Algebra II Common Core State Standards

In Algebra I, students added, subtracted, and multiplied polynomials. In Algebra II, students divide polynomials with remainder, leading to the factor and remainder theorems. This is the underpinning for much of advanced algebra, including the algebra of rational expressions.

Themes from middle school algebra continue and deepen during high school. As early as grade 6, students began thinking about solving equations as a process of reasoning (6.EE.5). This perspective continues throughout Algebra I and Algebra II (A-REI). "Reasoned solving" plays a role in Algebra II because the equations students encounter can have extraneous solutions (A-REI.2).

In Algebra II, they extend the real numbers to complex numbers, and one effect is that they now have a complete theory of quadratic equations: Every quadratic equation with complex coefficients has (counting multiplicities) two roots in the complex numbers.

In grade 8, students learned the Pythagorean theorem and used it to determine distances in a coordinate system (8.G.6–8). In Geometry, students proved theorems using coordinates (G-GPE.4–7). In Algebra II, students will build on their understanding of distance in coordinate systems and draw on their growing command of algebra to connect equations and graphs of conic sections (e.g., G-GPE.1).

In Geometry, students began trigonometry through a study of right triangles. In Algebra II, they extend the three basic functions to the entire unit circle.

As students acquire mathematical tools from their study of algebra and functions, they apply these tools in statistical contexts (e.g., S-ID.6). In a modeling context, they might informally fit an exponential function to a set of data, graphing the data and the model function on the same coordinate axes.

Mathematical Practices

- While all of the mathematical practice standards are important in all three courses, four are especially important in the Algebra II course:
- Construct viable arguments and critique the reasoning of others (MP.3). As in geometry, there are central questions in advanced algebra that cannot be answered definitively by checking evidence. There are important results about *all* functions of a certain type the factor theorem for polynomial functions, for example and these require general arguments (A-APR.2). Deciding whether two functions are equal on an infinite set cannot be settled by looking at tables or graphs; it requires arguments of a different sort (F-IF.8).
- Attend to precision (MP.6). As in the previous two courses, the habit of using precise language is not only a tool for effective communication but also a means for coming to understanding. For example, when investigating loan payments, if students can articulate something like, "What you owe at the end of a month is what you owed at the start of the month, plus 1/12 of the yearly interest on that amount, minus the monthly payment," they are well along a path that will let them construct a recursively defined function for calculating loan payments (A-SSE.4).
- Look for and make use of structure (MP.7). The structure theme in Algebra I centered on seeing and using the structure of algebraic expressions. This continues in Algebra II, where students delve deeper into transforming expressions in ways that reveal meaning. The example given in the standards that x4 y4 can be seen as the difference of squares is typical of this practice. This habit of seeing sub-expressions as single entities will serve students well in areas such as trigonometry, where, for example, the factorization of x4 y4 described above can be used to show that the functions $\cos 4x \sin 4x$ and $\cos 2x \sin 2x$ are, in fact, equal (A-SSE.2).

In addition, the standards call for attention to the structural similarities between polynomials and integers (A-APR.1). The study of these similarities can be deepened in Algebra II: Like integers, polynomials have a division algorithm, and division of polynomials can be used to understand the factor theorem, transform rational expressions, help solve equations, and factor polynomials.

• Look for and express regularity in repeated reasoning (MP.8). Algebra II is where students can do a more complete analysis of sequences (F-IF.3), especially arithmetic and geometric sequences, and their associated series. Developing recursive formulas for sequences is facilitated by the practice of abstracting regularity for how you get from one term to the next and then giving a precise description of this process in algebraic symbols (F-BF.2). Technology can be a useful tool here: Most Computer Algebra Systems allow one to model recursive function definitions in notation that is close to standard mathematical notation. And spreadsheets make natural the process of taking successive differences and running totals (MP.5).

The same thinking — finding and articulating the rhythm in calculations — can help students analyze mortgage payments, and the ability to get a closed form for a geometric series lets them make a complete analysis of this topic. This practice is also a tool for using difference tables to find simple functions that agree with a set of data.

