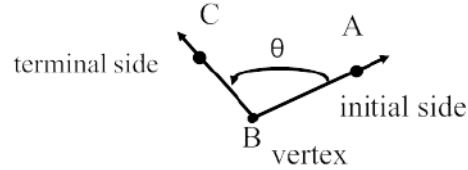


Chapter 13: Periodic Functions and Trig

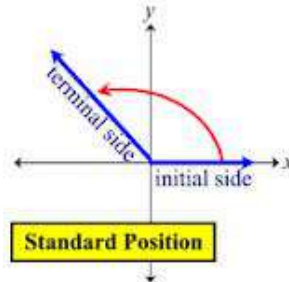
Converting Between Radian and Degree Measures

Angle: formed by two rays with a common endpoint
 $\theta = \text{theta}$



Standard Position of an Angle: an angle is in **standard position** if

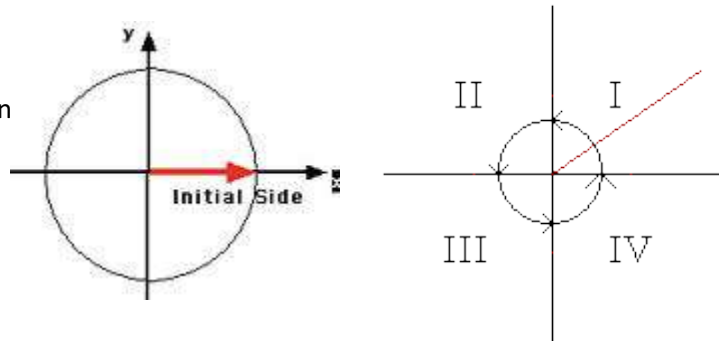
- its vertex is at the origin of a rectangular coordinate system
- its initial side lies along the positive x-axis



Measuring Angles in Degrees:

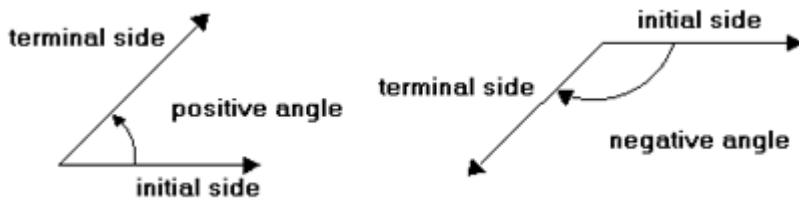
Note: An angle is always measured in standard position

- $0^\circ - 360^\circ$ is one rotation or less
- more than 360° is more than one rotation



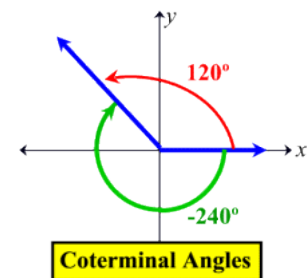
Positive Angles vs. Negative Angles:

a positive angle: generated by a counterclockwise rotation.
 a negative angle: generated by a clockwise rotation.



Coterminal Angles:

two angles with the same initial and terminal sides.



Sketch each angle in standard position

- 1) 45° angle 2) 225° angle 3) -135° angle 4) 370° angle

Determine the quadrant in which the terminal side of the angle lies

- 1) 210° 2) -120° 3) 30° 4) 390°

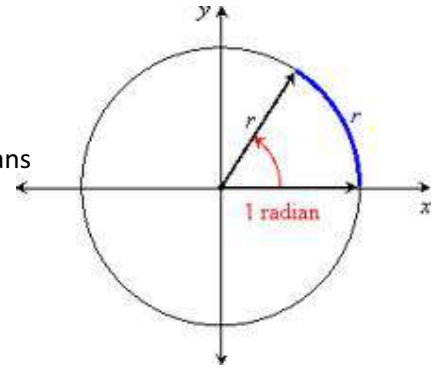
Determine the coterminal angle for the given angle.

1. 60° 2. -150° 3. 200° 4. 270° 5. -80°

Measuring in Radians: An angle made by taking the **radius** and **wrapping it along the edge** of a circle.

