



Getting to the Core

Grade 4 Unit of Study

Division

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Unit Title:	Division			
Grade Level:	4 th Grade	Time Frame: 3 weeks		
Big Idea (Enduring Understandings):	Quantities can be divided into equal groups.			
Essential Questions:	 How is an array related to an area model? How is repeated subtraction related to equal groups in division? What are the patterns that occur? How can you prove the properties of multiplication and the rules of division? What is another way to solve a division problem using a different algorithm? How is the remainder expressed? Where have you used division to solve a problem in your life? 			
21 st Century Skills:	Learning and Innovation: Critical Thinking & Problem Solving Communication & Collaboration Information, Media and Technology: Online Tools Software			
Essential Academic Language:	Tier II:ArrayModelMultipleSharingExplainEqual groupRemainderImage: Constrain of the second seco	Tier III:Inverse operationDividendPartitioningPropertiesDivisorRegroupSquare numberQuotientDivisibilityPrime numberFactorComposite numberComposite numberMultiplier		
 What pre-assessment will be given? Check What You Know quiz, p. 119 (Chapter 6) Unit 6 prerequisite skills test 		How will pre-assessment guide instruction? Pre-assessment will determine whether students have the pre- requisite computation skills, academic vocabulary, and level of understanding of new content/standard. If students miss more than two in one skills area provide strategic intervention in a small group.		

Preparing the Learner Lesson A Launching Mathematical Discourse Preparing the Learner Lesson B Collaborative Work on Sequencing and Making Equal Shares Preparing the Learner Lesson C Multiplication Clusters and Mental M Preparing the Learner Lessons draw from the Progress to Algebra Continuum for 3 rd Grade: Understand the properties of multiplication and the relationship between multiplication and division. Arrays: Lessons 1 & 2 Grouping: Lessons 3 & 4 Fair Shares: Lessons 6 & 7 Remainders: Lessons 8 & 9		
Preparing the Learner Lessons draw from the Progress to Algebra Continuum for 3 rd Grade: Understand the properties of multiplication and the relationship between multiplication and division. Arrays: Lessons 1 & 2 Grouping: Lessons 3 & 4 Fair Shares: Lessons 6 & 7 Remainders: Lessons 8 & 9	Preparing the Learner Lesson C Multiplication Clusters and Mental Math	
Arrays: Lessons 1 & 2 Grouping: Lessons 3 & 4 Fair Shares: Lessons 6 & 7 Remainders: Lessons 8 & 9		
Multiplication and division are different ways to look at the same problem situation.Multiplication and division are different ways to look at the same problem situation.Division is used to solve problems in daily life.How the remainder is explained depends upon the problem situation.• Model multiplication and division problems using arrays.• Repeated subtraction• Quotative- known number in each group• Remainder may be expressed as a fraction or a decimal.• Use arrays to model properties of multiplication in cooperative group.• Making groups 	Optional Menu Activities: Lesson 10	
Prime and Composite Numbers: Lessons 11 & 12Multiplication Properties and Divisibility: Lessons 13 & 14Dividing Larger Numbers: Optional Lessons 16 – 18Rules of divisibility are based on number patterns. • Use arrays to prove numbers are either prime or composite. • Factor table array • Factor trees • Mystery number games ("I'm thinking of"; "I have, who has?")Multiplication Properties and Divisibility: Lessons 13 & 14Optional Lessons 16 – 18 Division is used to solve problems in daily life. • Multiples of 10s, 100s, 1000sUnit Assessments Summative Multiple Choice and Property • Commutative Property • Identity Property • Divisibility Rules • Making ConjecturesOptional Lessons 16 – 18 Division is used to solve problems in daily life. • Multiples of 10s, 100s, 1000sUnit Assessments Summative Multiple Choice and Performance-Based Task		

Standards	Assessment of Standards (include formative and summative)		
Common Core Learning Standards Taught and Assessed	What assessment(s) will be utilized for this unit? (F = formative, S = summative)	What does the assessment tell us?	
 Common Core Mathematics Content Standard(s): 4th Grade Operations and Algebraic Thinking Gain familiarity with factors and multiples. 4. Find all factor pairs for a whole number in the range 1–100. Recognize that a whole number is a multiple of each of its factors. Determine whether a given whole number in the range 1–100 is a multiple of a given one-digit number. Determine whether a given whole number in the range 1–100 is prime or composite. 4th Grade Number and Operations in Base Ten Use place value understanding and properties of operations to perform 	 F: Problem solving journal F: Visual representation of thinking F: Work collaboratively to write the sequence of events in a story, adding a creative ending illustrating how the number of cookies provided and the number of children present affects the number of cookies each child can eat. F: Performance Task, Explaining 13 / 4 = 3 R1 F: Performance Task, How are multiplication and division alike? 	Ongoing evidence of students' understanding of the concepts presented Diagnostic information for intervention or acceleration	
6. Find whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.	S: End of Unit Test S: Performance Task, Writing a Division Story for an Expression	Student comprehension of unit concepts and the big idea: "Quantities can be divided into equal groups."	
 Bundled Language Standard(s): 3. Use knowledge of language and its conventions when writing, speaking, reading, or listening. c. Differentiate between contexts that call for formal English (e.g., presenting ideas) and situations where informal discourse is appropriate (e.g., small-group discussion). 6. Acquire and use accurately grade-appropriate general academic and domain-specific words and phrases. 	 F: Teacher evaluation of student use of appropriate mathematical academic language during partner, small group, and class collaborative conversations. F: Use of appropriate academic vocabulary in daily math journals and creation of story problems. S: Use of accurate mathematical terms and appropriate sequential language in culminating written word problem and its solution. 	Do students use the appropriate academic language when speaking in class discussions and presentations and when writing in their daily math journals?	
 Bundled Speaking and Listening Standard(s): 1. Engage effectively in a range of collaborative discussions (one-on-one, in groups, and teacher-led) with diverse partners on grade 4 topics and texts, building on others' ideas and expressing their own clearly. a. Come to discussions prepared having read or studied required material; explicitly draw on that preparation and other information known about the topic to explore ideas under discussions. b. Follow agreed-upon rules for discussions and carry out assigned roles. 	Teacher evaluation of student speaking and listening:F: Ask and answer questions in pairs and small groups during and after lessons.F: Work collaboratively to create a tree map of a model for collaborative discussions.F: Participation in presentations of solutions for	When talking about mathematics in pairs and groups, do students follow protocol/rules/ routines for collaborative discussions?	

 c. Pose and respond to specific questions to clarify or follow up on information, and make comments that contribute to the discussion and link to the remarks of others. d. Review the key ideas expressed and explain their own ideas and understanding in light of the discussion. 4. Report on a topic or text, tell a story, or recount an experience in an organized manner, using appropriate facts and relevant, descriptive details to support main ideas or themes; speak clearly at an understandable pace. 		Mystery Numbers. S. Design and write a problem situation to match a given expression, solve the problem, and write a step-by-step explanation of the process used.		Can students plan and deliver an informative presentation with appropriately detailed sequencing? Do all students participate in the thinking, conversation, and final product? Do they follow rules and guidelines for collaboration?
Standards of Mathematical Practice:	 (Check all that apply) 1. Make sense of problems and persevere in solving them. 2. Reason abstractly and quantitatively. 3. Construct viable arguments and critique the reasoning of others. 4. Model with mathematics. 5. Use appropriate tools strategically. 6. Attend to precision. 7. Look for and make use of structure. 8. Look for and express regularity in repeated reasoning. 		 Opportunities for Observable Data (How will students demonstrate these Mathematical Practices?) 1. Students will deconstruct the problem. They will make a plan for solving the problem. They will continue with or without support until they reach a solution. 4. Students will solve problems based on a real life situation. 8. Students will notice that repeated subtraction is the same as making equal groups. 	
Resources & Materials: Interdisciplinary Connections:	Mathematical Tools: 1" square tiles, graph paper, index cards, multi-link cubes, base ten blocks, counters, math journals Media/Technology to be used to deepen learning: ST Math Whole Number Multiplication and Division Module; Factorization and Prime Numbers; PowerPoint presentations; NCTM Illuminations Website <http: illuminations.nctm.org=""> (Multiplication/Division games: Prime Time, Factor Dazzle, Times Square) Supplementary Materials (lessons from the following resources will be provided): TERC, Packages and Groups; TERC, Arrays and Shares; Burns, M., Math By All Means, Division; Burns, M., 50 Problem-Solving Lessons; Montgomery, M., Mystery Numbers; Equals, Get It Together; TERC, Math Appeal; Pincezes, E., One Hundred Hungry Ant; Pinczes, E., A Remainder of One; Hutchins, P., The Doorbell Rang Cite several interdisciplinary or cross-content connections made in this unit of study (i.e. literature, science, social studies, art, etc.) ELA Theme: money- Student generated word problems using division with money.</http:>			
	Science unit: Rocks and Minerals- making arrays for a rock collection.			

