

STUDENT NAME: _____

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SUBJECT: ALGEBRA 1

PERIOD: _____

Explain 1 Multiplying Binomials Using the Distributive Property

To multiply a binomial by a binomial, the Distributive Property must be applied more than once.

Example 1 Multiply by using the Distributive Property.

A $(x + 5)(x + 2)$

$$\begin{aligned}(x + 5)(x + 2) &= x(x + 2) + 5(x + 2) && \text{Distribute.} \\ &= x(x + 2) + 5(x + 2) && \text{Redistribute and simplify.} \\ &= x(x) + x(2) + 5(x) + 5(2) \\ &= x^2 + 2x + 5x + 10 \\ &= x^2 + 7x + 10\end{aligned}$$

B $(2x + 4)(x + 3)$

$$\begin{aligned}(2x + 4)(x + 3) &= 2x(x + 3) + \square(x + 3) && \text{Distribute.} \\ &= 2x(x + 3) + \square(x + 3) && \text{Redistribute and simplify.} \\ &= 2x(x) + \square(3) + \square(x) + \square(3) \\ &= \square x^2 + \square x + \square x + \square \\ &= \square x^2 + \square x + \square\end{aligned}$$

Multiply.

1. $(x + 5)(x + 6)$

2. $(a - 7)(a - 3)$

3. $(d + 8)(d - 4)$

4. $(2x - 3)(x + 4)$

5. $(5b + 1)(b - 2)$

6. $(3p - 2)(2p + 3)$

7. $(5k - 9)(2k - 4)$

8. $(2m - 5)(3m + 8)$

9. $(4 + 7g)(5 - 8g)$

10. $(r + 2s)(r - 6s)$

11. $(3 - 2v)(2 - 5v)$

12. $(5 + h)(5 - h)$

Explain 3 Multiplying Polynomials

To multiply polynomials with more than two terms, the Distributive Property must be used several times.

Example 3 Multiply the polynomials.

A $(x + 2)(x^2 - 5x + 4)$

$$(x + 2)(x^2 - 5x + 4) = x(x^2 - 5x + 4) + 2(x^2 - 5x + 4) \quad \text{Distribute.}$$

$$= x(x^2 - 5x + 4) + 2(x^2 - 5x + 4) \quad \text{Redistribute.}$$

$$= x(x^2) + x(-5x) + x(4) + 2(x^2) + 2(-5x) + 2(4) \quad \text{Simplify.}$$

$$= x^3 - 5x^2 + 4x + 2x^2 - 10x + 8$$

$$= x^3 - 3x^2 - 6x + 8$$

B $(3x - 4)(-2x^2 + 5x - 6)$

$$(3x - 4)(-2x^2 + 5x - 6) = 3x(-2x^2 + 5x - 6) - \square(-2x^2 + 5x - 6) \quad \text{Distribute.}$$

$$= 3x(-2x^2 + 5x - 6) - \square(-2x^2 + 5x - 6) \quad \text{Redistribute.}$$

$$= 3x(-2x^2) + 3x(\square) + 3x(\square) - 4(\square) - 4(\square) - 4(\square)$$

Simplify.

$$= \square x^{\square} + \square x^{\square} - \square x + \square x^{\square} - \square x + \square$$

$$= \square x^{\square} + \square x^{\square} - \square x + \square$$

Multiply the polynomials.

13. $(x - 3)(x^2 + 2x + 1)$

14. $(x + 5)(x^3 + 6x^2 + 18x)$

15. $(x + 4)(x^4 + x^2 + 1)$

16. $(x - 6)(x^5 + 4x^3 + 6x^2 + 2x)$

17. $(x^2 + x + 3)(x^3 - x^2 + 4)$

18. $(x^3 + x^2 + 2x)(x^4 - x^3 + x^2)$

FACTORING BY GROUPING.

1)

STEP 1: Separate the polynomial in groups of 2. Use parenthesis to separate them.

STEP 2: Take out the common factor in each group.

STEP 3: Write the the binomial that's common to both groups in front, then write the remaining terms as another binomial.

STEP 4: Check your work by multiplying the binomials back. See if you get the original problem back.

$$\begin{aligned} \text{EXAMPLE 1: } 2x^3 - 6x^2 + 5x - 15 &= (2x^3 - 6x^2) + (5x - 15) \quad \text{STEP 1} \\ &= 2x^2(x - 3) + 5(x - 3) \quad \text{STEP 2} \end{aligned}$$

$$= (x - 3)(2x^2 + 5) \quad \text{STEP 3}$$

THIS IS YOUR ANSWER.

$$\begin{aligned} \text{Check your work: } (x - 3)(2x^2 + 5) &= x(2x^2 + 5) - 3(2x^2 + 5) \\ &= 2x^3 + 5x - 6x^2 - 15 \quad \text{this can also be written in standard form} \\ &\quad \text{(exponents in descending order) as} \\ &= 2x^3 - 6x^2 + 5x - 15 \quad \text{IT'S THE SAME!!} \end{aligned}$$

2) EXAMPLE 2:

$$3x^3 + 15x^2 - 2x - 10 = (3x^3 + 15x^2) - (2x + 10) \quad \text{** Notice that the sign for 10 has changed.}$$

That's because you placed the negative sign outside the parenthesis. Watch out for this each time you separate terms of a polynomial by grouping.

$$= 3x^2(x + 5) - 2(x + 5) \quad \text{STEP 2}$$

$$= (x + 5)(3x^2 - 2) \quad \text{STEP 3}$$

Now check by multiplying the binomials and see if you get the original problem back:

$$(x + 5)(3x^2 - 2) = \underline{\hspace{15em}}$$

Factor each completely. Show all steps and box your final answer. Remember to check by multiplying the binomials back.

3) $15x^3 + 40x^2 + 9x + 24$

4) $3x^3 + 24x^2 - x - 8$

5) $16x^3 + 4x^2 - 12x - 3$

6) $2x^3 - 6x^2 + x - 3$

7) $6x^3 + 15x^2 - 2x - 5$

8) $18x^3 + 21x^2 - 6x - 7$

9) $18x^3 + 6x^2 + 3x + 1$

10) $49x^3 - 28x^2 + 35x - 20$

11) $7x^3 + 56x^2 + 6x + 48$

12) $49x^3 + 28x^2 + 35x + 20$