Note: $360^\circ =$ one time around
 one time around = circumference ($C = 2\pi r$)

If radius is 1 unit then $\rightarrow 360^\circ = 2\pi(1)$ or $360^\circ = 2\pi$ so $180^\circ = \pi$ radians



- To convert degrees to radians, multiply degrees by $\frac{\pi \text{ radians}}{180^\circ}$
- To convert radians to degrees, multiply radians by $\frac{180^\circ}{\pi \text{ radians}}$

Find the exact radian measure that corresponds to the degree measure. Give all answers in terms of π .

- 1) 30° 2) 90° 3) -135° 4) 260°

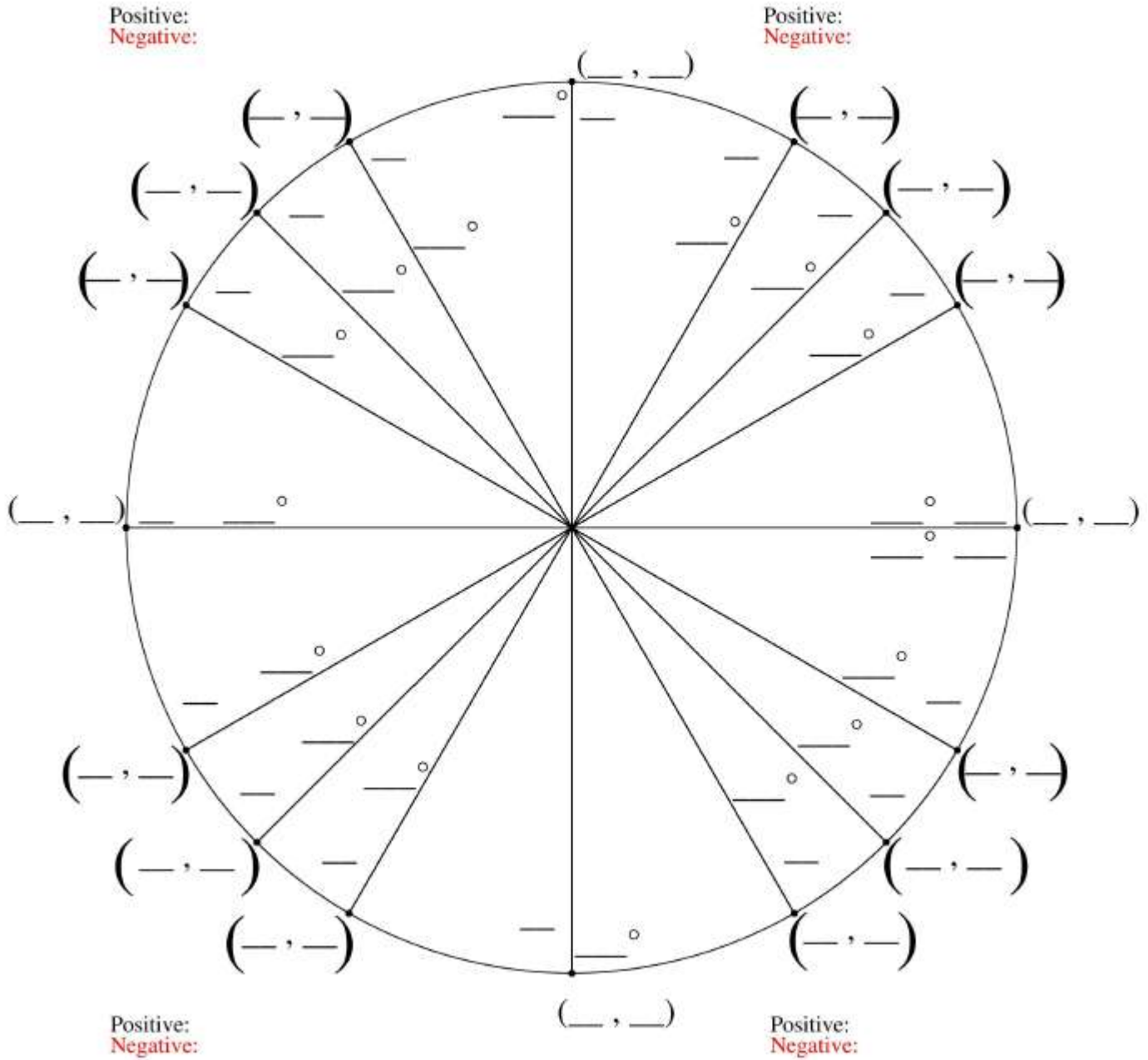
Find the exact degree measure that corresponds to the radian measure. If necessary, round to the nearest tenth of a degree.