Differentiated	Based on desired student outcomes, what instructional	Based on desired student outcomes, what instructional
Instruction:	variation will be used to address the needs of English	variation will be used to address the needs of students
	 Learners by language proficiency level? Use of sentence frames (appropriate for language level) to facilitate academic language and conversations. Use of visual organizers to assist processing mathematical ideas Explicitly teach key academic vocabulary. Use of manipulatives to facilitate conceptual understanding Flexible grouping to support language acquisition and target instruction Use of collaboration to promote socio-cultural learning Opportunities for verbal rehearsal of concepts 	 with special needs, including gifted and talented? Special Needs- Use of visual organizers in organizing and evaluating evidence. Explicitly teach key academic vocabulary. Monitor student responses for corrective teaching Use of games ST Math Opportunities for verbal rehearsal of concepts GATE- Use of pre-assessment results to accelerate/compact curriculum and instruction for students who demonstrate mastery (85% +)

Prerequisite Skills Test

	Name	
Show the expressions using addition:		
1. 2 X 4	2. 3 X 5	
Solve:		-
3. How can 7 X 4 be solved using addition?		
4. What division does 12 − 3 − 3 − 3 − 3 = 0 sho	w?	
5. Mary wants to show 20 ÷ 5 using subtraction	n. How can she show this?	
6. What is the product of 7 X 8?	7. What is the product of 6 and 3?	
		-
8. What is 0 X 5?	9. What is 6 ÷ 2?	
		-
10. What is 5 ÷ 5?	11. What is 9 ÷ 3?	
		_

Name _____

12. Keisha has 9 boxes of crayons with 8 crayons in each box. What number sentence shows how many crayons she has?

13. Each of Eric's four friends gave him 9 marbles. How many marbles did Eric get?

14. Lian decides to plant an orchard. Her orchard looks like this.

What number sentence shows how many trees she has in her orchard?

Find the missing number in each number sentence:

15. 6 X _____ = 24

16. 42 ÷ _____ = 7

Solve:

17. Find the missing number. _____ X 8 = 8 X 5

What property does this number sentence show?

18. Michelle needs to find the missing number in a number sentence.

	2 X (5 X 7) = (2 X 5) X	
	What property does she need to use?	
19.	Find the missing number. 4 X 1 X 8 = 8 X X 1	
	What property does the number sentence show?	

20. Lee had a bag of dimes. She divided the dimes into 7 groups. If every group had 7 dimes in it, how many dimes did Lee have?



Prerequisite Skills Test

Answer Key

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1. 2 + 2 + 2 + 2 or 4 + 4
2. 5+5+5 or 3+3+3+3+3
3. 7+7+7+7 or 4+4+4+4+4+4+4
4. 12÷3
5. 20-5-5-5-5
6. 56
7. 18
8. 0
9. 3
10. 1
11.3
12. 9 X 8 = 72 or 8 X 9 = 72
13.36
14. 3 X 5 = 15 or 5 X 3 = 15
15.4
16.6
17. 5, commutative property
18. 7, associative property
19. 4, commutative property
20.49
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This test measures the following prerequisite skills:

Items 1-3, 6-8, 13, 20-Multiply 1-digit numbers

- Items 4–5, 9–11—Divide using repeated subtraction
- Items 12, 14–16—Find missing numbers in number sentences

Items 17–19—Recognize and use the commutative and associative properties of multiplication

Any students that miss two or more items in any given area should be given appropriate intervention instruction.

G Level 4 th	rade I/Course Grade	Duration: 60 min.Unit: DivisionDate:Preparing the Learner Lesson # ALaunching Mathematical Discourse			
Comn Star	non Core ndards	 4th Grade Operations and Algebraic Thinking Gain familiarity with factors and multiples. 4. Find all factor pairs for a whole number in the range 1–100. Recognize that a whole number is a multiple of each of its factors. Determine whether a given whole number in the range 1–100 is a multiple of a given one-digit number. Determine whether a given whole number in the range 1–100 is prime or composite. 			
Materials/ Resources/ Lesson Preparation		Mathematical Tools: Mystery Number cards; Hundred Chart; peanut butter, a knife, and bread Media/Technology to be used to deepen learning: ST Math Whole Number Multiplication and Division Module Supplementary Materials: <i>Get it Together</i> by Equals;			
Obj	ectives	Content:		Language:	
De Knowle	pth of edge Level	Level 1: Recall	Level 2:	Skill/Concept	
Store d	landa fan				
Standards for Mathematical		\square 1. Make sense of problems and persevere in solving them.			
Practice		\square 2. Acason abstractly and quantitatively.			
		\square 5. Construct viable arguments and critique the reasoning of others.			
		\sim 4. Model with mathematics.			
		\Box 5. Use appropriate tools strategically			
		7 Look for and make use of structure			
		\boxtimes 8. Look for and express regularity in reneated reasoning			
Comp	non Core	Focus on the Standards			
Instr	uctional	\boxtimes Coherence within and across grade levels			
Sh Math	ifts in 1ematics	\boxtimes Bigor (Balance of concentual understanding, procedural skill & fluency, and application of skills)			
	z	KEY WORDS ESSENTIAL TO	UNDERSTANDING	WORDS WORTH KNOWING	
ocabulary Fier III)	TEACHER PROVIDES SIMPLE EXPLANATIO	Digits Multiple Clue		Mystery	
ic Vo I & J	H	Even		Located	
adem Fier]		Odd Sum		Largest	
AC AC C C STUD IGURE (Difference			
Pre-t	eaching				
Consid	derations				

Lesson Delivery						
Instructional Check method(s) used in the lesson:						
Methods		⊠ Modeling	Guided Practice	🔀 Collaboration		
		Independent Practice	🛛 Guided Inquiry	⊠ Reflection		
	Lesson	Prior Knowledge:				
	Opening	Context and Motivation: Today we are going to practice hat telling someone else how you mad sandwich? (Ask for volunteers. Ac thought of your own.) "Put the pea bread. Children will laugh.) "Oper the loaf of bread.) "Use the knife," If I didn't know anything about how Math talk has to be the same way. of the steps. Today, we'll practice telling each	ving a productive classroom dis- le something and why. Who can ecording to responses, act really mut butter on the bread." (Place in the jar first." Then what? (Ope etc. we to make a peanut butter sand You have to tell exactly what you other what we did to solve a pro-	cussion through "math talk". Math talk is like tell me the steps to making a peanut butter dense, and do only what they say, with no the jar of peanut butter on top of the loaf of en the jar, then place the open jar on top of wich, could I make one with these directions? ou did to solve a problem, not leaving out any blem.		
		The purpose of this lesson is to	launch quality discourse in t	he Differentiated Instruction:		
uum	tanding	mathematics classroom. <u>Preparation for the lesson:</u> Run cards so that each group will ge of Mystery Number cards, so tw for a class of 32. Cut the six car envelope or baggie. Each group Hundreds Chart.	enough copies of the Myster et one set. There are four diffe wo copies of each set will be rds apart and place them into o will also need one copy of t	y Number erent sets sufficient an he English Learners: Sentence frames using key vocabulary words: The are 1, 2, 3, 4, 5, 6, 7, 8, and 9. When put together, they form (digits, numbers)		
Lesson Continu	Activities/Tasks/ Strategies/Technology/ Questioning/Engagement/Writing/Checking for Underst	Hundreds Chart. <u>Discuss Group Norms:</u> 1) Listen respectfully. 2) Only one person can talk at a 3) Everyone must get a turn to <u>Guided PracticeFishbowl:</u> Select one group of three or four thinking process, while everyon Place this group in the center, w around them. Give this group a Hundreds Chart. <u>Instructions:</u> "In the envelope you will find of will take just one card to begin. Each card contains a clue to he Number." "Take turns reading your clues fit that clue. Use the Hundreds clues, until you have decided w "If you get stuck, take another of	a time. speak. Ir students to demonstrate the ne else watches. with everyone else seated in a set of Mystery Number card Leave the extra cards in the lp you figure out the Mystery out loud, and deciding which Chart to help you keep track which number fits all the clues clue out of the envelope."	My number is an number. I say it when I count by (even, 2s)My number is a of I say it when I count by (multiple, 5, etc.)eirYou find the of two numbers when you (sum, add or difference, subtract)ch of you envelope.Special Needs: Heterogeneous groups to give support for struggling students.numbers of all the s."Same sentence frames as given for English Learners.		
		"Keep talking about the clues u number."	ntil everyone agrees on the s	ame		

	 Each member of the group will read their card aloud, and discuss which numbers fit their clue. The teacher will chart the process for the group on chart paper or white board. Fishbowl Reflection: Did the members of this group take turns speaking? Did everyone have a turn to talk? Were the others quiet while one person was speaking? If more than one number fit the clue, how did they decide which number was the correct one? Do you have any suggestions for this group? Who can tell this group one thing they did that made their discussion interesting? Independent Practice: Place students in groups of three or four, with a variety of levels in each group (high, medium, and low, if possible). Make sure that students in each group are seated close enough together to see clearly and to share materials. Pass one Hundreds Chart and one set of Mystery Number cards to each group. Review Instructions: "How many cards are in each envelope? How many cards will each person take to begin? Where will you leave the extra cards? Remember to take turns and make sure everyone has a chance to talk. Keep talking about the clues until everyone agrees on the same number. What will you do if you get stuck?" "When everyone in your group agrees that you have found the right number, write down the steps your group used to solve the mystery." Allow groups to work until they have found the Mystery Number. Then ask groups to record the steps they used to find the Mystery Number. Math Meeting: Bring students together to discuss their solutions and how they worked together. Did the group clearly state each step they followed in finding their Mystery Number? 	Accelerated Learners: Advanced learners can be asked to create their own clues for a number, and present their clues for others to solve.
	Lesson Reflection	
Teacher Reflection Evidenced by Student Learning/ Outcomes		

Hundred Chart

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Tim's Number	Tim's Number
Tim's number is a multiple of three.	Tim's number is a multiple of five.
Help your group find Tim's number on the Hundred's Chart.	Help your group find Tim's number on the Hundred's Chart.
Tim's Number	Tim's Number
If you add the digits of Tim's number, you get an odd number.	Tim's number is odd.
Help your group find Tim's number on the Hundred's Chart.	Help your group find Tim's number on the Hundred's Chart.
Tim's Number	Tim's Number
If you multiply the digits of Tim's number together, you get an even number.	Tim's number is near the center of the chart.
Help your group find Tim's number on the Hundred's Chart.	Help your group find Tim's number on the Hundred's Chart.

