

**Practice with Examples**

For use with pages 356–363

**GOAL** Use properties of trapezoids and kites**VOCABULARY**

A **trapezoid** is a quadrilateral with exactly one pair of parallel sides. The parallel sides of a trapezoid are the **bases** of the trapezoid.

For each of the bases of a trapezoid, there is a pair of **base angles**, which are the two angles that have that base as a side.

The nonparallel sides of a trapezoid are the **legs** of the trapezoid.

If the legs of a trapezoid are congruent, then the trapezoid is an **isosceles trapezoid**.

The **midsegment** of a trapezoid is the segment that connects the midpoints of its legs.

A **kite** is a quadrilateral that has two pairs of consecutive congruent sides, but opposite sides are not congruent.

**Theorem 6.14** If a trapezoid is isosceles, then each pair of base angles is congruent.

**Theorem 6.15** If a trapezoid has a pair of congruent base angles, then it is an isosceles trapezoid.

**Theorem 6.16** A trapezoid is isosceles if and only if its diagonals are congruent.

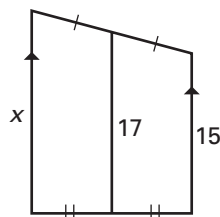
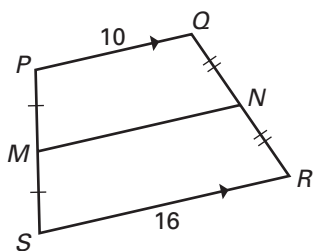
**Theorem 6.17** The midsegment of a trapezoid is parallel to each base and its length is one half the sum of the lengths of its bases.

**Theorem 6.18** If a quadrilateral is a kite, then its diagonals are perpendicular.

**Theorem 6.19** If a quadrilateral is a kite, then exactly one pair of opposite angles is congruent.

**EXAMPLE 1** Finding Midsegment Lengths of Trapezoids and Using Algebra

- a. Find the length of the midsegment  $MN$ .      b. Find the value of  $x$ .



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### SOLUTION

- a. Use the Midsegment Theorem for Trapezoids.

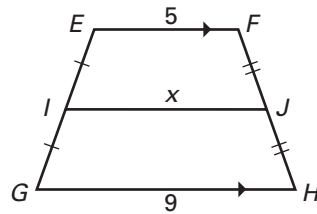
$$MN = \frac{1}{2}(PQ + SR) = \frac{1}{2}(10 + 16) = \frac{1}{2}(26) = 13$$

- b.  $17 = \frac{1}{2}(15 + x)$       Midsegment Theorem for Trapezoids  
 $34 = 15 + x$               Multiply each side by 2.  
 $19 = x$                       Subtract.

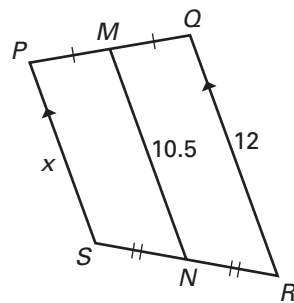
### Exercises for Example 1

Find the value of  $x$ .

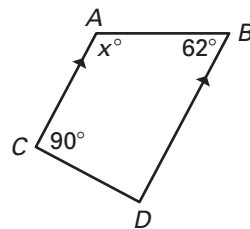
1.



2.



3.

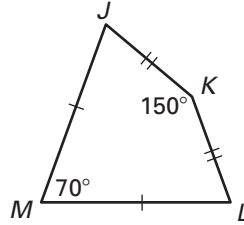


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### EXAMPLE 2 Using Properties of Kites

$JKLM$  is a kite. What is  $m\angle J$ ?



#### SOLUTION

$JKLM$  is a kite, so  $\angle J \cong \angle L$  and  $m\angle J = m\angle L$ .

$$2(m\angle J) + 150^\circ + 70^\circ = 360^\circ$$

Sum of measures of int.  $\angle$  of a quad. is  $360^\circ$ .

$$2(m\angle J) = 140^\circ$$

Simplify.

$$m\angle J = 70^\circ$$

Divide each side by 2.

#### Exercises for Example 2

Find the value of  $x$ .