Algebra II is a course in which students can learn some technical methods for performing algebraic calculations and transformations, but sensemaking is still paramount (MP.1). For example, analyzing Heron's formula from geometry lets one connect the zeros of the expression to the degenerate triangles. As in Algebra I, the modeling practice is ubiquitous in Algebra II, enhanced by the inclusion of exponential and logarithmic functions as modeling tools (MP.4). Computer algebra systems provide students with a tool for modeling all kinds of phenomena, experimenting with algebraic objects (e.g., sequences of polynomials), and reducing the computational overhead needed to investigate many classical and useful areas of algebra (MP.5).

Note: The standards addressed here are based on the CCSS document and the PARCC Mathematics Model Frameworks document that the state has indicated will be used as a guideline for EOC assessments. Instructional notes are taken from the Appendix A in the CCSS document.

★ = specific modeling standards appear throughout the high school standards indicated by a star symbol.

		The Real Num		
Clusters with Instructional Notes				
	N.RN.1	Explain how the define		
Extend the properties of exponents to		properties of integer		
rational exponents		rational exponents. F		
rational exponents.		$5^{(1/3)3}$ to hold, so $(5^{-1})^{-1}$		
	N.RN.2	Rewrite expressions		
	1	Quant		
Reason quantitatively and use units to		Define ennemiete a		
solve problems.	IN.Q .2	Denne appropriate q		
Foundation for work with expressions,				
equations and functions				
		The Complex Nu		
	N.CN.1	Know there is a con		
Perform arithmetic operations with		bi with a and b real.		
complex numbers.	N.CN.2	Use the relation $i^2 =$		
Folynomials with real coefficients		subtract, and multip		
Use complex numbers in polynomial	N.CN.7	Solve quadratic equ		
identities and equations.	1.001.07	sorre quadrane equ		
		Cooing Structure is		
	1	Seeing Structure I		
Internet the structure of evenessions	A SSE 2	Use the structure of s		
Polynomial and rational	A.55E.2	$(v^2)^2$ thus recognizin		
r olynomiai and rational		()) , intas recognizin		
	A.SSE.3	Choose and produce		
		quantity represented		
Write expressions in equivalent forms		c. Use the properti		
to solve problems		example the exp		
Quadratic and exponential		approximate eq		
	A.SSE.4	Derive the formula		
		use the formula to s		
	Arithmetic with Polynomials			
	A.APR.2	2 Know and apply the		
Understand the relationship between		on division by $x - a$		
zeros and factors of polynomials	A.APR.3	3 Identify zeros of po		
		construct a rough gr		
	A.APR.4	Prove polynomial ic		
		polynomial identity		
Use polynomial identities to solve	A.APR.5	(+) Know and apply		
problems		positive integer n , w		
		Pascal s Triangle.		
		Rewrite simple ratio		
Rewrite rational expressions		where $a(x) = b(x) = a(x)$		
Rewrite rational expressions		using inspection long		
		Creating Equ		
Create equations that describe				
numbers or relationships.	A.CED.	Create equations and		
Equations using all available types of		equations arising fro		
functions		functions.		

ber System (N.RN)

Standards

inition of the meaning of rational exponents follows from extending the exponents to those values, allowing for a notation for radicals in terms of *For example, we define* $5^{1/3}$ *to be the cube root of* 5 *because we want* $(5^{1/3})^3 = \frac{1}{3}^3$ must equal 5.

involving radicals and rational exponents using the properties of exponents. ities (N.Q)

uantities for the purpose of descriptive modeling.

mber System (N.CN)

nplex number *i* such that $i^2 = -1$, and every complex number has the form a + 1

= -1 and the commutative, associative, and distributive properties to add, bly complex numbers.

ations with real coefficients that have complex solutions.