Meg's Number	Meg's Number
The sum of the digits of Meg's number is greater than ten. Help your group find Meg's number on the Hundred's Chart.	The difference between the two digits of Meg's number is greater than three. Help your group find Meg's number on the Hundred's Chart.
Meg's Number	Meg's Number
Meg's number is a multiple of seven.	The first digit of Meg's number is larger than the second.
number on the Hundred's Chart.	number on the Hundred's Chart.
Meg's Number	Meg's Number
Meg's number is not odd.	Both digits of Meg's number are even.
Help your group find Meg's number on the Hundred's Chart.	Help your group find Meg's number on the Hundred's Chart.

Paul's Number	Paul's Number
Paul's number is not located on an edge or a corner.	Paul's number is not an even number.
Help your group find Paul's number on the Hundred's Chart.	Help your group find Paul's number on the Hundred's Chart.
Paul's Number	Paul's Number
The difference of the digits in Paul's number is three.	Paul's number is not a multiple of three, five, or seven.
Help your group find Paul's number on the Hundred's Chart.	Help your group find Paul's number on the Hundred's Chart.
Paul's Number	Paul's Number
Paul's number is less than fifty.	The sum of the digits in Paul's number is eleven.
Help your group find Paul's number on the Hundred's Chart.	Help your group find Paul's number on the Hundred's Chart.

Kelly's Number	Kelly's Number
Kelly's number is a multiple of three.	The sum of the digits of Kelly's number is even.
Help your group find Kelly's number on the Hundred's Chart.	Help your group find Kelly's number on the Hundred's Chart.
Kelly's Number	Kelly's Number
Kelly's number is the largest number on the chart that fits all of the other clues.	Kelly's number is a multiple of five.
Help your group find Kelly's number on the Hundred's Chart.	Help your group find Kelly's number on the Hundred's Chart.
Kelly's Number	Kelly's Number
When you multiply the digits of Kelly's number together, you get an odd number.	Kelly's number is larger than 50.
Help your group find Kelly's number on the Hundred's Chart.	Help your group find Kelly's number on the Hundred's Chart.

Grade Level/Course 4 th Grade	Grade Level/Course 4th GradeDuration: 60 min. Date:Unit: Division Preparing the Learner Lesson # B Collaborative Work on Sequencing and Making Equal Share			
Common Core Standards	4th Grade Operations Gain familiarity with f 4. Find all factor pairs for multiple of each of its fa multiple of a given one- 100 is prime or composi	ons and Algebraic Thinking ith factors and multiples. Its for a whole number in the range 1–100. Recognize that a whole number is a ts factors. Determine whether a given whole number in the range 1–100 is a one-digit number. Determine whether a given whole number in the range 1– posite.		
Materials/ Resources/ Lesson Preparation	Mathematical Tools: Math journals, Thinking Maps, counters, realia (cookies or brownies) Media/Technology to be used to deepen learning: ST Math Whole Number Multiplication and Division Module Supplementary Materials: The Doorbell Rang, by Pat Hutchins			
Objectives	Content: Students will practice w collaboratively and shar Students will determine cookies per child based children and the number	working aring strategies. e the number of d on the number of er of cookies. Language: Students will write the story in sequence and add effective ending to the story. Students will share stories orally in group presentations.		
Depth of Knowledge Level	□ Level 1: Recall □ Level 2: Skill/Concept □ Level 3: Strategic Thinking □ Level 4: Extended Thinking			
Standards for Mathematical Practice	 1. Make sense of pro 2. Reason abstractly 3. Construct viable 4. Model with math 5. Use appropriate t 6. Attend to precision 7. Look for and matical 8. Look for and exp 	oblems and perseve y and quantitativel arguments and cri ematics. tools strategically on. ke use of structure press regularity in r	ere in solving them. y. tique the reasoning of others. repeated reasoning.	
Common Core Instructional Shifts in Mathematics	 ➢ Focus on the Standards ➢ Coherence within and across grade levels ➢ Bizer (Belence of concentral and across frame areas have built of the second seco			
DES DES	KEY WORDS ESSENTIAL TO	UNDERSTANDING	WORDS WORTH KNOWING	
Academic Vocabulary (Tier II & Tier I TEACHER PROVII SIMPLE EXPLANAT	Division			

	STUDENTS IGURE OUT THE	Equal shares Equal amount The same Divided equally
Pr Coi	e-teaching nsideration	s This lesson is designed for students who have basic concept of division.
In	structional	Lesson Delivery Check method(s) used in the lesson:
111	Methods	\boxtimes Modeling \square Guided Practice \square Collaboration
		$\square \text{ Independent Practice} \qquad \square \text{ Guided Inquiry} \qquad \square \text{ Reflection}$
	Lesson	Prior Knowledge: This lesson is designed for students who have basic concent of division
Lesson Continuum	Opening	The Ruberteelest in a construction is ducents with have basic concept of division. Context and Motivation: "Today we are going to read a story about a family that is sharing cookies with the neighborhood children. How many of you have heard this story before?" (Show the cover of the book.) "Good, you can help us when we are recalling the number of children present and how many cookies each child will get to eat. Now let's read the story." Read the book, <i>The Doorbell Rang</i> . "Let's make a flow map to show the sequence of this story, focusing on the number of children present and the number of cookies each child can eat." In the beginning, there were how many children? (2) How many cookies did mother bake? (12) If Mother baked 12 cookies for 2 children, how many cookies could each child eat? (6) Let's put that information into a Flow Map. Start the story with the students, adding transition words, and soliciting from them the number of children and the number of cookies for each child. Ask, "Did the children always share the cookies equally? Did every child get the same amount?" In the beginning there were 2 children with 12 cookies. Each child could eat cookies. Each child could eat cookies. Each child could eat cookies. Finally, the story. Way, adding information from them. Then ask them to go to the researt and complete the Flow Map, adding information for the number of children and the number of cookies they could eat. "Now we are going to write the end of the story. Work with a partner to rewrite the story, adding a logical ending. You need to tell how many cookies Grandma brought with her, and how many cookies equally. If there are twelve children, how can be sure that the children can share the cookies equally. If there are twelve children, how can be sure that the children will be able to share all the cookies equally.

	Today's lesson has several purposes: 1) to encourage collaborative work among the students, 2) to write a sequential narration of events using appropriate transitional words 3) to show a relationship between the number of children, the number of cookies, and the number of cookies each child can eat.	Differentiated Instruction: English Learners: children eat cookies.
Activities/Tasks/ Strategies/Technology/ Questioning/Engagement/Writing/Checking for Understanding	Guided Inquiry: 1) Form pairs or small groups of three students to work together. Students should be grouped so that everyone can see easily and share materials with one another. 2) Students need paper or math journals for writing. 3) First the students will complete the Flow Map to show the sequence of the story. 4) Then, they will add an ending that tells how many cookies Grandma brought, and how many cookies each child can eat. 5) The final part is to show the relationship between the number of cookies provided, and the number each child can eat. Students may draw a picture, make a table, use tally marks, or show the relationship in a Bridge map Circulate around the room as students are working, asking guiding questions, and encouraging diverse thinking. As you walk around, take note of students who have depicted the information in mathematically powerful ways. Look for organization, clarity, and connections between depictions. The actual work should not take more than about twenty minutes. Math Meeting: Call students together. Ask select students to share their endings to the story. How many cookies did Grandma bring? Students can share their various methods to depict the information. Make connections between different students' work. Ask students to describe how a drawing may show the same information. Post sample sentence frames to aid student responses: I like how children, just as 's table shows the same information. used to show the cookies were divided into equal groups. and by	If there were children sharing cookies, they would each get cookies. If Grandma brought , then there would be and each child could eat Special Needs: Give counters Students may draw their responses. Same sentence frames as given for English Learners.

