

Algebra 2 Applied

Unit 2 Review

What to expect on the test

Quick Review

A **relation** is a set of ordered pairs. The **domain** of a relation is the set of x -coordinates. The **range** is the set of y -coordinates. When each element of the domain is paired with exactly one element of the range, the relation is a **function**.

Example

Determine whether the relation is a function. Find the domain and range.

$$\{(5, 0), (8, 1), (1, 3), (5, 2), (3, 8)\}$$

In this relation, the x -coordinate 5 is paired with both 0 and 2. This relation is not a function.

The domain is the set of x -coordinates, which is $\{5, 8, 1, 3\}$.

The range is the set of y -coordinates, which is $\{0, 1, 3, 2, 8\}$.

Quick Review

A linear equation of the form $y = kx$, $k \neq 0$, represents **direct variation**. The **constant of variation** is k . You can use proportions to solve direct variation problems.

Example

In the table, determine whether y varies directly with x . If so, what is the constant of variation and the function rule?

$\frac{6}{2} = \frac{9}{3} = \frac{24}{8} = 3$, so y varies directly with x , and the constant of variation is 3.

The function rule is $y = 3x$.

x	y
2	6
3	9
8	24

Quick Review

The graph of a **linear function** is a line. You can represent a linear function with a **linear equation**. Given two points on a line, the **slope** of the line is the ratio of the change in the y -coordinates to the change in the corresponding x -coordinates. The slope is the coefficient of x when you write a linear equation in **slope-intercept form**.

Example

What is the slope of the line that passes through (3, 5) and (-1, -2)?

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

Find the difference between the coordinates.

$$= \frac{5 - (-2)}{3 - (-1)} = \frac{7}{4}$$

Simplify.

Quick Review

You write the equation of a line in **point-slope form** when you have a point and the slope or when you have two points. The **standard form** of an equation has both variables and no constants on the left side.

When two lines have the same slope, they are **parallel**.

When two lines have slopes that are negative reciprocals of each other, they are **perpendicular**.

Example

Write an equation in standard form for the line with a slope of 2, going through (1, 6).

$$y - 6 = 2(x - 1)$$

Write the equation in point-slope form, substituting the given point and slope.

$$y = 2x - 2 + 6$$

Simplify.

$$-2x + y = 4$$

Write in standard form.

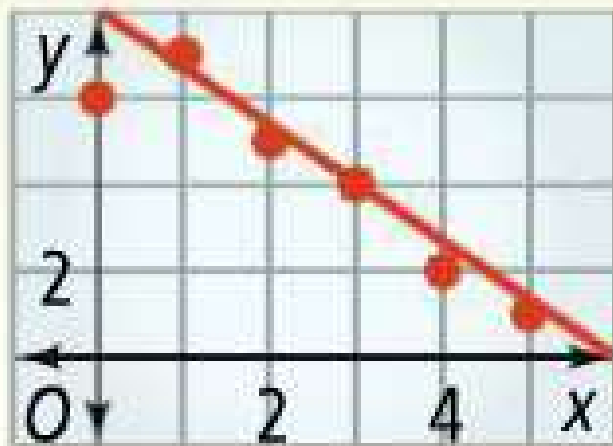
Quick Review

You can use a **scatter plot** to show relationships between data sets. You can make predictions using a trend line, which approximates the relationship between two data sets. The most accurate trend line is a **line of best fit**.

Example

Draw a scatter plot of the data. Is a linear model reasonable? If so, predict the value of y when $x = 9$.

$$\{(0, 6), (1, 7), (2, 5), (3, 4), (4, 2), (5, 1)\}$$



The points are close to the line $y = -\frac{4}{3}x + 8$, so a linear model is reasonable. When $x = 9$,

$$\begin{aligned} y &= -\frac{4}{3}(9) + 8 \\ &= -4 \end{aligned}$$

Quick Review

A **parent function** is the simplest form of a function in a family of functions. Each member is a **transformation** of the parent function.

Translations shift the graph horizontally, vertically, or both. A **reflection** flips the graph over a line of symmetry.

Vertical stretches and **compressions** change the shape of the graph by a factor.

Example

Write the equation of the transformation of the graph of $f(x) = x^2$ translated 3 units up, vertically stretched by a factor of 6, and reflected across the y -axis.

