FOR STUDENTS WHO HAVE COMPLETED ALGEBRA 1 (Students entering Geometry)

Name:	
Date:	Period:

Dear Parent/Guardian and Student,

Attached you will find a review packet of skills which each student is expected to know upon the start of the year. Students will be given a test (no calculators) on this information during the second week of the school year. Teachers will go over the answers from the packet during the first week of school and minimal direct instruction will be given on these concepts, as they are a review from Algebra 1. Students may seek additional help during RECAP to ask questions.

Topics from Algebra 1 to be tested during the second week of school.

Real Numbers and Operations Algebraic Expressions and Models Solving Linear Equations Rewriting Equations and Formulas Solving Linear Inequalities Solving Absolute Value Equations and Inequalities

Functions and Their Graphs Slope and Rate of Change Quick Graphs of Linear Equations Writing Equations of Lines Correlation and Best Fitting Lines Linear Inequalities in Two Variables

Solving Linear Systems by Graphing Solving Linear Systems Algebraically (Substitution and Linear Combinations) Graphing and Solving Systems of Linear Inequalities

Adding, Subtracting, Multiplying Polynomials Factoring

You may also access the following websites to assist your child.

www.purplemath.com, www.math.com, www.khanacademy.com

It is recommended that students who score between 80 and 100 continue with the current course. Students who score below an 80 may consider retaking Algebra 1, as it is imperative for future successes in math to have essential, baseline skills.

Have a good summer.

The PAMS Math Department

1. <u>Real Numbers and Operations</u>

Whole:0, 1, 2, ...Integers: ..., -2, -1, 0, 1, 2...Rational:Can be written as a fraction or a repeating or terminating decimal.Irrational:Cannot be written as a fraction or a repeating or terminating decimal.

Properties of Addition and Multiplication

1. Commutative Property: a + b = b + a

- 2. Associative Property: (a + b) + c = a + (b + c)
- 3. Identity Property: a + 0 = a for addition, $a \bullet 1 = 1$ for multiplication
- 4. Inverse Property: a + (-a) = 0 for addition, $a \bullet \frac{1}{a} = 1$
- 5. Distributive Property: a(b + c) = ab + bc

<u>**Practice Set 1**</u> - Identify the following numbers as either W, In, R, or Irr. Remember, the numbers could fall into more than one category!

1. 4.5 2. -17 3. $\frac{2}{3}$ 4. $\sqrt{15}$ 5. $\sqrt{16}$

6. Plot the following values on a number line. $-\frac{4}{3}, \sqrt{2}, 2.7, \pi, -1.2$

7.

- a. What is the sum of -9 and 16?
- b. What property is represented here: 4 + (1+5) = (4+1) + 5
- c. What property is represented here: $8 = 8 \cdot 1$
- d. True or False: (a b) = (b a)

2. <u>Algebraic Expressions and Models</u>

Order of Operations	<u>Vocabulary</u>
Parentheses Exponents Multiplication Division Addition Subtraction } From left to right!	<u>Terms</u> : Parts added together to make the expression. <u>Coefficients</u> : The number located in front of the variable. <u>Constant</u> : Numbers in an expression without a variable.

Practice Set 2

1. Simplify the following: a. 3^4 b. $(-3)^4$ c. $-(3)^4$

2. Simplify: a.
$$\frac{-4+2(-2+5)^2}{5-(2-4)^3}$$
 b. $-3x^2-5x+7$, when $x=-2$

c.
$$6^2 \div 4 \bullet 3 - (8 - 5) + 2^3$$

3. Identify the following components from the following expression. $5x^7 - 8x + 47$

a. The number of terms b. *Leading* coefficient c. Constant Term

4. Simplify: a. $3x^2 - x + 7 - x^2$ b. 2(x+1) - 3(2x-4)

c.
$$4(x^2-2)-2(3-5x^2)$$

3. Solving Linear Equations

Practice Set 3:

1. Solve the following equations.

a.
$$\frac{3}{7}x + 9 = 15$$
 b. $5n + 11 = 7n - 9$

c.
$$4(3x-5) = -6\left(-\frac{5}{3}x+8\right) - 6x$$
 d. $\frac{1}{3}x + \frac{1}{4} = x - \frac{1}{6}$