	Activities/Tasks/ Strategies/Technology/ Questioning/Engagement/Writing/Checking for Understanding	Make a Bridge Map to show the relationship between the number of children sharing cookies and the number of cookies they get to eat. <u>12 Cookies</u> 2 children <u>4 children</u> <u>6 children</u> <u>6 cookies</u> <u>3 cookies</u> <u>2 cookies</u> Relating factor: "could eat" or "would receive" Have students "read" the Bridge Map. "If there were 2 children sharing 12 cookies, each child could eat 6 cookies. However, if there were 6 children sharing 12 cookies, each child could eat only 2 cookies." Replace numbers of cookies with those given in the student responses. <u>Possible culminating activity:</u> Bring in cookies or brownies for the students to share equally.	Accelerated Learners: Choice of number of cookies brought by Grandma. If not a multiple of twelve, how can the cookies be divided equally? Ask students how many cookies would each child get if there were twelve cookies for five children, or for eight or nine? These students can make a Bridge Map to show the relationship between the number of cookies and the number of children.
		Lesson Reflection	
Teacher Reflection Evidenced by Student Learning/ Outcomes			

G Level	rade I/Course	Duration: 60 min. Date:	Unit: Division Preparing the Learner Lesson # C				
4	Grade		Multiplication Clusters				
Comn Star	non Core ndards	4th Grade Operations Gain familiarity with f 4. Find all factor pairs for multiple of each of its fa multiple of a given one- 100 is prime or composi	Operations and Algebraic Thinking arity with factors and multiples. actor pairs for a whole number in the range 1–100. Recognize that a whole number is a each of its factors. Determine whether a given whole number in the range 1–100 is a a given one-digit number. Determine whether a given whole number in the range 1– e or composite.				
Materials/ Resources/ Lesson Preparation		Mathematical Tools: Math journals, base 10 blocks may be used, if needed Media/Technology to be used to deepen learning: ST Math Whole Number Multiplication and Division Module Supplementary Materials: Multiplication Cluster pages					
Obj	jectives	Content: Students will solve clust multiplication problems some way.	ters of that are related in	Language: Students will tell and write how they solved the cluster of problems, and how the problems are related.			
De Knowle	epth of edge Level	Image: Second state in the second s					
Standards for Mathematical Practice		 ☑ 1. Make sense of problems and persevere in solving them. ☑ 2. Reason abstractly and quantitatively. ☑ 3. Construct viable arguments and critique the reasoning of others. ☑ 4. Model with mathematics. ☑ 5. Use appropriate tools strategically ☑ 6. Attend to precision. ☑ 7. Look for and make use of structure. ☑ 8. Look for and express regularity in repeated reasoning. 					
Common Core Instructional Shifts in Mathematics		 ☑ Focus on the Standard ☑ Coherence within and ☑ Rigor (Balance of con 	ds l across grade levels ceptual understandi	ng, procedural skill & fluency, and application of skills)			
ocabulary Tier III)	TEACHER PROVIDES SIMPLE EXPLANATION	KEY WORDS ESSENTIAL TO Solve Cluster Product Related	UNDERSTANDING	WORDS WORTH KNOWING			
Academic V (Tier II &	STUDENTS FIGURE OUT THE MEANING						

Pre-teaching Considerations		g 15	This lesson is designed for students who have basic multiplication facts to 10.				
			Lesson Delivery				
Instructional		l	Check method(s) used in the lesson:				
Methods			🖂 Modeling	Guided Practice	🛛 Collab	oration	
			Independent Practice	🛛 Guided Inquiry	🛛 Reflec	tion	
m	Lesson P Opening C g ff c V n n 7 4 4 7 5		rior Knowledge: This lesson is designed for students who have basic multiplication facts to 10. ontext and Motivation: How many of you think you can solve tough multiplication problems in your head? Today we are bing to solve clusters of multiplication problems in creative ways, without pencil and paper. We will nd connections between the problems, and figure out ways to solve problems we never thought we build solve mentally." Write 4 X 32 on the whiteboard, then say, "The first problem we will attempt to solve is 4 X 32. How hany of you think you can solve that problem in your head without pencil and paper?" Give a few inutes to think. hen tell the students: A cluster of easier problems that may help us solve this tough problem are: X 3, 4 X 2, 3 X 10, 3 X 40, and 4 X 30. Write these problems on the whiteboard. sk students to turn to an elbow partner to discuss the cluster problems and how the problems are clated to each other, and how they are related to the original problem. Call on specific students to hare their ideas. (4 X 3 is related to 4 X 30, because 30 is ten times as much as 3.)				
Lesson Continu	Activities/Tasks/ Strategies/Technology/ Questioning/Engagement/Writing/Checking for Understanding	Th str Nc wi eau ab pro Se Se Se Se Se Se Se	the purpose of this lesson is to rategies can lead to competence ow we will solve other cluster ill receive two clusters of mul ill decide how the problems an och of the problems in the clus bout how you solved it. Tell he oblem to help you find the an et A: 5 X 3, 5 X 10, 10 X 3, 30 et B: 2 X 5, 3 X 5, 10 X 5, 30 et C: 5 X 7, 10 X 7, 2 X 7, 20 et D: 3 X 5, 2 X 5, 10 X 5, 20 et E: 3 X 6, 3 X 3, 3 X 10, 6 X et F: 2 X 5, 2 X 4, 2 X 10, 10 T	show how knowing multipli- ce in division, as well. Ts of problems. You and your tiplication problems. Togeth re related to each other, then ster. After you solve each clu ow you used the answer for o swer to another problem. O X 5, 50 X 3, 55 X 3 X 5, 32 X 5 X 7, 25 X 7 X 5, 23 X 5 X 10, 3 X 60, 63 X 3 X 5, 2 X 50, 2 X 54	cation partner er, you solve ster, write one	Differentiated Instruction: English Learners: Sentence frames: is like because I know that groups ofis, groups ofis, sogroups of would be If you multiply, the product is, while if you multiply, the product is	

		Special Needs:
	Set G: 7 X 2, 3 X 2, 7 X 10, 2 X 10, 7 X 20, 2 X 73	Access to base 10 blocks Perhaps just one cluster of
	Set H: 5 X 3, 6 X 2, 10 X 6, 6 X 5, 60 X 5, 6 X 52	problems to solve Work with a partner
	Set I: 8 X 2, 8 X 10, 20 X 8, 10 X 2, 80 X 2, 81 X 2	Sentence frames as
	Set J: 2 X 6, 10 X 6, 3 X 6, 13 X 6, 23 X 6	Learners.
	All of these cluster problems are found on the pages following this lesson. Give one page to each pair of students.	Accelerated Learners: Students may write their own cluster of problems
	Give time for students to solve their cluster, and to write about how they solved the problems. Allow access to base ten blocks or other manipulatives for those students that need them.	and tell how the problems are related.
	Post and use these sentence frames to help EL Learners to put their ideas into words. Model how to use the sentence frames with the first cluster you gave students. Tell students they could also use the sentence frames for journal responses.	
	Sentence frames: is likebecause	
	I know that groups of is, so groups of would be	
	If you multiply, the product is, while if you multiply, the product is	
	Math Meeting: Call students together with their math journals. Ask pairs of students to present their solutions to the cluster of problems they solved. You may ask student presenters to lead the discussion by asking other students to point out connections between the problems. This will involve all students in focusing on the problems presented and their solutions.	
	<u>Guiding Questions:</u> How will solving clusters of problems like this help us to be better problem solvers? Can you think of a time when being able to solve tough multiplication problems in your head might be important?	
	division?	
	Lesson Reflection	
Teacher		
Reflection		
by Student		
Learning/		
Outcomes		

Sets A and B

Set A	
	5 X 3 =
	5 X 10 =
	$10 \times 3 =$
	$30 \times 5 =$
	$50 \times 3 =$
	50 X 5
	$55 \times 3 =$
Sat D	
Set D	
	2 X 5 =
	3 X 5 =
	$10 \times 5 =$
	$30 \times 5 =$
	50×5
	$32 \times 5 =$

Sets C and D

Set C		
	5 X 7 =	
	10 X 7 =	
	2 X 7 =	
	20 X 7 =	
	25 X 7 =	
Set D		
	3 X 5 =	
	2 X 5 =	
	10 X 5 =	
	20 X 5 =	
	23 X 5 =	

Sets E and F

Set E	
	3 X 6 =
	3 X 3 =
	3 X 10 =
	6 X 10 =
	3 X 60 =
	63 X 3 =
Set F	
	2 X 5 =
	2 X 4 =
	2 X 10 =
	$10 \ge 5 =$
	2 X 50 =
	2 X 54 =

Sets G and H

Set G	
	7 X 2 =
	3 X 2 =
	7 X 10 =
	2 X 10 =
	7 X 20 =
	2 X 73 =
Set H	
	5 X 3 =
	6 X 2 =
	10 X 6 =
	6 X 5 =
	60 X 5 =
	6 X 52 =

Sets I and J

Set I	
	8 X 2 =
	8 X 10 =
	20 X 8 =
	10 X 2 =
	80 X 2 =
	81 X 2 =
Set J	
	2 X 6
	10 X 6
	3 X 6
	13 X 6
	23 X 6