n Expressions (A.SSE)

an expression to identify ways to rewrite it. For example, see $x^4 - y^4 as (x^2)^2 - ag$ it as a difference of squares that can be factored as $(x^2 + y^2) (x^2 - y^2)$

an equivalent form of an expression to reveal and explain properties of the by the expression.*

ties of exponents to transform expressions for exponential functions. For pression 1.15^{t} can be rewritten as $(1.15^{1/12})^{12t} \approx 1.012^{12t}$ to reveal the uvivalent monthly interest rate if the annual rate is 15%.

for the sum of a finite geometric series (when the common ratio is not 1), and solve problems. For example, calculate mortgage payments. \star

and Rational Expressions (A.APR)

e Remainder Theorem: For a polynomial p(x) and a number a, the remainder is p(a), so p(a) = 0 if and only if (x - a) is a factor of p(x).

alynomials when suitable factorizations are available, and use the zeros to raph of the function defined by the polynomial.

dentities and use them to describe numerical relationships. For example, the $y(x^2 + y^2)^2 = (x^2 - y^2)^2 + (2xy)^2$ be used to generate Pythagorean triples. y the Binomial Theorem for the expansion of $(x + y)^n$ in powers of x and y for a where x and y are any numbers, with coefficients determined for example by

nal expressions in different forms; write a(x)/b(x) in the form q(x) + r(x)/b(x),), and r(x) are polynomials with the degree of r(x) less than the degree of b(x), ag division, or, for the more complicated examples, a computer algebra system. **nations* (A.CED)**

inequalities in one variable and use them to solve problems. *Include m linear and quadratic functions, and simple rational and exponential*