4. <u>Rewriting Equations and Formulas</u>

Practice Set 4:

1. Solve the following equation for *y*. 7x - 3y = 8

2. Solve the Fahrenheit equation for Celsius.
$$F = \frac{9}{5}C + 32$$

5. Solving Linear Inequalities



Practice Set 5

1. Graph the following solutions on the number line provided:

◀		→	←	 •	
a.	<i>x</i> < 3		b. $x \ge -5$	c. $7 \ge x$	

- 2. Solve and graph the following inequalities.
 - a. -5x-8 < 12 b. $-2 \le 3x-8 \le 10$ c. 2x+3 < 12 or 4x-7 > 21

6. Solving Absolute Value Equations and Inequalities

*The absolute value of a number x, is written |x|, is the distance the value is from zero. The absolute value of a number is always positive. |x| = 5 or -5

Example 1: Solve:
$$|2x-5|=9 \longrightarrow 2x-5=9$$
 or $2x-5=-9$
 $x=7$ or $x=-2$

*To solve an absolute value inequality, it is important to remember that $a < or \leq$ represents an *and* statement and $a > or \geq$ represents an *or* statement.

Example 2:	2x+7 < 11		$ 3x-2 \ge 8$			
Example 2:	-11 < 2x + 7 < 11 -18 < 2x < 4	Example 3:	$3x - 2 \le -8$	or	$3x - 2 \ge 8$	
	-9 < x < 2		$x \leq -2$	or	$x \ge \frac{10}{3}$	

Practice Set 6:

Directions: Solve the following absolute value equations.

1. |6x-3| = 152. |4x+7| - 11 = -2

<u>Directions</u>: Solve and graph the following absolute value inequalities.

3.
$$|4x+10| < 20$$
 4. $|x-16| \ge 24$

7. Finding Slope



Practice Set 7:

<u>Directions</u>: Find the slope of the following lines.



5. (8, 10), (-7, 14)	6. (-19, 6), (15, 16)

8. Graphing Linear Equations



Practice Set 8:

Directions: Graph the following equations.

1. y = 3x - 1 m = 2 b = 22. $y = \frac{-2}{3}x + 2$ b = 2 x - int. y = -6y - int.



9. Graphing Linear Inequalities

- 1. Graph the line the same way you would any other linear equation.
- 2. Remember, $\langle or \rangle$ represents a dashed line and $\leq or \geq$ represents a solid line.
- 3. Chose a test point on the graph to see if it satisfies the inequality. If it does, shade to cover the test point as it is a solution. If it does not work, shade away from it.

Example: Graph
$$y < -\frac{1}{4}x + 3$$

Test Point: (0, 0)
 $0 < \frac{1}{4}(0) + 3$
 $0 < 3$
TRUE, so shade toward (0, 0)



Practice Set 9:

Directions: Graph the following inequalities.

1.
$$y > -2x - 3$$
 2. $-3y \ge -12x - 6$ 3. $4y + 3 < 4$



10. Writing Linear Equations in Slope-Intercept Form

Slope	e-intercept form:		Imnortant!
	y = mx + b	(-4, 5), (1, -9)	<u>important.</u>
1)	Find the slope of the line.	$m = \frac{-9-5}{1-(-4)} = \frac{-14}{5}$	*1. Two lines are parallel if they have the same slope.
2)	Find the <i>y</i> -intercept.	$-9 = \frac{-14}{5}(1) + b$ $-9 = \frac{-14}{5} + b$	*2. Two lines are perpendicular if they have opposite reciprocal slopes.
		$-9 - \left(\frac{-14}{5}\right) = \frac{5}{-14} - \left(\frac{-14}{5}\right)$ $\frac{-31}{5} = b$	
3)	Write an equation of the line.	$y = \frac{-14}{5}x + \frac{-31}{5}$	

<u>Practice Set 10</u>: <u>Directions</u>: Write the equation of the line in slope-intercept form.

