

Student Time Expectation per day: **30 minutes**

Content Area & Materials	Learning Objectives	Tasks	Check-in Opportunities	Submission of Work for Grades	
<p>Digital</p> <p>(If you can work digitally, please do. It will help to keep us all safe 😊)</p> <p>Khan Academy (KA) Access Code: G2Z9QPT5</p> <p>EdPuzzle (EP) Access Code: WEFOBEC</p>	<p><u>Suggested Order / Pacing</u></p> <ul style="list-style-type: none"> Angles of Rotation/ Reference Angles and Arc Length (Monday) Radians/Conversion (Tuesday) Triangle on a Coordinate Plane (Wednesday) Building the Unit Circle (Thursday-Friday) 	<ul style="list-style-type: none"> Students are to complete the assigned Khan Academy and EdPuzzle Assignments. 	<p>Mrs. De La Mora is available during the office hours at the times indicated below.</p> <ul style="list-style-type: none"> 12:00 – 2:00 pm Monday-Friday Remind App CODE: 9b69ee adelamora@tusd.net 	<ul style="list-style-type: none"> KA assignments will be recorded with the highest scores attained 	
<p>Hard Copy (Please only use this if you do not have technology available)</p> <ul style="list-style-type: none"> Notes + Examples Assignments <div style="border: 2px solid red; border-radius: 50%; padding: 10px; display: inline-block; margin-top: 20px;"> <p>Do these assignments ONLY if you do not have digital access.</p> </div>	<p><u>Suggested Order / Pacing</u></p> <ul style="list-style-type: none"> Angles of Rotation/ Reference Angles and Arc Length (Monday) Radians/Conversion (Tuesday) Triangle on a Coordinate Plane (Wednesday) Building the Unit Circle (Thursday-Friday) 	<ul style="list-style-type: none"> Students are to read the lesson and examples provided On a separate sheet of paper for each assignment, complete ALL problems showing your work. 	<p>Mrs. De La Mora is available during the office hours at the times indicated below.</p> <ul style="list-style-type: none"> 12:00 – 2:00 pm Monday-Friday Remind App CODE: 9b69ee adelamora@tusd.net 	<ul style="list-style-type: none"> Group your work together for your math class IN ORDER, and with the following labels clearly displayed: <div style="border: 1px solid black; padding: 5px; margin-top: 5px;"> <p>Student Name: Teacher Name: Class Name/Subject: Period: Assignment Week #</p> </div> <ul style="list-style-type: none"> Assignments will be scored on accuracy. 	
<p>Scheduled, if possible,</p> <ul style="list-style-type: none"> Discussion 	<p>Zoom classes can be held during tutoring hours. Schedule your meetings by visiting the class website: kimballmath.wordpress.com</p> <p>Discussions will revolve around discovery and application of concepts assigned for the week.</p>				
<p>Scaffolds & Supports</p>	<p>KA assignments can often be re-tried to improve learning. Videos are utilized to demonstrate not only key concepts, but also frequent points of errors, helping students avoid pitfalls.</p>				
<p>Teacher Office Hours 2 hours daily (all classes):</p> <ul style="list-style-type: none"> Contact Platform 	<p>Monday</p> <p>12:00 – 2:00 pm</p>	<p>Tuesday</p> <p>12:00 – 2:00 pm</p>	<p>Wednesday</p> <p>12:00 – 2:00 pm</p>	<p>Thursday</p> <p>12:00 – 2:00 pm</p>	<p>Friday</p> <p>12:00 – 2:00 pm</p>

Student Name:
 Teacher Name: **De La Mora**
 Class Name/Subject:
Algebra 2
 Period:
 Assignment Week #: **2**

NOTES: Complete all work on a separate sheet of paper. Include the heading provided on each worksheet you turn in. Show all work.

Monday

Answer **exactly**, using a **simplified radical** if needed.

Do not convert to decimals unless the problem starts with a decimal. Round your answer to the nearest hundredth.