$$y = x^2 + 3 \quad \text{Translated 3 units up.}$$

$$y = 6(x^2 + 3) \quad \text{Vertically stretched.}$$

$$y = 6(-x)^2 + 18 \quad \text{Reflected across the } y\text{-axis.}$$

$$y = 6x^2 + 18$$

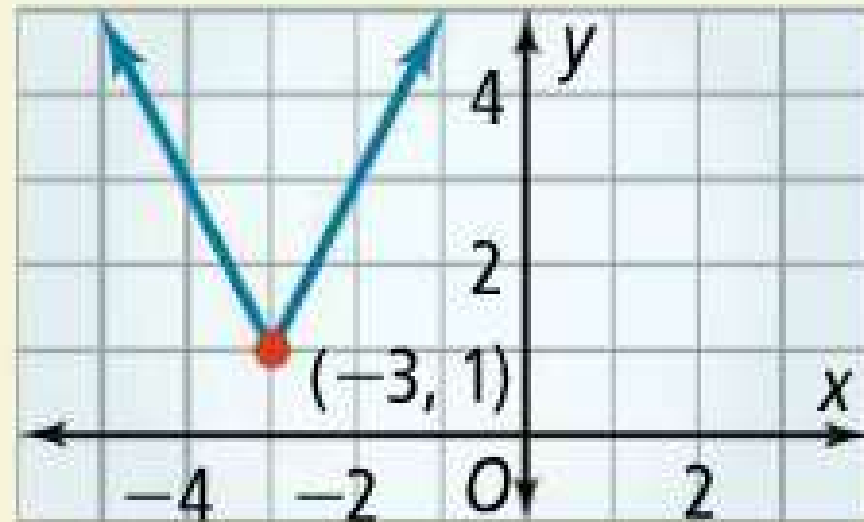
Quick Review

The **absolute value function** $y = |x|$ is the **parent function** for the family of functions of the form $y = a|x - h| + k$. The maximum or minimum point of the graph is the vertex of the graph.

$$y = 2|x + 3| + 1$$

$$a = 2, h = -3, k = 1$$

- Vertex is at $(-3, 1)$
- Translated left 3 units
- Stretched by a factor of 2
- Translated up 1 unit



Example

Write an equation for the translation of the graph $y = |x|$ up 5 units.

Because the graph is translated up, k is positive, so the equation of the translated graph is $y = |x| + 5$.

Quick Review

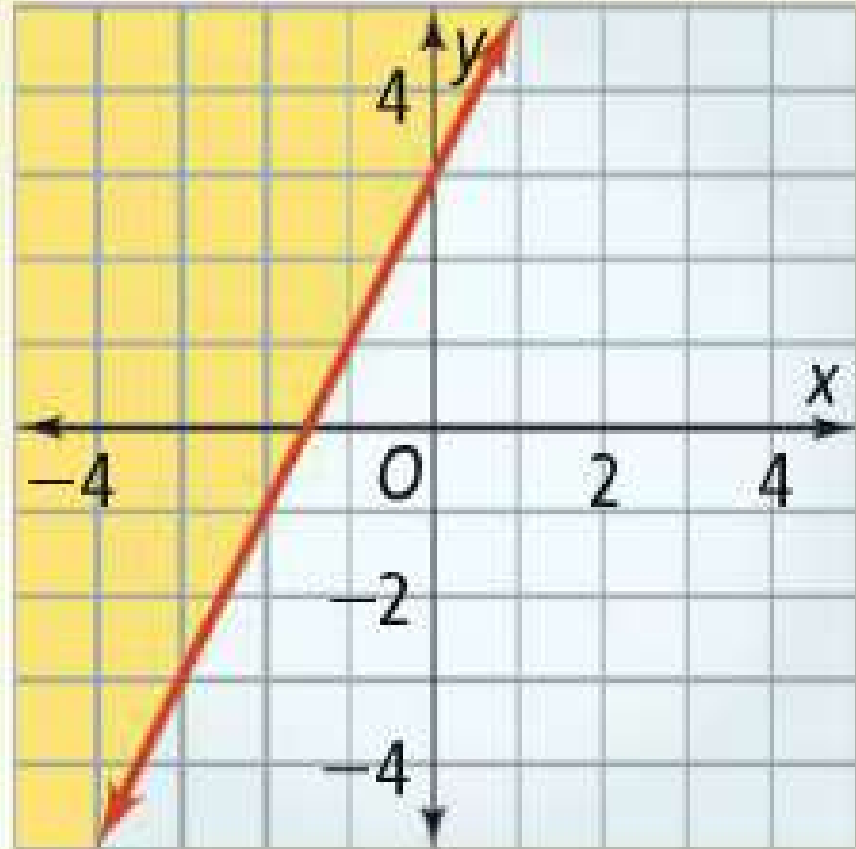
An inequality describes a region of the coordinate plane that has a **boundary**. To graph an inequality involving two variables, first graph the boundary. Then determine which side of the boundary contains the solutions. Points on a dashed boundary are not solutions. Points on a solid boundary are solutions.

Example

Graph the inequality
 $y \geq 2x + 3$.

Graph the solid boundary
line $y = 2x + 3$.

Since y is *greater than*
 $2x + 3$, shade above
the boundary.



Review Practice Pearson Algebra 2 pages 123 to 126

#3-5 pick 1 #7 or 8

#9-11 pick 1 #12-15 pick 1

#16-19 pick 1 #20 or 21 #22-25 pick 1

#26-29 pick 1 #30

#31-33 pick 1

#34-36 pick 1 #37-39 pick 1

#40-43 pick 1 #44-47 pick 1 #48 or 49

#50-53 pick 1 #54 & 55