Unit: D	ivision	Grade Level/Course	Duration: 60 min			
Lesson	#1	4 th Grade Date:				
Ar	rays					
Comm	on Core dards	4th Grade Operations	and Algebraic Thi	nking		
Stan	uarus	Gain familiarity with f	actors and multiple	es.		
		4. Find all factor pairs for	or a whole number i	n the range 1–100. Recognize that a whole number is a		
		multiple of each of its fa	ctors. Determine wl	nether a given whole number in the range 1–100 is a		
		multiple of a given one-	digit number. Deter	nine whether a given whole number in the range 1–		
		100 is prime or composi	te.	re Terr		
		4th Grade Number and Use place value unders	tanding and prope	se 1 cm rties of operations to perform multi-digit		
		arithmetic.	tanding and prope	rees of operations to perform mater agre		
		6. Find whole-number q	uotients and remain	ders with up to four-digit dividends and one-digit		
		divisors, using strategies	based on place val	ue, the properties of operations, and/or the relationship		
		between multiplication a	and division. Illustra	te and explain the calculation by using equations,		
		rectangular arrays, and/c	n area moders.			
Mate	erials/	Mathematical Tools: 1	" square tiles, graph	ing paper, counters, realia (egg cartons, six pack of		
Reso	urces/	juice)				
Les	sson	Media/Technology to b	e used to deepen le	earning: ST Math Whole Number Multiplication and		
гтера	iration	Division Module Supplementary Materials: TERC Math Anneal, "Frog-Gone"(provided in PowerPoint)				
		Supplementary materi				
Obje	ectives	Content:		Language:		
		Students will be able use	e arrays to model	Students will be able to explain the relationship		
	and division. Students will relate			between multiplication and division using arrays.		
		multiplication and division notation				
		representing arrays.				
Dep	oth of day Level	Level 1: Recall Level 2: Skill/Concept				
KIIOWIC	uge Level	☐ Level 3: Strategic Thinking ☐ Level 4: Extended Thinking				
Standa	ards for	🛛 1. Make sense of pro	oblems and persev	ere in solving them.		
Mathe	matical	2. Reason abstractly and quantitatively.				
r ra	cuce	3. Construct viable arguments and critique the reasoning of others.				
		│ ── │ ⊠ 4. Model with math	ematics.			
		\Box 5. Use appropriate t	ools strategically			
		\square 6 Attend to precision	on			
		\Box 7. Look for and ma	ke use of structure			
		\boxtimes 8. Look for and exp	ress regularity in r	eneated reasoning.		
Comm	on Core	Eccus on the Standard	1055 10gunu 10g 11 1	cpearea reasoning.		
Instru	ictional	\square Coherence within and across grade levels				
Shifts in		Denote the second secon				
Mathe	Mathematics 🛛 🖄 Rigor (Balance of conceptual understanding, procedural skill & fluency, and application of			ig, procedural skill & fluency, and application of skills)		
Î	IDES N	KEY WORDS ESSENTIAL TO	UNDERSTANDING	WORDS WORTH KNOWING		
nic lary 'ier l		Inverse operations				
ader abul & T	R PR MPI	Dimensions				
Ac: Voc: T II	SII SII	Orientation				
(Tie	TEA(E)					

	Ш	Array		Multiplic	cation			
		Row		Division				
		Column						
	STU URE							
Pr	e-teaching							
Сог	nsideration	s Knowledge of	equal groupings	, repeated addition				
				Lesson Delivery				
In	structional	Check metho	d(s) used in the	lesson:				
	Methods	☐ Modeling	.,	Guided Practice	\square Collaboration			
			ent Practice	Guided Inquiry	Ketlection			
	Lesson	Prior Knowledg	e: Knowledge of	f equal groupings, repea	ated addition			
	Opening	Context, Motiva	tion :	1 1				
		Today's big idea	is "Multiplication	on and division are diffe	", "erent ways to look at the same problem			
		"Today you are o	in be represented	evidence to prove the h				
		Today you are g	,oning to rook for	evidence to prove the e				
		"First let's notice	arrays in this po	em: (read "Frog-Gone'	") What about the objects around us?"			
		(Get student resp	Get student responses, quick draw a few of their responses)					
		Ask students if th	iey remember wl	hat the arrangement is c	called. Introduce the word dimension into			
		your conversion	and write <u>dimens</u>	<u>sion</u> to the side of a pict	ture from the story with the description of the			
		allay.	array.					
		How many rows	Tell students: "Groups of things often come in rectangular arrays. Imagine a six-pack of juice cans.					
Е		On the based base	do you see! Ho		State it and the iteration of the iterat			
inn		On the board beg	gin a chart where	e you can write the nar	ten in both ways) and draw the array in			
ntin		both orientations. Here's a format you could use:		ten in ootn ways), and draw the array in				
Col		Item	Total	Dimension	Arravs			
uo		Eggs	12	2 rows of 6				
ess		00*		2x6 6 rows of 2				
Η				6x2				
		pack of juice	6					
		Box of						
		muffins						
		Show the follow	ing items as they	vare discussed: a six-n	ack of juice cans, eggs, pack of vogurt (For			
		ELs and visual learners)						
		Write down some of the students' ideas on your chart. Begin to use the word <i>dimensions</i> naturally,						
		just as you have introduced other mathematical terms into the dialogue with your class. Describe the						
		arrays as "3 by 2"	' or "4 by 3," so	students become used t	o hearing this language.			
		Show students pictures of simple arrays. Show first 26 slides. Pause for discussion after the orchards.						
		Ask students for	ideas to add to o	ur chart.				

		Guided Inquiry	Differentiated Instruction:
		"When a group of people need to sit down, we often arrange chairs in an array that fits the space. Can you think of some of the places this happens?" (movie theater, bus. airplane, school auditorium) Show slides 28-31.	English Learners: Use visuals, realia
		"How could we arrange chairs in a rectangular array for a group of 18 people? How else might 18 chairs be arranged in an array?"	Special Needs: Use visuals, realia
		Students, working in pairs, use cubes to make all the arrays they can for 18. Ask each group to choose one of their arrays and cut it out from the graph paper.	
gy/ Understanding	logy/ or Understanding	Make sure each possible array for 18 is represented. Collect a sample of each array for 18 from the students and post them where all can see them. Some students will see 3 x 6 and 6 x 3 as two different arrays; others will think of them as the same. Allow students to discuss their ideas about this. We suggest that you put up both arrangements, posting pairs next to each other. Arrays provide a model that helps students visualize how multiplication pairs, such as 3 x 6 and 6 x 3, are related. (If you put up all the pairs, you should have 6 arrays: 1 x 18, 18 x 1, 2 x 9, 9 x 2, 3 x 6, and 6 x 3.)	Accelerated Learners: Give students multiple opportunities to explore arrays such as in an online investigation.
	strategies/Techno iting/Checking fo	Ask students to help you label the dimensions of the arrays. This is a good time to establish a class convention for which arrays will be labeled $3 \times 6 (3 \text{ rows of } 6)$ and which will be labeled $6 \times 3 (6 \text{ rows of } 3)$. A convention will help students and you communicate with one another more clearly.	
	vities/Tasks/ S ngagement/Wr	Show slides 33 to 42 and assign pairs of students to create arrays for either the doughnut problem or the ornament boxes. (Students could create their arrays with blocks, tiles, in their journals, or on graph paper.	
Activ Questioning/En	Acti Questioning/En	Reflection: Counting Squares in Arrays Ask students for their ideas about ways to count one of the arrays, for example, the 3 by 6 array. Some students will count the arrays by 1s, counting each individual square. Other students will see that a 3 x 6 array can be counted by 3s $(3, 6, 9, 12, 15, 18)$ or by 6s $(6, 12, 18)$. Sometimes students come up with more inventive ways, such as seeing a 3 x 6 as consisting of two 9s. Emphasize counting by groups by having students look at other arrays for 18. As students make arrays for other numbers in the next activity, continue to encourage them to count their arrays by groups.	
		"What items have the same number of objects along each side? (For example, 10 x 10) How are these arrays different from other arrays? These are square numbers."	
		Closing questions: "How is what we did today related to the big idea: Multiplication and division are different ways of looking at the same problem situation? Both can be represented using What goes in the blank? (arrays) Why? Write about it. What are some other numbers you would like to investigate?"	

Lesson Reflection			
Teacher			
Reflection			
Evidenced			
by Student			
Learning/			
Outcomes			


Unit: Division	Grade Level/Course	Duration: 60 min					
Lesson # 2	4 th Grade	Date:					
More Arrays	Contont Standarda						
Standards	4th Grade Operations	and Algebraic Thi	nking				
	Gain familiarity with f	actors and multiple	es.				
	4. Find all factor pairs for	or a whole number i	n the range 1–100. Recognize that a whole number is a				
	multiple of each of its fa	ctors. Determine w	hether a given whole number in the range 1–100 is a				
	100 is prime or composi	aigit number. Deter	mine whether a given whole number in the range 1–				
	4th Grade Number and	d Operations in Ba	se Ten				
	Use place value unders	tanding and prope	rties of operations to perform multi-digit				
	arithmetic.						
	6. Find whole-number q	uotients and remain	ders with up to four-digit dividends and one-digit				
	between multiplication a	and division. Illustra	te and explain the calculation by using equations,				
	rectangular arrays, and/o	or area models.					
Materials/	Mathematical Tools: 1	" square tiles graph	ning paper counters				
Resources/	Media/Technology to b	e used to deepen le	earning: ST Math Whole Number Multiplication and				
Lesson	Division Module ; http:/	/www.harcourtscho	ol.com/activity/space_arrays/;				
Preparation							
Objectives	Content:		Language:				
	Students will be able to	analyze a number	Students will be able to express their number's factor,				
	amount to solve a proble candy boxes (arrays). The	eir work focuses	product, divisors, dividends, and quotient, and present their findings in a poster				
	on:	ien work locuses	present then manigs in a poster.				
	 finding factors of 	of numbers					
	 recognizing prin 	ne numbers as					
	numbers with or	nly one pair of					
	lactors						
Donth of			Sh:W/Concept				
Knowledge Level	Level 1: Recall	nking 🕅 ovol 4:	Skin/Concept				
Standards for Mathematical	■ 1. Make sense of pro	oblems and perseve	ere in solving them.				
Practice	2. Reason abstractly	y and quantitativel	у.				
	3. Construct viable	arguments and cri	tique the reasoning of others.				
	🛛 4. Model with math	ematics.					
	🗌 5. Use appropriate t	cools strategically					
	6. Attend to precision	on.					
	7. Look for and ma	ke use of structure					
	🛛 8. Look for and exp	ress regularity in r	epeated reasoning.				
Common Core	Focus on the Standard	ds					
Instructional Shifts in	Coherence within and	across grade levels					
Mathematics	Rigor (Balance of con	ceptual understandi	ng, procedural skill & fluency, and application of skills)				