Main Ideas/Questions	Notes
Angles in Standard Form 	<ul style="list-style-type: none"> An angle on the coordinate plane is in standard form when the vertex is on the origin and one ray lies on the positive x-axis. The ray on the x-axis is called the <u>initial side</u>. The other ray is called the <u>terminal side</u>. Counterclockwise rotations result in <u>positive</u> angle measures. Clockwise rotations result in <u>negative</u> angle measures. One full revolution = <u>360°</u>.
Drawing Angles	Directions: Sketch an angle with the given measure in standard position. 1. 75° 2. -160° 3. 430°
Coterminal Angles	Angles in standard position with the same terminal side are coterminal angles . Give two coterminal angles for each given angle, one positive and one negative: 10. 65° $65 + 360 = 425°$ $65 - 360 = -295°$ 11. 540° $540 - 360 = 180°$ $180 - 360 = -180°$ 12. $\frac{13\pi}{18}$ $\frac{13\pi}{18} + 2\pi = \frac{49\pi}{9}$ $\frac{13\pi}{18} - 2\pi = -\frac{23\pi}{9}$ 13. $\frac{14\pi}{9}$ $\frac{14\pi}{9} + 2\pi = \frac{32\pi}{9}$ $\frac{14\pi}{9} - 2\pi = -\frac{4\pi}{9}$
Reference Angles	For an angle θ in standard form, the reference angle is the positive acute angle formed by the terminal side and the x-axis. Sketch and find the reference angles for each angle: 14. 225° $225 - 180 = 45°$ 15. -310° $-310 + 360 = 50°$ 16. $\frac{2\pi}{3}$ (120°) $\pi - \frac{2\pi}{3} = \frac{\pi}{3}$

Directions: Sketch each angle. Then give two coterminal angles (one positive and one negative) and the reference angle.

13. 115° Coterminal 4°: $115 + 360 = 475°$, $115 - 360 = -245°$. Reference 4°: $180 - 115 = 65°$

14. 350° Coterminal 4°: $350 + 360 = 710°$, $350 - 360 = -10°$. Reference 4°: $360 - 350 = 10°$

17. $\frac{5\pi}{18}$ (50°) Coterminal 4°: $\frac{5\pi}{18} + 2\pi = \frac{41\pi}{9}$, $\frac{5\pi}{18} - 2\pi = -\frac{31\pi}{9}$. Reference 4°: $\pi - \frac{5\pi}{18} = \frac{13\pi}{18}$

18. $\frac{11\pi}{9}$ (130°) Coterminal 4°: $\frac{11\pi}{9} + 2\pi = \frac{29\pi}{9}$, $\frac{11\pi}{9} - 2\pi = -\frac{7\pi}{9}$. Reference 4°: $\pi - \frac{11\pi}{9} = \frac{8\pi}{9}$

Reference Angle
 Standard Angle = θ
 Reference Angle = θ'

Quadrant II: $\theta' = 180 - \theta$
 Quadrant III: $\theta' = \theta - 180$
 Quadrant I: $\theta' = \theta$
 Quadrant IV: $\theta' = 360 - \theta$

Tuesday

Radians vs. Degrees	A radian is a unit of angle measure based on arc length. One radian is defined as the measure of the angle formed when the radius is equivalent to the length of the intercepted arc. Recall that the circumference of a circle is $2\pi r$, therefore: $360° = 2\pi$ radians ; $180° = \pi$ radians 				
	<table border="1"> <tr> <td>Converting Degrees → Radians</td> <td>Converting Radians → Degrees</td> </tr> <tr> <td>Radians = Degrees $\cdot \left(\frac{\pi \text{ radians}}{180}\right)$</td> <td>Degrees = Radians $\cdot \left(\frac{180}{\pi \text{ radians}}\right)$</td> </tr> </table>	Converting Degrees → Radians	Converting Radians → Degrees	Radians = Degrees $\cdot \left(\frac{\pi \text{ radians}}{180}\right)$	Degrees = Radians $\cdot \left(\frac{180}{\pi \text{ radians}}\right)$
Converting Degrees → Radians	Converting Radians → Degrees				
Radians = Degrees $\cdot \left(\frac{\pi \text{ radians}}{180}\right)$	Degrees = Radians $\cdot \left(\frac{180}{\pi \text{ radians}}\right)$				
Degrees → Radians	Directions: Convert each measure to radians. 4. 30° $30 \cdot \frac{\pi}{180} = \frac{30\pi}{180} = \frac{\pi}{6}$ 5. 150° $150 \cdot \frac{\pi}{180} = \frac{150\pi}{180} = \frac{5\pi}{6}$ 6. -220° $-220 \cdot \frac{\pi}{180} = -\frac{220\pi}{180} = -\frac{11\pi}{9}$				
Radians → Degrees	Directions: Convert each measure to degrees. 7. $\frac{4\pi}{3}$ $\frac{4\pi}{3} \cdot \frac{180}{\pi} = \frac{720}{3} = 240°$ 8. $-\frac{5\pi}{36}$ $-\frac{5\pi}{36} \cdot \frac{180}{\pi} = -\frac{900}{36} = -25°$ 9. $\frac{7\pi}{4}$ $\frac{7\pi}{4} \cdot \frac{180}{\pi} = \frac{1260}{4} = 315°$				
	Directions: Convert each measure to radians. 1. 225° $225 \cdot \frac{\pi}{180} = \frac{225\pi}{180} = \frac{5\pi}{4}$ 2. 20° $20 \cdot \frac{\pi}{180} = \frac{20\pi}{180} = \frac{\pi}{9}$ 3. -255° $-255 \cdot \frac{\pi}{180} = -\frac{255\pi}{180} = -\frac{17\pi}{12}$				
	Directions: Convert each measure to degrees. 7. $\frac{23\pi}{12}$ $\frac{23\pi}{12} \cdot \frac{180}{\pi} = \frac{4140}{12} = 345°$ 8. $-\frac{31\pi}{36}$ $-\frac{31\pi}{36} \cdot \frac{180}{\pi} = -\frac{5580}{36} = -155°$ 9. $\frac{\pi}{12}$ $\frac{\pi}{12} \cdot \frac{180}{\pi} = \frac{180}{12} = 15°$				

