use smaller units for more precise measure-
	ments

D. Measurement Performance Standard Determine measurement directly* using standard units (metric and US customary) with these suggested degrees of accuracy: lengths to the nearest mm or 1/16 of an inch weight (mass) to the nearest 0.1 g or 0.5 ounce liquid capacity to the nearest ml angles to the nearest degree temperature to the nearest Centigrade and Fahrenheit degree elapsed time to the nearest second 7th Grade 1. Determine measurements to the following degrees of accuracy: length to the nearest sixteenth, eighth, quarter, half-inch, foot, yard, millimeter, centimeter, meter _ weight to the nearest ounce, pound, gram, and kilogram _____ temperature to the nearest degree in Celsius and Fahrenheit time to the nearest second liquid capacity to the nearest ounce, cup, pint, quart, half-gallon, gallon, milliliter, liter, and fluid ounce angles to the nearest degree. 2. Determine appropriate units to measure length, mass, temperature, capacity and time. ____ 3. Apply measurement skills to real life problems. Performance Standard Determine measurements indirectly* using: D.8.4 estimation conversion of units within a system (e.g., quarts to cups, millimeters to centimeters) ratio and proportion (e.g., similarity*, scale drawings*) geometric formulas to derive lengths, areas, volumes of common figures (e.g., perimeter, circumference, surface area) the Pythagorean* relationship geometric relationships and properties for angle size (e.g., parallel lines and transversals; sum of angles of a triangle, vertical angles*) 7th Grade

Convert units within metric/customary systems	
Estimate measurement indirectly by using non-standard units	
Create ratio and proportion/scale drawings	
Apply geometric formulas to calculate:	
perimeter and circumference	
area of triangles, quadrilaterals, and circles	
• surface area and volume of rectangular prisms and cylinders	

D. Measurement

5.	5. Distinguish geometric relationships and properties for angle size (parallel lines and transversal; vertical, supplementary, corresponding, and alternate interior; sum of the angles of triangle.)		
6.	Apply the Pythagorean Theorem ($a + b = c$).		
7.	Solve basic rate problems (unit price, distance per unit of time)		
8.			
9.	9. Apply measurement skills to real life problems.		
Vocab	ulary		
7 th Gra	nde		
	altitude (segment in quadirilateral) base (of trapezoid) leg		
	Pythagorean Theorem similar figures similar polygons		

E. Statistics and Probability

Content Standard: Students in Wisconsin will use data collection and analysis, statistics and probability in problem solving situations, employing technology where appropriate.

Rationale: Dramatic advances in technology have launched the world into the Information Age, when data are used to describe past events or predict future events. Whether in the business place or in the home, as producers or consumers of information, citizens need to be well versed in the concepts and procedures of data analysis in order to make informed decisions.

Performance Standard

- E.8.1. Work with data in the context of real-world situations by:
 - formulating questions that lead to data collection and analysis
 - designing and conducting a statistical investigation
 - using technology to generate displays, summary statistics* and presentations

7th Grade

1. 2. 3. 4. 5. 6.	 Conduct surveys, experiments or simulations and display results Formulate questions and determine the appropriate data to collect and how to collect data Draw reasonable conclusions about real-world data Use technology to produce a simple database and be able to present it 	
Perfor	mance Standard	
E.8.2	Organize and display data from statistical investigations using: appropriate tables, graphs and/or charts (e.g., circle, bar, or line, for multiple sets of data) appropriate plots (e.g., line*, stem-and-leaf*, box*, scatter*)	
7 th Gra	ade	
1. 2. 3. 4. 5. 6.	Gather and organize data into a table Construct circle graphs Construct bar graphs and line graphs with multiple sets of data Construct line plots, stem and leaf plots, and scatter plots Assess the most effective way of displaying data Create story problems based on collected data for classmates to solve	

Performance Standard

- E.8.3 Extract, interpret and analyze information from organized and displayed data by using:
 - frequency and distribution, including mode* and range*
 - central tendencies* of data (mean* and median*)
 - indicators of dispersion (e.g., outliers*)

E. Statistics and Probability

7 th	Grade

	Predict and calculate the mean, median, mode and range from a set of data		
	 Analyze information based on frequency and distribution Assess and select the appropriate scale and interval for graphs or frequency tables 		
	Examine the effect of extreme values on measures of central tendency.		
	Assess and select the best measure of central tendency to represent data.		
	Determine and understand the function of an outlier		
	Solve data problems by extracting, interpreting, and analyzing data		
Performance Standard			
E.8.4	Use the results of data analysis to:		
	make predictions		
	develop convincing arguments		
	• draw conclusions		
7 th Grade			
1.	Predict and draw conclusions from data		
2.	Analyze data from simple line, bar, circle graphs, and scatter plots.		
	Apply results of the data analysis to solve problems		
	Determine if the conclusion drawn is valid for the data presented		
5.	Construct and present arguments to support analysis and display of data		
Performance Standard			
E.8.5	Compare several sets of data to generate, test, and, as the data dictate, confirm or deny hypotheses.		
7 th Gra	ade		
1.	Formulate a hypothesis from multiple sets of actual data.		
2.	* * * * * * * * * * * * * * * * * * *		
3.	Construct a database on the computer using charts or graphs		
4.	Prepare a presentation using technology and present it to the class		
Perfor	mance Standard:		
E.8.6	Evaluate presentations and statistical analyses from a variety of sources for:		
	• credibility of the source		
	• techniques of collection, organization and presentation of data		
	• missing or incorrect data		
	• inferences		