	DES	-	KEY WORDS ESSENTIAL TO UNDERSTANDING	WORDS WORTH KNOWING					
Vocabulary		SIMPLE EXPLANATION	Factors Prime number Composite number Area model	Inverse Dimension					
Academic Tron II	STUDENTS	FIGURE OUT THE MEANING							
Pr Cor	e-teach 1siderat	ing tions	Notation of dimensions of arrays are determ	ined by their orientation (rows of)					
T			Lesson Deli	very					
In	structio Method	onal Is	Check method(s) used in the lesson:						
Wiethous			□ Modeling □ Guided Practice □ Collaboration						
			🗌 Independent Practice 🛛 🖾 Guided	Inquiry 🛛 Reflection					
	Lesso	n P	rior Knowledge: Notation of dimensions of	arrays are determined by their orientation (rows of					
	Openii	ng T si	_) context and Motivation: oday's big idea is "Multiplication and divisio tuation."	n are different ways to look at the same problem					
Е									
nnu			Unclear Idea Already Know	Research New Think How to Information Apply It					
Lesson Contin			Ants needed best way to get to the picnic <u>if</u> they are closer they may move faster∧	Experiment with information 2 by 50 Ants travel 4 by 25 best in a line 5 by 20 10 by 10∧					
		T T C T P	his makes a nice bridge map. The analogy rel hey will go through the same process. First properties the bridge map. oday we will investigate the big idea further. ower point also shows the story. Stop before y	ates to the process the ants went through to learn. resent the learning process. Then read the story. Then We will start by reading "100 Hungry Ants" The you go on to the chocolates.					

Questioning/Engagement/Writing/Checking for Understanding	Guided InquiryEach student works with a partner to find different ways to formarrays using a given number.At the end of the story are slides of chocolates. Present the context ofthe activity and then show the slides.Context: You are in the candy business. Your company must designcandy boxes to package a certain number of chocolates. Each designteam must create boxes for a different number of chocolates. Flanall your ideas, draw them, cut them out and paste them on yourteam's poster.Write the multiplication equations on one side and the division onthe third for your number of chocolates.Just as the ants found the arrays for 100, you (students) will findall the arrays for your number of chocolates.Ask students to contribute any interesting numbers they would like toinvestigate. We suggest students make arrays for the following sizegroups: 10, 14 through 30, 32, 36, 40, 42, 44, 45, 48, 49, and 50.Either assign to each pair of students one of these numbers to work onor write the numbers on an index card or post-it and let studentschoose the number they would like. List on a chart the numbers thatstudents have chosen as a way of keeping track of which numbershave chosen as a way of skeeping track of which numbershave been done. Students can use cubes or 124 Chocolates." Theyhave been done. Students and use for y	Differentiated Instruction: English Learners: Using sentence frames Using visuals Using a variety of guided questions: How can you know when you have found all the arrays for one number? (ELD Levels: I, EA) Have you found any numbers that have only one array? (ELD Levels: I, EA) How can you count your array to make sure the total is correct? (ELD Levels: All levels) Special Needs: Working in pairs Selecting appropriate numbers Using sentence frames Accelerated Learners: Choice of numbers to investigate
Quest	Gallery Walk: Place posters around the room accessible to students. Next to each poster place a blank sheet of paper. In pairs, students walk around to view all the array posters and jot down discoveries they have made. Students may add to observations made by others or pose questions.	
	 " As you walk around and look at the arrays, here are some things to pay attention to: How many arrays does each number have? (ELD Levels: B EI, I., EA) Can you find out anything about even and odd numbers? (ELD Levels: B. I.) See if you can make some discoveries by looking at all our arrays. (ELD Levels: I, A) 	

	Math Monting:
	In a class discussion students share and discuss these discoveries
	Make a graphic organizer of students' observations about the arrays
	they've constructed.
	Students might notice:
	Some numbers have only two arrays (for example, 13 x 1 and 1 x 13).
	Some students might say these numbers just have one array (since the
	two are really the same one in a different orientation). Another way to
	number itself. These special numbers are called <i>prime numbers</i> . What
	prime numbers have students found? Do they know any above 50?
	Numbers having more than two arrays—or more than two factors—
	are called <i>composite numbers</i> .
	Since arrays come in pairs (for example, 3 x 4 and 4 x 3), most
	numbers have an even number of arrays.
	A few numbers have an odd number of arrays. This occurs when one
	of the arrays is a square (for example 10×10) which does not have
	another orientation. Some students may recognize that these numbers.
	such as 16, 25, and 36, are the square numbers.
	Lesson Reflection
Teacher	
Reflection	
Evidenced	
Learning/	
Outcomes	
outcomes	

Unit: Division	Grade Level/Course	Duration: 60 min				
Multiplication	4 Graue	Date:				
& Division						
Concept	Ath Crada Onorations	and Algobraic Thi	aking			
Standards	Gain familiarity with f	actors and multiple	es.			
	4. Find all factor pairs for	or a whole number in	n the range 1–100. Recognize that a whole number is a			
	multiple of each of its fa	ctors. Determine wl	nether a given whole number in the range 1–100 is a			
	100 is prime or composi	te.	mine whether a given whole number in the range 1–			
	4th Grade Number and	l Operations in Ba	se Ten			
	Use place value unders	tanding and prope	rties of operations to perform multi-digit			
	6. Find whole-number a	uotients and remain	ders with up to four-digit dividends and one-digit			
	divisors, using strategies	based on place value	ue, the properties of operations, and/or the relationship			
	between multiplication a	nd division. Illustra	te and explain the calculation by using equations,			
	rectangular arrays, and/c	area moders.				
Materials/	Mathematical Tealer 1	²² a ann an t-1 a a ann 1	ing non-or counters moth issued for note taking			
Resources/ Lesson	Media/Technology to b	e used to deepen le	earning: ST Math Whole Number Multiplication and			
Preparation	Division Module	be used to deepen rear mig. ST that where reamber that preaten and				
Objectives	Content:		Language:			
	Students will be able to a	udents will be able to solve division Students will take notes on visual strategies and avalating a various strategies are related				
	strategies.	ty of visual explain now various strategies are related.				
Donth of			Skill/Concent			
Knowledge Level	Level 3: Strategic Thi	nking 🛛 Level 4:	s Skii/Concept Extended Thinking			
Standards for	1 Maka sansa af nr	blams and narsay	are in solving them			
Mathematical		blems and persevo	ere in solving them.			
Practice	2. Reason abstractly	y and quantitative	y.			
	3. Construct viable	arguments and cri	tique the reasoning of others.			
	▲ 4. Model with math	ematics.				
	5. Use appropriate t	ools strategically				
	6. Attend to precisio	on.				
	7. Look for and ma	ke use of structure.				
	🛛 8. Look for and exp	ress regularity in r	repeated reasoning.			
Common Core	Focus on the Standard	ls				
Shifts in Coherence within and across grade levels						
Mathematics	Rigor (Balance of con	ceptual understandi	ng, procedural skill & fluency, and application of skills)			
ic ury DVIDES ION	KEY WORDS ESSENTIAL TO	UNDERSTANDING	WORDS WORTH KNOWING			
idem abula II & R PRC MPLE NATI	Number line		T-Chart			
Aca Voca <u>Fier J</u> SIP SIP						
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	ΗE	Equal Groups Qui	ick Draws
		Repeated Subtraction	
		EAN	
	ST	Σ	
Pr	e-teaching	g Students should be able to relate multiplication a	and division as inverse operations.
Cor	nsideration	ns	-
In	structional	Lesson Delivery Check method(s) used in the lesson:	
	Methods	Modeling Cuided Pra	actice Collaboration
		Independent Practice Cuided Inc.	wiry \square Paflaction
		Duion Vn and day. Students should be able to relate	
		operations.	e multiplication and division as inverse
		Context and Motivation:	
		Today we want to make new connections to our big	g idea "Multiplication and division are different
		and question marks.)	students a tree map with the big idea and arrays,
	ing	Multiplication and division are dif	fferent ways to look at the
	pen	same problem situation.	
	0 u 0		
	esse	Arrays ? ?	<u> </u>
	Ι		
		Have students create the tree map in their math jour	rnals. You will need 8 hangers.
		What are some things that come in groups? (Anticip	pate things your students would say come in
u		pencils, Legos, bag of beads)	unche team, six pack of juice, soeks, nan ties,
Inur			
ntin		Start with a simple division word problem like 48 di the problem in context using one of the student's ide	livided by 8. Put leas i.e. Justin had
C0	L	48 marbles. He wanted to give some to 8 of his frien	nds so that each
sson	y/ Ig fo	friend had the same amount. How many marbles wi	ill each friend
Le	ologi ckin		
	chnc Che	Ask students how they would interpret the expression	on $48 \div 8$. Guide
	/Tec ing/	students to create an array of 8 rows of 6. Talk stude	lents through the
	gies Vrit ding	Ask "How many squares should we make in a row?	?
	rate ent/V stan	St.: Eight	
	s/ St jeme nder	1.: How many more do we need to make? St : 6 more	
	ask Igag Ur	Guide students to draw the array and label it with st	tudents using the
	es/T g/E1	correct number sentence $48 \div 8 = 6$.	
	iviti nin	Ask: How many marbles will each of Justin's friend Sts: They will receive 6 marbles each.	ds receive?
	Act estic		
	Qu		

