

Name \_\_\_\_\_

1. Write the first 5 terms of the sequence whose  $n$ th term is  $a_n = \frac{n!}{(n+3)!}$ .

$$\frac{1!}{4!}, \frac{2!}{5!}, \frac{3!}{6!}, \frac{4!}{7!}, \frac{5!}{8!} = \frac{1}{1 \cdot 2 \cdot 3 \cdot 4}, \frac{1}{1 \cdot 2 \cdot 3 \cdot 4 \cdot 5}, \frac{1}{1 \cdot 2 \cdot 3 \cdot 4 \cdot 5 \cdot 6}, \frac{1}{1 \cdot 2 \cdot 3 \cdot 4 \cdot 5 \cdot 6 \cdot 7}, \frac{1}{1 \cdot 2 \cdot 3 \cdot 4 \cdot 5 \cdot 6 \cdot 7 \cdot 8}$$

2. Simplify:  $\frac{(n)!}{(n-2)!} = \frac{n \cdot (n-1) \cdot \cancel{(n-2) \dots}}{\cancel{(n-2) \dots}} = n(n-1) = n^2 - n$

3. Find a formula for the  $n$ th term of the sequence:  $\frac{1}{2}, \frac{1}{4}, \frac{1}{6}, \frac{1}{8}, \frac{1}{10}, \frac{1}{12}, \frac{1}{14}, \dots$

$$\frac{1}{2n(n-1)!}$$

4. Use sigma notation to write the sum:  $\frac{2}{14} + \frac{3}{8} + \frac{4}{6} + \frac{5}{8} + \frac{6}{14} + \dots$

$$\sum_{n=1}^{n=1} \frac{2n}{n+2}$$

5. Which of the following is an arithmetic sequence?

- (a) 2, 4, 8, 16, 32, ...
- (b) -2, 4, -8, 16, 32, ...
- (c) 3, 6, 9, 12, 15, ...
- (d) all of these

6. Find the first 4 terms of the arithmetic sequence with  $a_1 = 7$  and  $d = 2$ .

$$7, 9, 11, 13$$

7. Find  $a_n$  for the arithmetic sequence with  $a_1 = 12$ ,  $d = \frac{1}{3}$ , and  $n = 52$ .

$$29$$

8. Find the sum of the first 50 positive integers that are multiples of 3.

$$3+6+9+\dots = \frac{1}{2}(a_1 + a_n) \quad a_1 = 3, \quad a_{50} = 150 \quad 25(3 + 150) = 3825$$

9. Find the sum of the first 30 terms of the sequence:  $\sqrt{2}, 2\sqrt{2}, 3\sqrt{2}, 4\sqrt{2}, 5\sqrt{2}, \dots$

$$a_n = n\sqrt{2} \quad 15(\sqrt{2} + 30\sqrt{2}) = 15(31\sqrt{2}) = 465\sqrt{2}$$

10. Find the sum of the first  $n$  terms of the arithmetic sequence: -7, 1, 9, 17, ...

$$4n^2 - 11n$$

11. Find the sum of the first 14 terms of the arithmetic sequence whose  $n$ th term is  $a_n = 2n + 3$ .

$$7(5 + 31) = 252$$

12. Find a formula for  $a_n$  for the arithmetic sequence with  $a_3 = 8$  and  $d = -3$ .

$$a_1 = 14$$

$$a_n = -3n + 17$$

13. Find the sum:  $\sum_{n=1}^{200} (2n + 3)$        $100(5 + 403) = 40,800$

14. Find the sum:  $\sum_{i=1}^9 3(i - 2)$        $\frac{9}{2}(-3 + 21) = 81$

15. Determine the seating capacity of an auditorium with 30 rows of seats if there are 25 seats in the first row, 28 seats in the second row, 31 seats in the third row, and so on.

