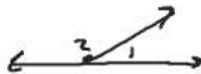


Spiral Review



1. Find a counter example to show that the statement is not true. If angles are supplementary then they form a linear pair.



2. Find the coordinates of the point  $\frac{7}{10}$  of the way from A to B.

$$\text{Distance } x\text{-values} \\ 9 - (-4) = 13$$

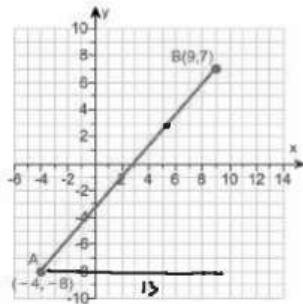
$$(13)\left(\frac{7}{10}\right) = \frac{91}{10} = 9.1$$

$$\text{Distance } y\text{-values} \\ 7 - (-8) = 15$$

$$15\left(\frac{7}{10}\right) = 10.5$$

$$-4 + 9.1 = 5.1 \\ -8 + 10.5 = 2.5$$

$$(5.1, 2.5)$$



3. Consider the statement: If James has 2 dimes, then he has at least 20 cents.

- a. Is this a true statement? Justify your reasoning.

True

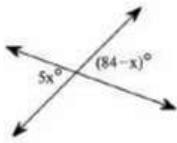
- b. Write the converse of the given statement. Is the converse a true statement?

Explain.

If James has at least 20 cents, then he has at least 2 dimes.

False       $\begin{matrix} 20 \text{ pennies} \\ 5 \text{ Nickels} \end{matrix}$

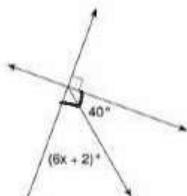
4. Find the value of the variable.



$$5x = 84 - x$$

$$6x = 84$$

$$x = 14$$

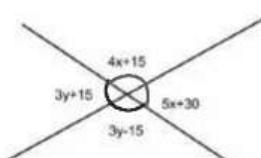


$$6x + 2 + 40 = 90$$

$$6x + 42 = 90$$

$$6x = 48$$

$$x = 8$$



$$3y + 15 + 3y - 15 = 180$$

$$6y = 180$$

$$y = 30$$

$$4x + 15 + 5x + 30 = 180$$

$$9x + 45 = 180$$

$$9x = 135$$

$$x = 15$$

## Properties of Parallel Lines

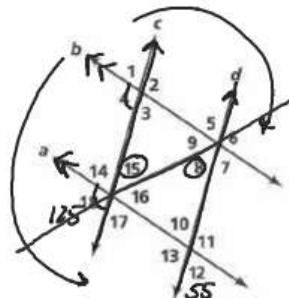
### Section: Properties of Parallel Lines

Use the figure to answer each question in this section.

5. If  $c \parallel d$ ,  $a \parallel b$ , and  $m\angle 12 = 55^\circ$ , then  $m\angle 4 = \underline{125^\circ}$

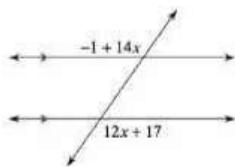
6. If  $\angle 15 \cong \angle 8$  then which two lines are parallel? Explain your answer.

$c \parallel d$  Converse of Alternate  
Int C's.



7. Find the value of  $x$ .

$$-1 + 14x = 12x + 17$$



$$180 - 55$$

$$-1 + 2x = 17$$

$$2x = 18$$

$$x = 9$$

8. Use the figure to the right. Lines  $a$ ,  $b$ ,  $c$ , and  $d$  intersect as shown.

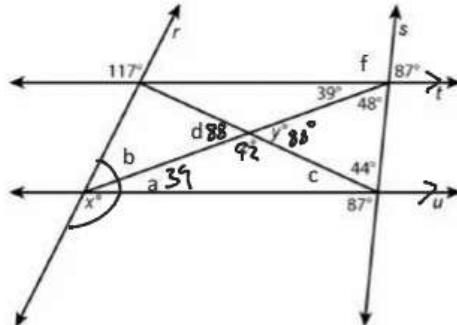
a. Which pairs of lines are parallel?