											Differentiated Instruction:
	Tl Ju m	he array Istin's fi uch spa	v model riends h ace wou	can als ave 48 ld each	o be use square f friend b	ed to rej feet in v be using	present which to g fairly?	area. Fo play m	or exam arbles,	ple, if how	English Learners: Visual representation Guided teacher modeling of note taking
	[1	2	3	4	5	6	7	8	Use student ideas and verbalizations
			9	10	11	12	13	14	15	16	Provide sentence frames.
		9	17	18	19	20	21	22	23	24	
		•	25	26	27	28	29	30	31	32	
ng			33	34	35	36	37	38	39	40	
tandi			41	42	43	44	45	46	47	48	Special Needs:
/ derst	L					<u> </u>	2	I			student who will be able to
logy/ r Un						ſ)				provide support during the
hnol g foi											Provide sentence frames.
/Tec ckin		Have a	n array :	ready fo	or the ne	ext dem	onstrati	on. Cut	the arra	ay by	
egies /Che	1	rows ar	nd place	them to	ogether	end to	end. Ma	ark each	group	so that it	
tring		represe	nts a nu	mber n	ne.						
ks/ S /Wri											Accelerated Learners:
/Tas. nent			<u> </u>						<u> </u>		work with more challenging
ities, agen				8				16			numbers.
/Eng	H	ave stu	dents dr	aw a nu	ımber li	ne in th	eir jour	nals.			
Aning											
stio	Le	ead stuc	lents to	create a	another	represe	ntation	of the p	roblem	using a	
Que	l - to	Chart (their jo	output/	input),	out com	plete th	e chart.	Have s	tudents	add this	
		NUI	mber of	marble	es		gro	ups			
			8 16)			
			24				2	-			
			32	<u> </u>				, 			
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			•				•				

	M = 1 = 1 + 1 = = = = + + 1 = =		1.1.1.	
	Model the next thi	record them in the	you did the previous	
	and have students		iten journais.	
	Making Groups	Quick Draws	Number Chart	
			Students circle	
			every 8th	
Activities/Tasks/ Strategies/Technology/ Questioning/Engagement/Writing/Checking for Understanding	Now give students that come in group today. You want to the concept buildi example: (student r of objects). He/Sh of people) so that How many will ea In pairs, ask stude strategies from the Walk around the r doing and which s students using too to try another acco Have a class mat Choose a few of the different strategies Have students disc • Making gibecause • The numb because • I thought	a story problem os" idea. Do not to o have students en g strategies. The name) has a buck e wants to share each person rece ch friend get? Ints to solve the p bir journal. oom asking stude trategy they are to much of the sam ording to their ab h meeting: ne students' journs. cuss their similar coups is similar to er line relates to the the the	<pre>using another "things use 3 digit numbers experiment with any of e following is only an eet of(number them with(number ives an equal amount.</pre> oroblem using any two ents what they are using. If you see he, direct student pairs ilities. nals that demonstrate ities and differences. o the number chart egy relates to the e inguistic support for	
		Le	sson Reflection	
Teacher Reflection	Go back to the first	graphic organize	er. Ask students what they sh	ould write under the questions
Evidenced	Have students share	e their favorite co	oncept strategy for division.	
by Student	My favorite concep	t strategy was	because	
Learning/		<i></i>		_
Outcomes				

Teacher Sample: Students' final notes should be similar to below. They fold their notes in half and paste one side into journal page so that it will fold out.



rectangular arrays or	r equal groups
Array Model	
• • • • • • • • • • • • • • • • • • • • • • • • • • • • • • • • • • • • • • • • • Area Model •	
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40	
	Image: 1 2 3 4 5 6 7 8 9 10
0	11 12 13 14 15 16 17 18 19 20
	21 22 23 24 25 26 27 28 29 30
	31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50
	51 52 53 54 55 56 57 58 59 60
Name:	

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Unit: Division	Grade Level/Course	Duration: 60 min					
Lesson # 4	4 th Grade	rade Date:					
Subtraction							
Common Core	4th Grade Operations a	nd Algebraic Thi	nking				
Standards	Gain familiarity with fa	ctors and multiple	es.				
	4. Find all factor pairs for multiple of each of its fac	a whole number in a whole number in a whole number in a second seco	n the range $1-100$. Recognize that a whole number is a bether a given whole number in the range $1-100$ is a				
	multiple of a given one-d	igit number. Deter	mine whether a given whole number in the range 1–				
	100 is prime or composite	e.	_				
	4th Grade Number and	Operations in Ba	se Ten				
	arithmetic.	anding and prope	rices of operations to perior in multi-digit				
	6. Find whole-number qu	otients and remain	ders with up to four-digit dividends and one-digit				
	divisors, using strategies	based on place values	ue, the properties of operations, and/or the relationship				
	rectangular arrays, and/or	area models.	the and explain the calculation by using equations,				
Materials/ Resources/	Mathematical Tools. iou	irnal a box of cou	aters or cubes				
Lesson	Media/Technology to be	e used to deepen le	earning: ST Math Whole Number Multiplication and				
Preparation	Division Module;						
Objectives	Content:		Language:				
, i i i i i i i i i i i i i i i i i i i	Students will be able to se	olve division	Students will explain how they used a strategy to				
	problems using a visual s	roblems using a visual strategies or a solve a division problem with a 3-digit number.					
	number strategy.						
Depth of	Level 1: Recall	Level 2:	Skill/Concept				
Knowledge Level	Level 3: Strategic Thin	king 🛛 Level 4:	Extended Thinking				
Standards for	🛛 1. Make sense of pro	blems and perseve	ere in solving them.				
Mathematical Practice	2. Reason abstractly	and quantitativel	у.				
Tractice	🗌 🗌 3. Construct viable a	rguments and cri	tique the reasoning of others.				
	🛛 4. Model with mathe	matics.					
	🔲 🗆 5. Use appropriate to	ools strategically					
	6. Attend to precision	n.					
	7. Look for and mak	e use of structure					
	│ ─ │ ⊠ 8. Look for and expr	ess regularity in r	epeated reasoning.				
Common Core	Focus on the Standards	5					
Instructional	Coherence within and a	across grade levels					
Shifts in Mathematics	│ ─ │ ⊠ Rigor (Balance of conc	eptual understandi	ng, procedural skill & fluency, and application of skills)				
2 s Z	KEY WORDS ESSENTIAL TO L	JNDERSTANDING	WORDS WORTH KNOWING				
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lemic Dular Tie PROV VLAN			T-Chart				
Acad ocab <u>II &</u> HER I							
V V EACH MPLE							

	STUDENTS FIGURE OUT THE MEANING	Groups of Quick Draws Number line Repeated Subtraction				
Pr Cor	Pre-teaching Considerations Students should be able to relate multiplication and division as inverse operations. Students should also be able to interpret a division expression and form equal groupings.					
-		Lesson Deliver	·y			
	structional Methods	Check method(s) used in the lesson: $\nabla A = A^{2}$				
		⊠ Modeling ⊠ Guided Pi	ractice Collaboration			
		Drien Knowledges Student should be able to relat	iquiry Reflection			
	Lesson Opening	Students should also be able to interpret a division Context and Motivation: "Multiplication and division are different ways to students a tree with the big idea and the ways to re yesterday.) Tell students: Yesterday we made a tree map abore represented in groups. We will call them grouping investigate a number strategy related to division. I answer the following question. Post the question s How is repeated subtraction related to equal groccur? Modeling and Note Taking	n expression and form equal groupings. look at the same problem situation." (Show epresent the big idea which they completed but how multiplication and division can be g and counting strategies. Today we are going to By the end of today's lesson you should be able to so students can read it with you. roups in division? What are the patterns that			
			English Learners:			
ı Continuum	ology/ or Understanding	Begin with empty comparison map. Have students foldable in their journals. They should use at least example in lesson addendums.	s build a concept t two colors. See Pair ELD students who may need support with a note taking partner. Using visuals Working in pairs			
Lesson	sks/ Strategies/Techn tt/Writing/Checking 1		Special Needs: Pair Special Needs students who may need support with a note taking partner. Using visuals Working in pairs			
	vities/Ta ıgagemen	Remember how <u>MULTIPLICATION is repeated</u> the outside of left side fold)	ed addition (write on Accelerated Learners: Challenge accelerated			
	Acti stioning/Er	Let's draw one group of four Draw another group of four to the picture. And And another group. And yet one more group.	d another group. learners to represent their thinking in two to three ways of their choice.			
	Que	$5 \times 4 = 4 + 4 + 4 + 4 + 4 = 20$. (write and draw or side fold)	n the inside of left			

Let's reverse the process. You start out with 20 sticks. Make one group of four. In your mind, "move it away" from the picture. Form another group of four. Again, "move it away" in your mind, or subtract it from the picture. Keep forming groups of four till you have none left. 20 - 4 - 4 - 4 - 4 - 4 = 0(write and draw on the inside of the right side fold) This is repeated subtraction. You subtract 4 repeatedly, or many times, till you hit zero. Each subtraction is forming a group of 4. How many groups did you form? How many times did you subtract? That is the answer to the division problem $20 \div 4$. **Division is repeated subtraction** (write on the outside of their *left side fold*) 84 ÷ 21 = ?? Questioning/Engagement/Writing/Checking for Understanding 84 - 21 1 63 - 21 1 Activities/Tasks/ Strategies/Technology/ 42 - 21 1 21 <u>– 21 1</u> 0 4 Often, it is handier to actually add instead of subtract Since 13 + 13 = 26, 13 goes to 26 two times. So $26 \div 13 = 2$ Since 21 + 21 + 21 + 21 = 84, 21 goes to 84 four times. So $84 \div 21 = 4$ Write a multiplication sentence AND a division sentence that fits the addition/subtraction facts. 23 + 23 + 23 =40 + 40 =-23 - 23 - 23 = 0-40 - 40 = 0Add one more box to your journal page. On the left side: *Multiplication* is repeated addition, and it is like jumps on the number line. 15 5 10 20 25 30



Activities/Tasks/ Strategies/Technology/ Questioning/Engagement/Writing/Checking for Understanding When the 48 cubes have been removed, ask a student how many groups of 8 were removed and record this on the board: 128 + 8 =10 x 8 =80

6 x 8 = 48

Count the total number of groups of 8 removed from the box of 128 and record the answer to the problem $128 \div 8 = 16$.