Answer **exactly**, using a **simplified fractions**.

Remember to **cross cancel** to **simplify fractions**.

Watch the signs!

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Wednesday

Ratios must be exact
 answers. Do not convert
 to decimals.

Trig Functions

Let θ be an angle in standard form and $P(x, y)$ be a point on the terminal side of θ . The distance from P to the origin, r , can be found using the formula:
 $x^2 + y^2 = r^2$ (The Pythagorean Theorem).

$\sin \theta = \frac{y}{r}$	$\cos \theta = \frac{x}{r}$	$\tan \theta = \frac{y}{x}$
$\csc \theta = \frac{r}{y}$	$\sec \theta = \frac{r}{x}$	$\cot \theta = \frac{x}{y}$

17. $P(5, -2)$ is a point on the terminal side of θ in standard form. Find the exact values of the trigonometric functions of θ :

$5^2 + 2^2 = r^2$
 $25 + 4 = r^2$
 $29 = r^2$
 $r = \sqrt{29}$

$x = 5$
 $y = -2$

$\sin \theta = \frac{-2}{\sqrt{29}} = -\frac{2\sqrt{29}}{29}$	$\cos \theta = \frac{5}{\sqrt{29}} = \frac{5\sqrt{29}}{29}$	$\tan \theta = -\frac{2}{5}$
$\csc \theta = -\frac{\sqrt{29}}{2}$	$\sec \theta = \frac{\sqrt{29}}{5}$	$\cot \theta = -\frac{5}{2}$

19. $(-5, 12)$

$5^2 + 12^2 = r^2$
 $25 + 144 = r^2$
 $169 = r^2$
 $13 = r$

$x = -5$
 $y = 12$
 $r = 13$

$\sin \theta = \frac{12}{13}$	$\csc \theta = \frac{13}{12}$
$\cos \theta = -\frac{5}{13}$	$\sec \theta = -\frac{13}{5}$
$\tan \theta = -\frac{12}{5}$	$\cot \theta = -\frac{5}{12}$

20. $(2, 8)$

$2^2 + 8^2 = r^2$
 $4 + 64 = r^2$
 $68 = r^2$
 $2\sqrt{17} = r$

$x = 2$
 $y = 8$
 $r = 2\sqrt{17}$

$\sin \theta = \frac{8}{2\sqrt{17}} = \frac{4\sqrt{17}}{17}$	$\csc \theta = \frac{2\sqrt{17}}{8} = \frac{\sqrt{17}}{4}$
$\cos \theta = \frac{2}{2\sqrt{17}} = \frac{\sqrt{17}}{17}$	$\sec \theta = \frac{2\sqrt{17}}{2} = \sqrt{17}$
$\tan \theta = \frac{8}{2} = 4$	$\cot \theta = \frac{2}{8} = \frac{1}{4}$

Answer **exactly**, using a **simplified fractions**.