	1 1
1. $(2,-1), m=3$	2. (3,4), $m = \frac{1}{2}$
3. Write the equation of the line that is parallel	4. Write the equation of the line perpendicular
to $y = 4x - 5$ and passes through (-3, 10).	to $y = \frac{1}{4}x + 7$ and passes through (2, -9).
5. Passes through (-4,-1),(-9,2)	6. Passes through (-17,-8),(-7,-4)

11. Writing Linear Equations in Point-Slope Form

Example 1:	Example 2:
$m = \frac{3}{4}, (-5, 4)$	(-4,1) and $(5,-3)$
$m = \frac{3}{4}$	$m = \frac{-3-1}{5-(-4)} = \frac{-4}{9}$
$y - 4 = \frac{3}{4}(x + 5)$	$y-1 = \frac{-4}{9}(x+4) \ OR \ y+3 = \frac{-4}{9}(x-5)$
	Example 1: $m = \frac{3}{4}, (-5, 4)$ $m = \frac{3}{4}$ $y - 4 = \frac{3}{4}(x + 5)$

<u>Practice Set 11</u>: <u>Directions</u>: Write the equation in point-slope form.

1. $(2,-1), m=3$	2. (3,4), $m = \frac{1}{2}$
3. (5,12), (6,-2)	4. (-4,-1), (-9,2)

12. Writing Linear Equations in Standard Form

Standard Fo	orm:	Example 1:	Example 2:
Ax +	-By = C		
1. Isolat	e the variable terms	$y = \frac{2}{5}x - 3$	(2, -2), (3, -4)
on the term of	e left and the constant on the right.	$-\frac{2}{5}x + y = -3$	$m = \frac{-4 - (-2)}{3 - 2} = \frac{-2}{1}$
3 Multi	nly each side by -5	$-5\left(-\frac{2}{5}x+y\right) = -5(-3)$	y-3=-2(x+4)
to hav	ve integer coefficients	2x - 5y = 15	y - 3 = -2x - 8
and A	to be positive.		2x + y = -5

<u>Practice Set 12</u>: <u>Directions</u>: Write the equation in standard form with integer coefficients.

1. $4x - y - 7 = 0$	2. $y = -\frac{3}{4}x + \frac{5}{2}$
3. $3x + 9 = \frac{7}{2}y$	4. (2,9), <i>m</i> = -7

13. Writing an Equation for Line of Best Fit



<u>Practice Set 13</u>: <u>Directions</u>: Draw a scatter plot of the data, approximate a best-fit line, and state the correlation.

1.	(0)	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
Year, t	1980	1981	1982	1983	1984	1985	1986	1987	1988
Pounds, h	1.6	1.8	2.2	2.3	2.7	2.9	3.5	3.6	4.2
	***Use t =		esent 1980						

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14. Solving Linear Systems by Graphing



Practice Set 14: <u>Directions</u>: Solve the following systems of equations by graphing.





15. Solving Linear Systems using Substitution

Substit	ution:	
1)	Solve one of the equations for one of its variables.	3x + 4y = -4
		$x + 2y = 2 \Rightarrow x = -2y + 2$
2)	Substitute the expression into the other equation	
	and solve for the other variable.	3(-2y+2) + 4y = -4
		-6y + 6 + 4y = -4
		-2y + 6 = -4
		-2y = -10
		y = 5
3)	Substitute the value into any equation from step 1	
	to solve for the other variable.	x = -2y + 2
		x = -2(5) + 2
4)	Write you answer as an ordered pair.	x = -8
		(-8, 5)

Problem Set 15: Directions: Solve the system using substitution.

1. $2x - 5y = 9$	2. $6x + 2y = 1$
-3x + y = -7	4x + y = 6
3. $x - 2y = -1$	4. $6x + 3y = -9$
5x - 10y = 4	2x + y = -3

16. Solving Linear Systems using Linear Combinations (Elimination)

Linear Combinations:				
1) Arrange all equations with like terms in columns.	$2x+6y=4 \rightarrow 3(2x+6y=4) 3x-7y=6 \rightarrow -2(3x-7y=6)$			
 Multiply one or both of the equations by a constant to obtain the same coefficients that differ in sign. 	6x + 18y = 12 $-6x + 14y = -12$	2x + 6y = 4 $2x + 6(0) = 4$		
3) Add the revised equations.	32y = 0 $y = 0$	2x = 4 $x = 2$		
4) Substitute the value into the equation from step 1.5) Write your answer as an ordered pair.	(2,0)			

Problem Set 16: Directions: Solve the system using linear combinations.