possible sources of bias

E. Statistics and Probability

7 th Grade		
2.	Determine if a source is credible and why Evaluate techniques of collection, organization and presentation of data Determine if any data is missing or incorrect and why	
Perfor	mance Standard:	
E.8.7	Determine the likelihood of occurrence of simple events by:	
	 using a variety of strategies to identify possible outcomes (e.g., lists, tables, tree diagrams*) conducting an experiment designing and conducting simulations* applying theoretical notions of probability (e.g., that four equally likely events have a 25% chance of happening) employing appropriate grade level technology for presentations 	
 Use a variety of strategies to identify possible outcomes (lists, tables, tree diagrams.) Design and conduct an experiment Design and conduct simulations Apply theoretical notions of probability: permutations independent/dependent events 		
Vocabulary		
	data baseintervalspermutationsextreme valuesmeanpositive & negative medianrelationshipsmodescaleoutliersectors rangespreadsheetstem & leaf plottrendindependent/dependent events	

F. Algebraic Relationships

Content Standard: Students in Wisconsin will discover, describe and generalize simple and complex patterns and relationships. In the context of real-world problem situations, the student will use algebraic techniques to define and describe the problem to determine and justify appropriate solutions.

Rationale: Algebra is the language of mathematics. Much of the observable world can be characterized as having patterned regularity where a change in one quantity results in changes in other quantities. Through algebra and the use of variables* and functions*, mathematical models* can be built which are essential to personal, scientific, economic, social, medical, artistic and civic fields of inquiry.

Performance Standard

- F.8.1 Work with algebraic expressions in a variety of ways, including:
 - using appropriate symbolism, including exponents* and variables*
 - evaluating expressions through numerical substitution
 - generating equivalent expressions
 - adding and subtracting expressions

7th Grade

1.	Use vocabulary symbols and notation of algebra correctly (n,n ,=,<,>)
	Evaluate numerical and simple algebraic expressions using order of operations.
3.	Demonstrate the use of exponents in algebraic expressions.
4.	Solve real-life problems involving algebraic expressions
5.	Write algebraic expressions from verbal phrases.

Performance Standard

- F.8.2 Work with linear and nonlinear patterns* and relationships in a variety of ways, including:
 - representing them with tables, with graphs and with algebraic expressions, equations and inequalities
 - describing and interpreting their graphical representations (e.g., slope*, rate of change, intercepts*)
 - using them as models of real-world phenomena
 - describing a real-world phenomenon that a given graph might represent

1.	Graph equations by plotting points
2.	Complete function tables
3.	Graph functions
4.	Model algebraic expressions
5.	Solve problems involving discounts and simple interest.
6	Identify inequalities

F. Algebraic Relationships

Performance Standard

F.8.3 Recognize, describe, and analyze functional relationships* by generalizing a rule that characterizes the pattern of change among variables. These functional relationships include exponential growth and decay (e.g., cell division, depreciation)

7th Grade

Performance Standard

- F.8.4 Use linear equations and inequalities in a variety of ways, including:
 - writing them to represent problem situations and to express generalizations.
 - solving them by different methods (e.g., informally, graphically, with formal properties, with technology).
 - writing and evaluating formulas (including solving for a specified variable).
 - using them to record and describe solution strategies.

7th Grade

1.	Identity, solve and graph linear equations by using mental math, the guess and check
	strategy (use of a replacement set) and inverse operations
2.	Solve problems by using a formula
3.	Solve equations:
	• proportions
	• linear equations using models
	• two-step equations using models
	• involving percents
4.	Solve and graph equations:
	• using rational numbers
	• with two variables
5.	Identify, solve and graph inequalities
6.	Use a calculator to solve equations
7.	Write algebraic equations from verbal sentences.
8.	Solve for a specified variable
9.	Solve more complex problems by writing and solving an equation.

Performance Standard

- F.8.5 Recognize and use generalized properties and relations, including:
 - additive and multiplicative property of equations and inequalities
 - commutativity* and associativity* of addition and multiplication
 - distributive* property
 - inverses* and identities* for addition and multiplication
 - transitive* property

F. Algebraic Relationships

1.	 Recognize, use, and differentiate between the basic properties of arithmetic: Order/Commutative property for +/x Zero property for +/x One/Identity Property for x/÷ Inverse property for +/- and x/÷ (12-3=9/9+3=12) Property of one for x and ÷ Associative property for + and x [5x(3x2)=(5x3)x2] Distributive property 		
2.	2. Identify and use addition, subtraction, multiplication and division properties of		
	equality		
Vocabulary			
7 th Gr	ade		
	addition property of equality base cubed multiplicative inverse powers/exponents squared subtraction property of equality	functionmultiplication property of equalitydivision property of equalityequivalent equationsfactorssubstitution	