Label all the sides of the triangle **Opposite**, **Adjacent**, and **Hypotenuse**.

Use **Pythagorean theorem** to find the missing side.

TRIGONOMETRIC FUNCTIONS	RECIPROCAL FUNCTIONS	DEFINITIONS
SINE	$\sin \theta = \frac{\text{opp}}{\text{hyp}} = \frac{y}{r}$	<ul style="list-style-type: none"> A trigonometric function is a function whose ratio is defined by a trigonometric ratio. A trigonometric ratio compares the lengths of two sides of the triangle. The Greek letter θ (θ) is used to represent the measure of an acute angle in a right triangle.
COSINE	$\cos \theta = \frac{\text{adj}}{\text{hyp}} = \frac{x}{r}$	
TANGENT	$\tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{y}{x}$	
COTANGENT	$\cot \theta = \frac{\text{adj}}{\text{opp}} = \frac{x}{y}$	
SECANT	$\sec \theta = \frac{\text{hyp}}{\text{adj}} = \frac{r}{x}$	
COSECANT	$\csc \theta = \frac{\text{hyp}}{\text{opp}} = \frac{r}{y}$	

Remember SOH CAH TOA for life!

Thursday

Round your answer to
 the nearest hundredth.

The Unit Circle

A unit circle is a circle with a radius of 1 unit.
 Because the value of r is 1 for each point $P(x, y)$ on the circle, the sine, cosine, and tangent values for θ are defined as:

$\sin \theta = \frac{y}{1} = y$	$\cos \theta = \frac{x}{1} = x$	$\tan \theta = \frac{y}{x}$
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**** The coordinates of P can be written as $(\cos \theta, \sin \theta)$ ****

Special Angles

The following angles are used frequently with the unit circle:
 $0^\circ, 30^\circ, 45^\circ, 60^\circ, 90^\circ, 180^\circ, 270^\circ,$ and 360°

Because the terminal side of $0^\circ, 90^\circ, 180^\circ$ and 270° angles lie on an axis, they are called **quadrantal angles**.

Memorize these values!

It's important you understand how to build it.

Look for patterns. Make sense of how the values are determined.

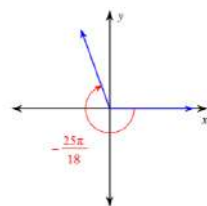
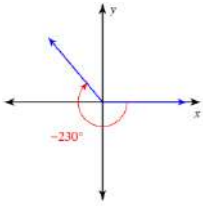
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Monday

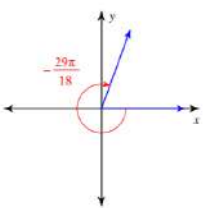
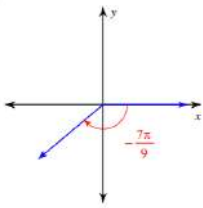
Tuesday

Find the reference angle for each.



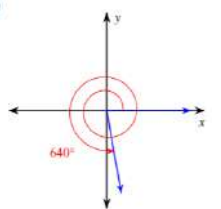
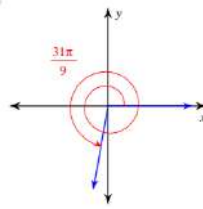
Convert the angle $\theta = \frac{8\pi}{9}$ radians to degrees.
 Express your answer exactly.

Find the reference angle for each.



Convert the angle $\theta = -\frac{19\pi}{5}$ radians to
 degrees.
 Express your answer exactly.

Find the reference angle for each.



Convert the angle $\theta = -310^\circ$ to radians.
 Express your answer exactly.

Find a coterminal angle between 0° and 360° .
Not multiple choice, find a cot. angle for each.

- a.) -330°
- b.) 640°
- c.) -435°

Convert the angle $\theta = \frac{17\pi}{18}$ radians to degrees.
 Express your answer exactly.

Find a coterminal angle between 0° and 360° .
Not multiple choice, find a cot. angle for each.

- a.) -442°
- b.) 285°
- c.) -545°

Convert the angle $\theta = \frac{257\pi}{360}$ radians to degrees.
 Express your answer exactly.

Find a coterminal angle between 0 and 2π .
Not multiple choice, find a cot. angle for each.