$t \parallel u$

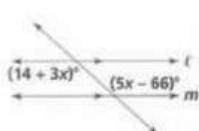
b. Find the values of the variables.

$$a = \underline{39^\circ} \quad b = \underline{24} \quad c = \underline{49} \quad d = \underline{88}$$

$$f = \underline{93} \quad x = \underline{117} \quad y = \underline{88} \quad z = \underline{92}$$



9. Find the value of the variable that will make the lines parallel.

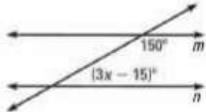


$$14 + 3x = 5x - 66$$

$$14 = 2x - 66$$

$$80 = 2x$$

$$x = 40$$

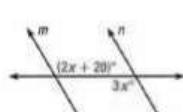


$$3x - 15 + 150 = 180$$

$$3x + 135 = 180$$

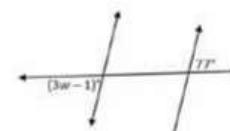
$$3x = 45$$

$$x = 15$$



$$2x + 20 = 3x$$

$$x = 20$$



$$3w - 1 = 77$$

$$3w = 78$$

$$w = 26$$

### Section: Parallel Lines and the Triangle Sum – Theorem

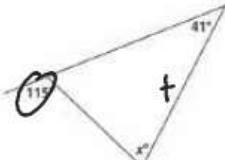
10. Find the value of the variable.

$$\begin{array}{c} 92^\circ \quad x^\circ \\ \text{---} \\ 63^\circ \end{array}$$

$$x + 92 + 63 = 180$$

$$x + 155 = 180$$

$$x = 25$$



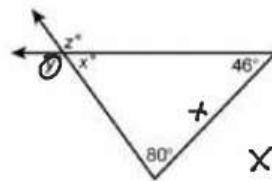
$$x + 41 = 115$$

$$x = 74$$

11. Given the figure, find the value of the variables.

$$\begin{array}{l} y = 46 + 80 \\ y = 126 \end{array}$$

$$z = 126$$



$$\begin{array}{l} x + 46 + 80 = 180 \\ x + 126 = 180 \\ x = 54 \end{array}$$

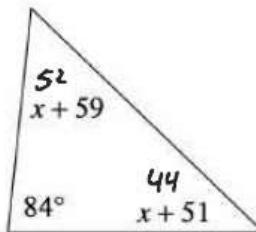
12. Find the value of x.

$$x + 59 + 84 + x + 51 = 180$$

$$2x + 194 = 180$$

$$2x = -14$$

$$x = -7$$



### Section: Slopes of Parallel and Perpendicular Lines.

13. Are the lines parallel, perpendicular, or neither?

Perpendicular

$$\nearrow m$$

$$\left(\frac{2}{3}\right)\left(-\frac{3}{2}\right) = -\frac{4}{6} = -1$$

$$y = \frac{2}{3}x + 5$$

$$3x + 2y = 8 \rightarrow y = mx + b$$

$$\frac{3}{2}y = -\frac{3}{2}x + \frac{8}{2} \quad y = -\frac{3}{2}x + 4$$

14. Write an equation (slope-intercept form) for the line that is parallel to  $y = -4x + 5$  that contains the point  $(1, -6)$ .

$$m = -4$$

$$m = -4$$

$$y - y_1 = m(x - x_1)$$

$$y - (-6) = -4(x - 1)$$

$$y + 6 = -4x + 4$$

$$y = -4x - 2$$

$$y - y_1 = m(x - x_1)$$

$\uparrow^m$

15. Write an equation (slope-intercept form) for the line that is perpendicular to  $y = 3x - 2$  and passes through the point  $(9, -2)$