	Reasoning with Equations and Inequalities (A.REI)		
Clusters with Instructional Notes	Standards		Linear, Quadratic, and
Understand solving equations as a	A.REI.1. Explain each step in solving a simple equation as following from the equality of numbers asserted at	Construct and compare linear,	F.LE.2. Construct linear and
process of reasoning and explain the	the previous step, starting from the assumption that the original equation has a solution. Construct a	quadratic, and exponential models	graph, a description
reasoning.	viable argument to justify a solution method.	and solve problems.	F.LE.4 For exponential mod
Simple radical and rational as well as	A.REI.2 Solve simple rational and radical equations in one variable, and give examples showing how	Logarithms as solutions for exponentials	and the base b is 2,
Master linear; learn as general principle	extraneous solutions may arise.	Interpret expressions for functions in	
	A.REI.3. Solve linear equations and inequalities in one variable, including equations with coefficients	terms of the situation they model	FIF5 Interpret the parame
Solve equations and inequalities in	represented by letters.	Linear and exponential of form	1.LL.S. Interpret the parameter
one variable.	A.REI.4. Solve quadratic equations in one variable.	$f(x)=b^x+k$	
Linear inequalities; literal that are	b. Solve quadratic equations by inspection (e.g., for $x^2 = 49$), taking square roots, completing the		Trigonometr
linear in the variables being solved for;	square, the quadratic formula and factoring, as appropriate to the initial form of the equation.		F.TF.1 Understand radian n
quadratics with real solutions.	Recognize when the quadratic formula gives complex solutions and write them as $a \pm bi$ for real	Extend the domain of trigonometric	angle.
	numbers a and b.	functions using the unit circle	F.IF.2 Explain how the uni
	A.REI.6. Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of		to all real numbers,
Solve systems of equations.	linear equations in two variables.	Madel noniedie nhenemene mith	ETE 5 Choose trigonometr
Linear-linear and linear-quadratic	A.KEI. / Solve a simple system consisting of a linear equation and a quadratic equation in two variables	widel periodic phenomena with	r. 1r. 5 Choose urgonomeu
	and the circle $x^2 + x^2 = 3$	trigonometric functions	E TE 8 Prove the Dythegore
	A REL 11 Explain why the x-coordinates of the points where the graphs of the equations $y = f(x)$ and $y = g(x)$	Prove and apply trigonometric identities	F.1F.8 Prove the Pythagore $\sin(\theta)$ and $\sin(\theta)$
Represent and solve equations and	intersect are the solutions of the equation $f(x) = g(x)$; find the solutions approximately, e.g. using	luentities	Expressing Coometric Pro
inequalities graphically.	technology to graph the functions, make tables of values, or find successive approximations.	Translate between the geometric	
Combine polynomial, rational, radical,	Include cases where $f(x)$ and/or $g(x)$ are linear, polynomial, rational, absolute value, exponential.	description and the equation of a	G GPE 2 Derive the equation
absolute value, and exponential functions	and logarithmic functions.*	conic section	G.GI E.2 Derive the equation
	Interpreting Functions (F.IF)		Interpreting Categorica
Understand the concept of a function		Summarize, represent, and interpret	S.ID.4 Use the mean and st
and use function notation.	F.IF.3. Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of	data on a single count or	population percenta
Learn as general principle; focus on	the integers. For example, the Fibonacci sequence is defined recursively by $f(0) = f(1) = 1$, $f(n+1) =$	measurement variable.	appropriate. Use cal
linear and exponential and on	$f(n) + f(n-1)$ for $n \ge 1$.		Making Inferences an
arithmetic and geometric sequences			S.IC1 Understand statistic
	F.IF.4. For a function that models a relationship between two quantities, interpret key features of graphs and	Understand and evaluate random	random sample from
Intermed for diana that arise in	tables in terms of the quantities, and sketch graphs showing key features given a verbal description	processes underlying statistical	S.IC.2 Decide if a specified
applications in terms of the context	of the relationship. Key features include: intercepts; intervals where the function is increasing,	experiments	using simulation. Fe
Emphasize selection of appropriate	decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and		Would a result of 5
models	periodicity.*		S.IC.3 Recognize the purpo
	F.IF.6. Calculate and interpret the average rate of change of a function (presented symbolically or as a	Make inferences and justify conclusions	studies; explain how
	table) over a specified interval. Estimate the rate of change from a graph.		S.IC.4 Use data from a sam
	F.IF.7. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases		error through the us
	and using technology for more complicated cases.*		S.IC.5 Use data from a fair
	c. Oraph polynomial functions, identifying zeros when suitable factorizations are available, and showing and behavior		S IC 6 Evaluate reports has
	e Graph exponential and logarithmic functions showing intercents and end behavior and		Conditional Probability and
Analyze functions using different	trigonometric functions, showing period, midline, and amplitude.		S CP 1 Describe events as s
representations.	F.IF.8. Write a function defined by an expression in different but equivalent forms to reveal and explain		categories) of the ou
Focus on using key features to guide	different properties of the function. ^t		"and," "not").
selection of appropriate type of model	b. Use the properties of exponents to interpret expressions for exponential functions. For example,		S.CP.2 Understand that two
	identify percent rate of change in functions such as $y = (1.02)^{t}$, $y = (0.97)^{t}$, $y = (1.01)^{12t}$, $y = (1.01)^{12t}$		is the product of the
	$(1.2)^{t/10}$, and classify them as representing exponential growth or decay.		independent.
	F.IF.9. Compare properties of two functions each represented in a different way (algebraically, graphically,	Understand independence and	S.CP.3 Understand the condit
	numerically in tables, or by verbal descriptions). For example, given a graph of one quadratic	dependence and use them to interpret	of A and B as saying
	function and an algebraic expression for another, say which has the larger maximum.	data	A, and the condition
	Building Functions (F.BF)	Link to data from simulations or	S.CP.4 Construct and interpre
Clusters with Instructional Notes	Standards	experiments	and to approximate
Build a function that models a	P.BF.1 white a function that describes a relationship between two quantities.		students in your sch
	a. Determine an explicit expression, a recursive process, or steps for calculation from a context.		probability that a ray
	b. Combine standard function types using anumetic operations. For example, build a function that models the temperature of a cooling body by adding a constant function to a decaying exponential		student is in tenth or
Include all types of functions studied	and relate these functions to the model		S.CP.5 Recognize and expla
	F BE.2 Write arithmetic and geometric sequences both recursively and with an explicit formula, use them to		language and every
	model situations, and translate between the two forms.*		a smoker with the cl
			S.CP.6 Find the conditional
Build new functions from existing	F.BF.3 Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$, $k f(x)$, $f(kx)$, and $f(x + k)$ for specific	Use the rules of probability to	and interpret the ans
functions	values of k (both positive and negative); find the value of k given the graphs. Experiment with cases	events in a uniform probability model	S.CP.7 Apply the Addition
Include simple radical, rational, and	and injustrate an explanation of the effects on the graph using technology. Include recognizing even	events in a unifor in probability model	of the model.
exponential functions; emphasize	and our functions from their graphs and algebraic expressions for them. F BE A Find inverse functions		
common effect of each transformation	a. Solve an equation of the form $f(x) = c$ for a simple function f that has an inverse and write an		
across function types	expression for the inverse For example $f(x) = 2x^3$ or $f(x) = (x+1)/(x-1)$ for $x \neq 1$		
	$(x_1 - x_2) = (x_1 - x_2) = $		