- a.) $\frac{11\pi}{3}$
- b.) $\frac{15\pi}{4}$
- c.) $-\frac{19\pi}{12}$
- d.) $-\frac{35\pi}{18}$

Convert the angle $\theta = -35^\circ$ to radians.
 Express your answer exactly.

Convert the angle $\theta = 100^\circ$ to radians.
 Express your answer exactly.

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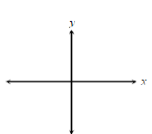
Complete all work on a separate sheet of paper. **Show all work.** Include the heading provided on each worksheet you turn in.

Wednesday

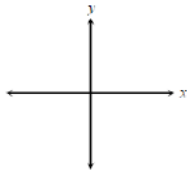
$P(5, -2)$ is a point on the terminal side of θ in standard form. Find the exact values of the trigonometric functions of θ :

	$\sin \theta =$	$\cos \theta =$	$\tan \theta =$
	$\csc \theta =$	$\sec \theta =$	$\cot \theta =$

$P(3, 2)$ is a point on the terminal side of θ in standard form. Find the exact values of the trigonometric functions of θ :

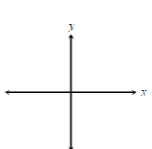
	$\sin \theta =$	$\cos \theta =$	$\tan \theta =$
	$\csc \theta =$	$\sec \theta =$	$\cot \theta =$

$P(-1, -1)$ is a point on the terminal side of θ in standard form. Find the exact values of the trigonometric functions of θ :

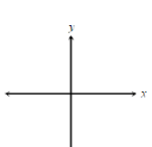


$\sin \theta =$	$\cos \theta =$	$\tan \theta =$
$\csc \theta =$	$\sec \theta =$	$\cot \theta =$

$P(-3, 6)$ is a point on the terminal side of θ in standard form. Find the exact values of the trigonometric functions of θ :

	$\sin \theta =$	$\cos \theta =$	$\tan \theta =$
	$\csc \theta =$	$\sec \theta =$	$\cot \theta =$

$P(-3, -2)$ is a point on the terminal side of θ in standard form. Find the exact values of the trigonometric functions of θ :

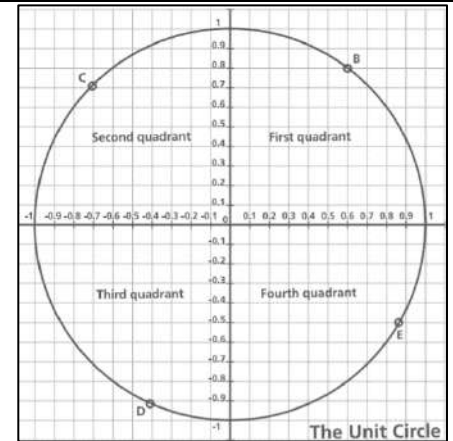
	$\sin \theta =$	$\cos \theta =$	$\tan \theta =$
	$\csc \theta =$	$\sec \theta =$	$\cot \theta =$

Thursday/Friday

The unit circle –

A circle whose center is at $(0,0)$ and whose radius is 1. Any point on the circumference of the circle can be described by an ordered pair (x,y) . The coordinates of

B are $(0.6, 0.8)$



1.) What are the coordinates of C, D, and E?

C = _____,

D = _____,

E = _____.

- In which quadrant are both x and y positive?
- In which quadrant is x negative and y positive?
- In which quadrant is x positive and y negative?
- In which quadrant is x negative and y negative?

Draw an angle of 30° in standard position on the unit circle (see above). Mark the initial ray and the terminal ray, Label it Q. Label the point where the terminal ray meets the circumference as θ .

1.) What are the coordinates of θ ?

Drop a perpendicular from Q to the x-axis to construct a right-angled triangle, centered at $(0, 0)$.

- What is the length of the hypotenuse?
- What is the length of the opposite?
- What is the length of the adjacent?

Using trigonometric ratios, (not a calculator), calculate the $\sin 30^\circ$, $\cos 30^\circ$ and the $\tan 30^\circ$.

5.) $\sin 30^\circ =$ _____

6.) $\cos 30^\circ =$ _____

7.) $\tan 30^\circ =$ _____

Compare these with the values of the x and y coordinates of Q.

8.) What do you notice about the x and y coordinates of Q and the trigonometric functions $\sin 30^\circ$, $\cos 30^\circ$ and $\tan 30^\circ$?

