Geometry – Things to Remember!

3-D Figures:

Prism: $V = Bh$

Pyramid: $V = \frac{1}{3}Bh$

Cylinder: $V = \pi r^2 h$; $SA = 2\pi rh + 2\pi r^2$

Cone: $V = \frac{1}{3}\pi r^2 h$; $SA = s\pi r + \pi r^2$

Sphere: $V = \frac{4}{3}\pi r^3$; $SA = 4\pi r^2 = \pi d^2$

Regular Solids:

Tetrahedron – 4 faces
Cube – 6 faces
Octahedron – 8 faces
Dodecahedron – 12 faces
Icosahedron – 20 faces

Triangles:

By Sides:
Scalene – no congruent sides
Isosceles – 2 congruent sides
Equilateral – 3 congruent sides

By Angles:
Acute – all acute angles
Right – one right angle
Obtuse – one obtuse angle
Equiangular – 3 congruent angles(60º)
Equilateral ↔ Equiangular

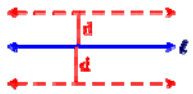
Exterior angle of a triangle equals the sum of the 2 non-adjacent interior angles.

Mid-segment of a triangle is parallel to the third side and half the length of the third side.

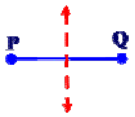
Locus Theorems:

Fixed distance from point.

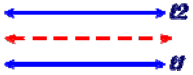
Fixed distance from a line.



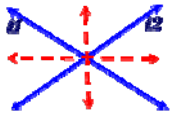
Equidistant from 2 points.



Equidistant 2 parallel lines.



Equidistant from 2 intersecting lines



Polygon Interior/Exterior Angles:

Sum of int. angles = $180(n-2)$

Each int. angle (regular) = $\frac{180(n-2)}{n}$

Sum of ext. angles = 360

Each ext. angle (regular) = $\frac{360}{n}$

Congruent Triangles

SSS
SAS
ASA
AAS
HL (right triangles only)

NO donkey theorem (SSA or ASS)

CPCTC (use after the triangles are congruent)

Related Conditionals:

Converse: switch if and then
Inverse: negate if and then
Contrapositive: inverse of the converse (contrapositive has the same truth value as the original statement)

Inequalities:

--Sum of the lengths of any two sides of a triangle is greater than the length of the third side.
--Longest side of a triangle is opposite the largest angle.
--Exterior angle of a triangle is greater than either of the two non-adjacent interior angles.

Pythagorean Theorem:

$c^2 = a^2 + b^2$

Converse: If the sides of a triangle satisfy $c^2 = a^2 + b^2$ then the triangle is a right triangle.

Similar Triangles:

AA
SSS for similarity
SAS for similarity
Corresponding sides of similar triangles are in proportion.

Mean Proportional in Right Triangle:

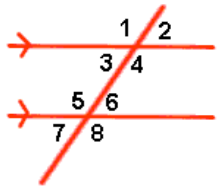
Altitude Rule:

$$\frac{\text{part of hyp}}{\text{altitude}} = \frac{\text{altitude}}{\text{other part hyp}}$$

Leg Rule:

$$\frac{\text{hypotenuse}}{\text{leg}} = \frac{\text{leg}}{\text{projection}}$$

Parallels: If lines are parallel …



Corresponding angles are equal.
m<1=m<5, m<2=m<6, m<3=m<7, m<4=m<8
Alternate Interior angles are equal.
m<3=m<6, m<4=m<5
Alternate Exterior angles are equal.
m<1=m<8, m<2=m<7
Same side interior angles are supp.
m<3+m<5=180, m<4+m<6=180

Quadrilaterals:

Parallelogram: opp sides parallel
opp sides =
opp angles =
consec. angles supp
diag bis each other
Rectangle: add 4 rt angles, diag. =
Rhombus: add 4 = sides, diag. perp, diag bisect angles.
Square: All from above.

Trapezoid:
Only one set parallel sides.

Median of trap is parallel to both bases and = ½ sum bases.:
Isosceles Trap:
legs =
base angles =
diagonals =
opp angles supp

Transformations:

$r_{x\text{-axis}}(x,y) = (x,-y)$
$r_{y\text{-axis}}(x,y) = (-x,y)$
$r_{y=x}(x,y) = (y,x)$
$r_{y=-x}(x,y) = (-y,-x)$
$r_{origin}(x,y) = (-x,-y)$
$T_{a,b}(x,y) = (x+a, y+b)$
$D_k(x,y) = (kx,ky)$
$R_{90°}(x,y) = (-y,x)$
$R_{180°}(x,y) = (-x,-y)$
$R_{270°}(x,y) = (y,-x)$

Glide reflection is composition of a reflection and a translation.

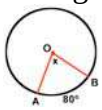
Isometry – keeps length.

Orientation – label order

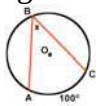
Circle Segments
In a circle, a radius perpendicular to a chord bisects the chord.
Intersecting Chords Rule:
(segment part)•(segment part) =
(segment part)•(segment part)
Secant-Secant Rule:
(whole secant)•(external part) =
(whole secant)•(external part)
Secant-Tangent Rule:
(whole secant)•(external part) = (tangent)^2
Hat Rule: Two tangents are equal.

Circle Angles:

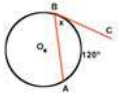
Central angle = arc



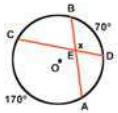
Inscribed angle = half arc



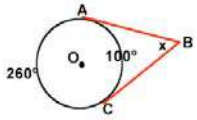
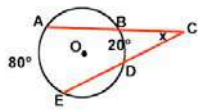
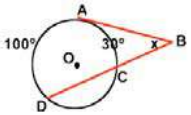
Angle by tangent/chord = half arc



Angle formed by 2 chords = half the sum of arcs



Angle formed by 2 tangents, or 2 secants, or a tangent/secant = half the difference of arcs

Slopes and Equations:

$m = \frac{vertical\ change}{horizontal\ change} = \frac{y_2 - y_1}{x_2 - x_1}$.

$y = mx + b$ slope-intercept

$y - y_1 = m(x - x_1)$ point-slope

Coordinate Geometry Formulas:

Distance Formula:

$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

Midpoint Formula:

$(x, y) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$

Circles:

Equation of circle center at origin:

$x^2 + y^2 = r^2$ where r is the radius.

Equation of circle not at origin:

$(x-h)^2 + (y-k)^2 = r^2$ where (*h*,*k*) is the center and r is the radius.