Exponential Models* (F.LE)

exponential functions, including arithmetic and geometric sequences, given a of a relationship, or two input-output pairs (include reading these from a table). dels, express as a logarithm the solution to $ab^{ct} = d$ where *a*, *c*, and *d* are numbers 10, or *e*; evaluate the logarithm using technology.

ters in a linear or exponential function in terms of a context.

ic Functions (F.TF)

heasure of an angle as the length of the arc on the unit circle subtended by the

t circle in the coordinate plane enables the extension of trigonometric functions interpreted as radian measures of angles traversed counterclockwise around the

ic functions to model periodic phenomena with specified amplitude, frequency,

an identity $\sin^2(\theta) + \cos^2(\theta) = 1$ and use it to find $\sin(\theta)$, $\cos(\theta)$, or $\tan(\theta)$ given (θ) and the quadrant of the angle.

perties with Equations (G.GPE)

of a parabola given a focus and directrix.

l and Quantitative Data (S.ID)

andard deviation of a data set to fit it to a normal distribution and to estimate ges. Recognize that there are data sets for which such a procedure is not culators, spreadsheets, and tables to estimate areas under the normal curve.

d Justify Conclusions (S.IC)

s as a process for making inferences about population parameters based on a n that population.

I model is consistent with results from a given data-generating process, e.g., or example, a model says a spinning coin falls heads up with probability 0.5. tails in a row cause you to question the model?

oses of and differences among sample surveys, experiments, and observational randomization relates to each.

ple survey to estimate a population mean or proportion; develop a margin of e of simulation models for random sampling.

domized experiment to compare two treatments; use simulations to decide if parameters are significant.

ed on data.

nd the Rules of Probability (S.CP

ubsets of a sample space (the set of outcomes) using characteristics (or atcomes, or as unions, intersections, or complements of other events ("or,"

events A and B are independent if the probability of A and B occurring together ir probabilities, and use this characterization to determine if they are

ional probability of A given B as P(A and B)/P(B), and interpret independence g that the conditional probability of A given B is the same as the probability of al probability of B given A is the same as the probability of B.

t two-way frequency tables of data when two categories are associated with each ed. Use the two-way table as a sample space to decide if events are independent conditional probabilities. For example, collect data from a random sample of ool on their favorite subject among math, science, and English. Estimate the adomly selected student from your school will favor science given that the rade. Do the same for other subjects and compare the results.

ain the concepts of conditional probability and independence in everyday lay situations. For example, compare the chance of having lung cancer if you are nance of being a smoker if you have lung cancer.

probability of A given B as the fraction of B's outcomes that also belong to A, wer in terms of the model.

Rule, P(A or B) = P(A) + P(B) - P(A and B), and interpret the answer in terms