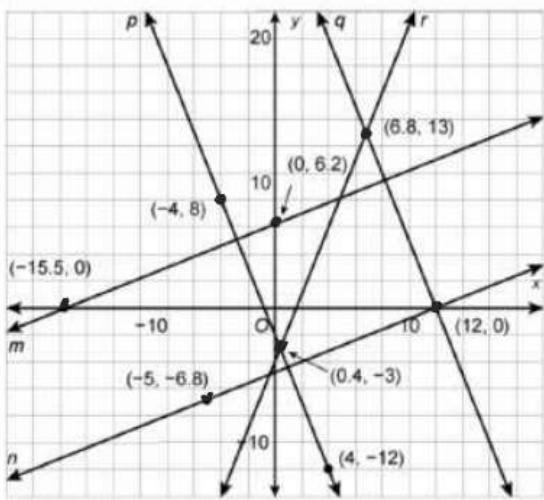
$$m = -\frac{1}{3}$$

$$y - (-2) = -\frac{1}{3}(x - 9)$$

$$y + 2 = -\frac{1}{3}x + 3$$

$$y = -\frac{1}{3}x + 1$$

16. Given the following figure, find which lines will be parallel and perpendicular. Verify using slopes.



$$\text{Slope} = \frac{y_2 - y_1}{x_2 - x_1}$$

$m \parallel n$        $p \parallel q$

$$m = \frac{6.2 - 0}{0 - (-15.5)} = \frac{2}{5}$$

$m \perp p$        $n \perp p$

$m \perp q$        $n \perp q$

$$n = \frac{0 - (-6.8)}{12 - (-5)} = \frac{6.8}{17} = \frac{2}{5}$$

$$p = \frac{-4 - 8}{0 - (-4)} = -2.5 = -\frac{5}{2}$$

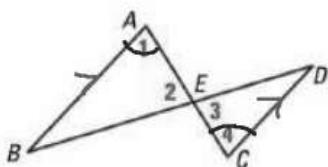
$$q = \frac{0 - 13}{12 - 6.8} = -2.5 = -\frac{5}{2}$$

$$r = \frac{13 - (-3)}{6.8 - 0} = 2.5 = \frac{5}{2}$$

### Section: Proofs

**GIVEN** ▶  $\angle 1 \cong \angle 2, \angle 3 \cong \angle 4$

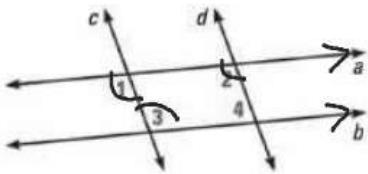
**PROVE** ▶  $\overline{AB} \parallel \overline{CD}$



Statement	Reason
1. $\angle 1 \cong \angle 2, \angle 3 \cong \angle 4$	1. Given
2. $\angle 2 \cong \angle 3$	2. Vertical L's
3. $\angle 1 \cong \angle 4$	3. Substitution prop
4. $\overline{AB} \parallel \overline{CD}$	4. Converse Alt Int L's

**GIVEN** ▶  $a \parallel b$ ,  $\angle 2 \cong \angle 3$

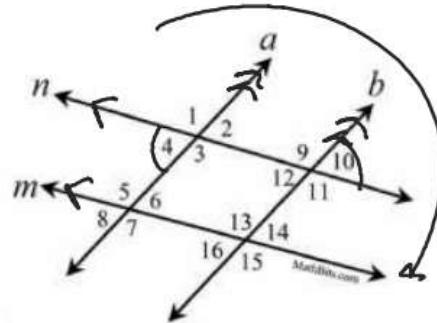
**PROVE** ▶  $c \parallel d$



Statement	Reason
1. $a \parallel b$ $\angle 2 \cong \angle 3$	1. Given
2. $\angle 1 \cong \angle 3$	2. Alt Fnt L's $\cong$
3. $\angle 1 \cong \angle 2$	3. Substitution Property
4. $c \parallel d$	4. Converse Corresponding L's

Given:  $m \parallel n$  and  $a \parallel b$

Prove  $\angle 4$  is supplementary  $\angle 15$



Statement	Reason
1. $m \parallel n$ and $a \parallel b$	1. Given
2. $\angle 4 \cong \angle 10$	2. Alt Ext L's
3. $\angle 10$ and $\angle 15$ are supplementary	3. Same-Side Ext L's
4. $m\angle 10 + m\angle 15 = 180^\circ$	4. Definition of Supplementary Angles
5. $m\angle 4 = m\angle 10$	5. Def $\cong$ L's
6. $m\angle 4 + m\angle 15 = 180^\circ$	6. Substitution Property
7. $\angle 4 + \angle 15$ are supp	7. Def of Supp L's