1. $2x - 3y = 4$	2. $x - 2y = -1$
16r + 6y = 2	5x - 10y = -5
	<i>SN</i> 10 <i>y</i> 5
3 - 2r + 3u - 8	1 - 3x - 9y - 3
5. 2x + 5y = 0	4. $5x - y = 5$
x - 5y = -4	-x + 3y = 13

17. Solving Linear Inequalities by Graphing



Problem Set 17: Directions: Solve the system of linear inequalities by graphing.





18. Writing and Solving Real World Systems

Writing a System of Equations

- 1) Define your unknowns.
- 2) Create a system to represent the problem.
- 3) Solve the system using the method of your choice.

Example: Rex wants to sign up with a new internet provider.

Internet Provider	Monthly Membership	Hourly Use Fee
Inter-Speedway	\$85	\$0.85
Cyber-Zone	\$60	\$1.35

• Write a system of equations to represent this situation.

x =# hours y =total cost y = .85x + 85

$$y = 1.35x + 60$$

 After how many hours will the cost of the different companies be the same? Use mathematics to explain your answer. Use words, symbols, or both to support your explanation.

Use substitution to solve:

y = .85x + 85	.85x + 85 = 1.35x + 60	y = .85x + 85
y = 1.35x + 60	5x = -25	y = .85(50) + 85
	x = 50	<i>y</i> = 42.5

After 50 hours, the cost at each company will be \$42.50.

<u>Problem Set 18</u>: <u>Directions</u>: Create a system to represent each real world scenario. Then, solve using the method of your choice.

1. A piggy bank contains a total of 84	2. The William	s family is going	to the						
coins in nickels and quarters worth 12.80 .	Jonnstown Summer Carnival. They have								
piggy bank?	two nexet options as shown in the table.								
L-287 cmm.	Ticket	Admission	Price per						
	Option	Price	Ride						
	A	\$5	\$0.30						
	В	\$3	\$0.80						
	How many ride in order for the same as the cos the cost be at th	s will the Willian cost of ticket option t for ticket option at time?	so.so ns have to ride ion A to be the B? What will						

19. Polynomials

1. Multiply Polynomials Use the distributive property to multiply. Ex. $(5x)(9x^2 - 8)$ Ex. (2x - 4)(-9x + 3) ***You can FOIL!!! $45x^3 - 40x$ $-18x^{2} + 6x + 36x - 12$ $-18x^{2} + 42x - 12$ 2. Factoring Factor each polynomial. Ex. $(6x^3 - 18x^2 - 54x)$ Ex. $-4a^2b - 8ab^2 + 2ab$ $6x(x^2 - 3x - 9)$ 2ab(-2a - 4b + 1)3. Factoring using *ac* method (when a = 1). Ex. Factor $x^2 + 9x - 36$ $a \cdot c = 1 \cdot (-36) = -36$ 1. Multiply the *a* and *c* terms. $12 \cdot (-3) = -36$ 2. Determine what two values multiply to the *ac* term but add to the *b* term. 12 + (-3) = 9 $x^2 + 9x - 36$ 3. Rewrite your middle term with these $x^2 + 12x - 9x - 36$ two numbers, split the new polynomial $x^2 + 12x \qquad -9x - 36$ and factor. x(x + 12) - 9(x + 12)(x + 12)(x - 9)4. Solving using *ac* method (when $a \neq 1$). Ex. Solve $3x^2 - 17x + 10 = 0$ 1. Multiply the *a* and *c* terms. $a \bullet c = 3 \bullet (10) = 30$ 2. Determine what two values multiply $-2 \cdot (-15) = 30$ -2 + (-15) = -17to the *ac* term but add to the *b* term. $3x^2 - 17x + 10 = 0$ 3. Rewrite your middle term with these $3x^2 - 2x - 15x + 10 = 0$ two numbers, split the new polynomial $3x^2 - 2x - 15x + 10 = 0$ and factor. x(3x-2) - 5(3x-2) = 0(x-5)(3x-2) = 0x-5=0 3x-2=0x=5 $x=\frac{2}{3}$ 4. Solve for your solutions. $x = 5, \frac{2}{2}$

<u>Problem Set 19</u>: Use the directions to complete each problem.