- 1) $\frac{\pi}{3}$ 2) $-\frac{5\pi}{3}$ 3) 6π radians 4) 1.2π radians

Determine the quadrant in which the terminal side of the angle lies, then sketch the angle in standard form.

- 1) $\frac{\pi}{4}$ 2) $-\frac{2\pi}{3}$ 3) $-\frac{\pi}{6}$ 4) 5 radians

The Unit Circle



Using the Unit Circle

Use the unit circle to find the exact value of each trigonometric function.

1. $\cos 210^\circ$
2. $\sin(-\pi)$
3. $\sin 150^\circ$
4. $\cos 150^\circ$

5. $\cos \frac{-2\pi}{3}$

6. $\cos \frac{2\pi}{3}$

7. $\sin \frac{11\pi}{6}$

8. $\cos \frac{4\pi}{3}$

Periodic functions

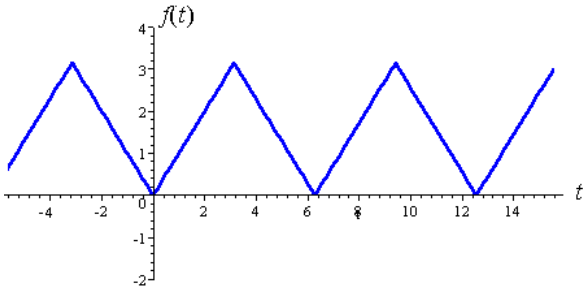
A periodic function repeats a pattern of y-values at regular intervals called cycles.

The period of a function is the **horizontal** length on one cycle.

The amplitude is half the difference between the maximum and minimum values of the function.

Find the period and amplitude of each function.

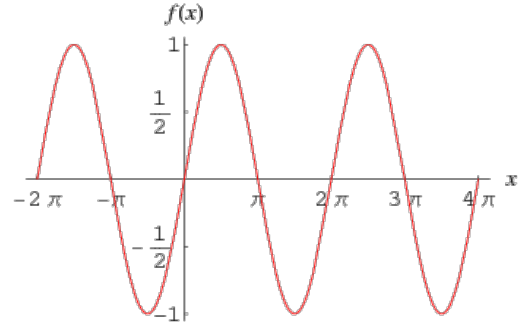
1.



Period: _____

Amplitude: _____

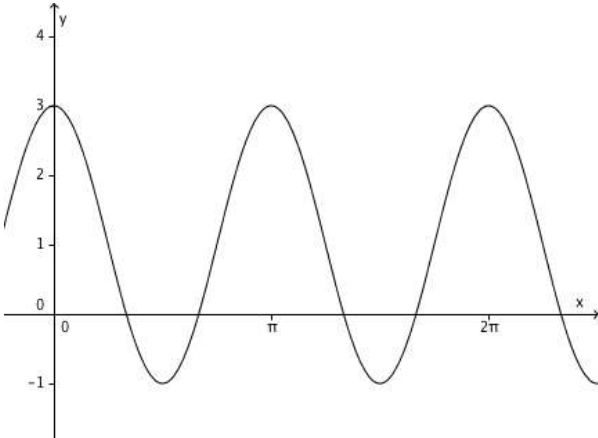
2.



Period: _____

Amplitude: _____

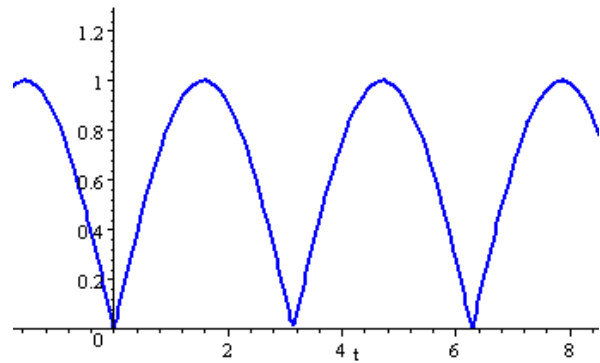
3.



Period: _____

Amplitude: _____

4.



Period: _____

Amplitude: _____