$$3n + 22 \quad 15(25 + 112) = 2055$$

16. Which of the following is a geometric sequence?

(a)  $-1, -3, -5, -7, -9, \dots$

(b)  $2, 3, 5, 7, 11, \dots$

(c)  $1, 2, 4, 7, 11, 16, \dots$

(d)  $-2, 4, -8, 16, -32, \dots$

17. Determine the common ratio for the geometric sequence:  $4, -2, 1, -\frac{1}{2}, \frac{1}{4}, \dots$        $-\frac{1}{2}$

18. Write the first five terms of the geometric sequence with  $a_1 = 5$  and  $r = \frac{1}{2}$ .

$$5 \quad \frac{5}{2} \quad \frac{5}{4} \quad \frac{5}{8} \quad \frac{5}{16}$$

19. Find the 10<sup>th</sup> term of the geometric sequence with  $a_1 = 3$  and  $r = 2.2$

$$3(2.2)^{10-1} = 3621.807653$$

20. Find the 28<sup>th</sup> term of the geometric sequence:  $2, 2.4, 2.88, 3.456, 4.1472, \dots$

$$r = 1.2 \quad 2(1.2)^{27} = 274.7411039$$

21. Find the sum and round your answer to four decimal places:  $\sum_{n=0}^{10} 2\left(\frac{1}{3}\right)^n$

$$2 \frac{1 - \frac{1}{3}^{11}}{1 - \frac{1}{3}} = 2 \frac{177146}{177147} \cdot \frac{3}{2} = \frac{531438}{177147} = 2.999982 \approx 3.0000$$

22. Find the sum and round your answer to two decimal places:  $\sum_{n=1}^{13} 3\left(\frac{3}{2}\right)^n$

$$a_1 = 3 \cdot \frac{3}{2} = \frac{9}{2} \quad \frac{9 \cdot 1 - \frac{3}{2}^{13}}{2 \cdot 1 - \frac{3}{2}} = 1742.575562 \approx 1742.58$$

23. Find the sum of the first six terms of the geometric sequence with  $a_1 = 3$  and  $a_2 = \frac{3}{2}$ .

$$3 \left( \frac{1 - \frac{1}{64}}{1 - \frac{1}{2}} \right) = 3 \left( \frac{\frac{63}{64}}{\frac{1}{2}} \right) = 3 \cdot \frac{63}{64} \cdot 2 = \frac{189}{32}$$

24. Evaluate:  $\sum_{n=0}^{\infty} 4\left(\frac{1}{4}\right)^n = 4 + 1 + \frac{1}{4} + \frac{1}{16} + \dots = \frac{4}{1 - \frac{1}{4}} = \frac{4}{\frac{3}{4}} = \frac{16}{3}$

25. Evaluate:  $\sum_{n=0}^{\infty} 5\left(\frac{1}{3}\right)^n = \frac{5}{1 - \frac{1}{3}} = \frac{5}{\frac{2}{3}} = \frac{15}{2}$

26. In a geometric sequence,  $a_4 = 125$  and  $a_{10} = \frac{125}{64}$ . Find  $a_{14}$ .

27. Find a rational number representation of the repeating decimal  $1.\overline{32}$

$$\begin{aligned} \overline{1.32} &= 1 + .32 + .0032\dots \\ &= 1 + \frac{.32}{1 - .01} \\ &= 1 + \frac{.32}{.99} \\ &= \frac{99}{99} + \frac{32}{99} = \frac{131}{99} \end{aligned}$$

$$\begin{aligned} a_{10} &= a_4 \cdot r^6 \\ \frac{125}{64} &= 125 \cdot r^6 \\ r^6 &= \frac{1}{64} \\ r &= \frac{1}{2} \\ a_{14} &= a_{10} \cdot r^4 \\ a_{14} &= \frac{125}{64} \cdot \frac{1}{2^4} \\ \frac{125}{64} \cdot \frac{1}{16} &= \frac{125}{1024} \end{aligned}$$