<u>Multiply.</u>

1.
$$4y(6y^4 - 2y + 5)$$
 2. $(3x + 4)(-5x + 9)$

3. $(2x+5)(5x^2-x-3))$

<u>Factor</u>.

4. $x^2 + 15x + 44$

5. $x^2 - x - 42$

6. $x^2 - 30x + 56$

7. $2x^2 + 9x - 18 = 0$ 8. $4x^2 - 13x + 10 = 0$

9. $4x^2 + 17x = -15$ (*HINT*: Set problem equal to zero before beginning!)

1. R2. In, R3. R4. Irr5. W, In, R6.
$$-\frac{4}{3}$$
, -1.2 , $\sqrt{2}$, 2.7 , π 7. a. 7b. Association of Addition
c. Identity of Multiplicationd. False

Practice Set 2

1. a. 81
 b. 81
 c. -81

 2. a.
$$\frac{14}{13}$$
 b. 5
 c. 32

 3. a. Three
 b. 5
 c. 47

 4. a. $2x^2 - x + 7$
 b. $-4x + 14$
 c. $14x^2 - 14$

Practice Set 3

1. a.
$$x = 14$$
 b. $n = 10$ c. $x = -\frac{7}{2}$ d. $x = \frac{5}{8}$

Practice Set 4

1.
$$y = \frac{7}{3}x - \frac{8}{3}$$
 2. $C = \frac{5}{9}(F - 32)$



1.
$$x = -2, 3$$

2. $x = \frac{1}{2}, -4$
3. $-7\frac{1}{2} < x < \frac{5}{2}$
4. $x \le -8 \text{ or } x \ge 40$
 -7.5
 2.5
 -8
 40

Practice Set 7

1. $m = \frac{3}{1}$ 2. $m = -\frac{1}{2}$ 3. $m = \frac{0}{1} = 0$ 4. Undefined 5. $m = \frac{4}{-15}$ 6. $m = \frac{5}{17}$

Practice Set 8











1.
$$y = 3x - 7$$

2. $y = \frac{1}{2}x + \frac{5}{2}$
3. $y = 4x + 22$
4. $y = -4x - 1$
5. $y = -\frac{3}{5}x - \frac{17}{5}$
6. $y = \frac{2}{5}x - \frac{6}{5}$

Practice Set 11

1.
$$y+1=3(x-2)$$
 2. $y-4=\frac{1}{2}(x-3)$

3.
$$y-12 = -14(x-5)$$
 OR $y+2 = -14(x-6)$
4. $y+1 = -\frac{3}{5}(x+4)$ OR $y-2 = -\frac{3}{5}(x+9)$

Practice Set 12

1. 4x - y = 7 2. 3x + 4y = 10 3. 6x - 7y = -18 4. 7x + y = 23

Practice Set 13

- 1. The equation should be close to y = .32x + 1.49
- 2. The equation should be close to y = .43x + 45.29





1.
$$(2, -1)$$
 2. $\left(\frac{11}{2}, -16\right)$ 3. No Solution 4. Infinite Solutions

Practice Set 16





1.
$$\begin{aligned} x + y &= 84 \\ .05x + .25y &= 12.80 \end{aligned}$$
$$\begin{aligned} y &= 41 \text{ nickels} \end{aligned}$$
$$\begin{aligned} y &= .3x + 5 \\ 2y &= .8x + 3 \end{aligned}$$
$$\begin{aligned} y &= The \text{ total will be $6.20} \end{aligned}$$

1.
$$24y^5 - 8y^2 + 20y$$

2. $-15x^2 + 7x + 36$
3. $10x^3 + 23x^2 - 11x - 15$
4. $(x + 11)(x + 4)$
5. $(x - 7)(x + 6)$
6. $(x - 28)(x - 2)$
7. $x = \frac{3}{2}, -6$
8. $x = \frac{5}{4}, 2$
9. $x = -\frac{5}{4}, -3$