Present a new problem to your students for them to solve with a partner. Record the new problem on the board or overhead: $212 \div 4 =$ Suppose you had 212 cubes in a box and wanted to see how many groups of 4 cubes you could take out of the box. (If you assembled 212 cubes in a different container, show them to the students.) Work with a partner and figure out how many groups of 4 that would be. When we did the last problem together, I had a way of keeping track of what we were doing. You and your partner should also have some way of keeping track of this problem. Make available any tools students might need to help them solve this problem (cubes, 300 charts, graph paper, paper and pencil). *Included is a 300 Chart; some* dyads may want to experiment with it. Remind students to doublecheck their work. Some ways students may solve 212 + 4 =are shown here.

Questioning/Engagement/Writing/Checking for Understanding Activities/Tasks/ Strategies/Technology/



	 As students are working on this problem, circulate around to different groups and observe the following: Are students using cubes? If so how are they using them? Are they making individual groups of 4, or are they pulling out larger groups, such as 40? How are students keeping track of their work? Are students breaking apart the problem into more familiar problems such as 200 ÷ 4 and 12 ÷ 4? Are they using their knowledge about number relationships—for example, that there are twenty-five 4's in 100 or ten 4's in 40? Are they double-checking their work? Students will vary in their approaches to this problem. While we do want students to use important landmarks and break apart problems, it is most important that students be able to understand what the problem means. Most likely there will be students in your class who will be counting out groups of 4 as a way of solving the problem. Encourage them to start using larger clumps: How many 4's are in 20? In 40? In 100? However, make sure students can really explain what they are doing meaningfully rather than simply copy a strategy you or other students use. Math Meeting As pairs of students finish, they can share their strategy with another pair. When most students have completed the task, bring the group members together to share their strategies. Ask pairs of students who used different approaches to share their work and to show how they kept track of their work.	
	Lesson Reflection	
Teacher Reflection Evidenced by Student Learning/ Outcomes	How is repeated subtraction related to equal groups in division? What are the patterns that occur? What do you understand better? What needs to be clarified for you?	

1	2	3	4	5	6	7	8	٩	10
I	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	<mark>5</mark> 3	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100
101	102	103	104	105	106	107	108	109	10
II	112	113	114	115	116	17	118	119	120
121	122	123	124	125	126	127	128	129	130
131	132	133	134	135	136	137	138	139	140
IHI I	142	143	144	145	146	147	148	149	150
151	152	153	154	155	156	157	158	159	160
161	162	163	164	165	166	167	168	169	170
171	172	173	174	175	176	177	178	179	180
181	182	183	184	185	186	187	188	189	190
ାମ	192	193	194	195	196	197	198	199	200
201	202	203	204	205	206	207	208	209	210
211	212	213	214	215	216	217	218	219	220
221	222	223	224	225	226	227	228	229	230
231	232	233	234	235	236	237	238	239	240
241	242	243	244	245	246	247	248	249	250
251	252	253	254	255	256	257	258	259	260
261	262	263	264	265	266	267	268	269	270
271	272	273	274	275	276	277	278	279	280
281	282	283	284	285	286	287	288	289	290
291	292	293	294	295	296	297	298	299	300

Mutiplication umber DPOTEC Journal Strategies 212:44 = 25 100 + 44 = 25 100 + 44 = 25 12 + 4 = 25 212 = 53 212 = 53 Division repealed Subt



Unit: Division	Grade Level/Course	Duration: 60 min				
Lesson # 5	4 th Grade	Date:				
Menu Activities						
Common Core Standards	4th Grade Operations and Algebraic Thinking Cain familiarity with factors and multiples					
Stanuarus	4. Find all factor pairs for	or a whole number in	n the range $1-100$. Recognize that a whole number is a			
	multiple of each of its fa	ctors. Determine w	hether a given whole number in the range 1–100 is a			
	multiple of a given one-	digit number. Deter	mine whether a given whole number in the range 1–			
	100 is prime or composi	te.				
	4th Grade Number and Use place value unders	I Operations in Ba	se I en			
	arithmetic.	tanding and prope	it ties of operations to perform multi-ungit			
	6. Find whole-number q	uotients and remain	ders with up to four-digit dividends and one-digit			
	divisors, using strategies	based on place val	ue, the properties of operations, and/or the relationship			
	between multiplication a	nd division. Illustra	te and explain the calculation by using equations,			
	rectangular arrays,					
	and/or area models.					
Materials/	Textbook: 4 th Grade Ho	ughton Mifflin Inte	rvention Activities			
Resources/	Mathematical Tools: an	ray cards				
Lesson	Media/Technology to b	e used to deepen le	earning: ST Math Whole Number Multiplication and			
Preparation	Supplementary Materi	als: Menu Activitie	s			
Objectives	Content: Language:					
	Students will be able to solve division Students will explain their thinking while playing					
	problems using a variety	broblems using a variety of strategies. division games.				
Denth of	Level 1. Recall	Level 2.	Skill/Concent			
Knowledge Level	I evel 3: Stratagic Thi	aval 3. Stratagia Thinking MI aval 4. Extanded Thinking				
		5; Strategic 1 minking Devel 4; Extended 1 minking				
Standards for Mathematical	I. Make sense of pro	oblems and perseve	ere in solving them.			
Practice	2. Reason abstractly	y and quantitativel	у.			
	3. Construct viable	arguments and cri	tique the reasoning of others.			
	🛛 4. Model with math	ematics.				
	🔲 5. Use appropriate t	ools strategically				
	6. Attend to precision	on.				
	7. Look for and ma	ke use of structure				
	🔀 8. Look for and exp	ress regularity in r	repeated reasoning.			
Common Core	S Focus on the Standards					
Instructional Shifts in	🛛 Coherence within and	across grade levels				
Mathematics	☐ Rigor (Balance of conceptual understanding, procedural skill & fluency, and application of skills)					
ON ES D	KEY WORDS ESSENTIAL TO	UNDERSTANDING	WORDS WORTH KNOWING			
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	STUDENTS FIGURE OUT THE MEANING					
Pr Cor	e-teaching isideration	s Students should be able to relate multiplication and division as inversions should also be able to interpret a division expression and form equal a	e operations. Students groupings.			
		Lesson Delivery				
In	structional	Check method(s) used in the lesson:				
	Methods	⊠ Modeling □ Guided Practice ⊠ Collab	boration			
		☐ Independent Practice ☐ Guided Inquiry ☐ Reflec	etion			
	Lesson Opening	 Prior Knowledge: Student should be able to relate multiplication and division as inverse operation Students should also be able to interpret a division expression and form equal groupings. Context and Motivation: To the Teacher: The following activities are provided so that students have independent opportunities to practice multiplication and division, while the teacher has opportunity to meet w students who are struggling. 				
		Students work on the Menu Activities, while the teacher works with	Differentiated Instruction:			
unnu	ology/ or Understanding	The following are Menu Activities : Multiplication Pairs Count and Compare Small Array/Big Array 100 Hungry Ants: Students work individually or with a partner to explore how to group other numbers of ants. Beread the story or	English Learners: Interventions given in body of lesson. Special Needs:			
Lesson Contin s/ Strategies/Techno Writing/Checking fo		have a class discussion in which the students retell what happened. Have students figure out how many ants were in each line whenever the ants regrouped. Show the students how rectangular arrays connect to division by using division symbolism to record how to represent each way the ants regrouped.	of lesson.			
	vities/Tas gagement	In students math journals students should keep a record of Menu Activities that they complete.	Accelerated Learners: Activity choices given in body of lesson.			
	Activ Questioning/En	Intervention Activities from Houghton Mifflin Strategic Intervention Book: Groupings pp. 37- 38, 43-44 (for students who are struggling with making equal groups) Inverse Operations pp. 45 (for students who are struggling with making a connection between multiplication and division)				

	Benchmark Intervention Book:Model Division p. 56 (for students who are struggling with showing their work using base ten blocks)English Learners Resources Book:Using Language and Solving Word Problems pp. 80-82 (for Beginning and Early Intermediate English Language Learners)Can be either Teacher Directed or students can listen to the CD and complete the activities in small groups or pairs
	Call students together to debrief the Menu Activities Session. Ask students: What challenges did you find while working? Is there a learning pair who wants to share how well they worked together? Why? Which activities did you complete? How did the activity help you?
	Lesson Reflection
Teacher Reflection Evidenced by Student Learning/ Outcomes	

Starting Menu Activities

If you set up your choices at stations, list the materials students will find at each station. Students can keep track of their choices on their own choice lists.

Choice 1: Array Game: Multiplication Pairs: directions; Array Cards, Sets A and B (1 set per pair) Choice 2: Array Game: Count and Compare: directions; Array Cards, Sets A and B (1 per pair) Choice 3: Array Game: Small Array/Big Array: directions; Array Cards, Sets A and B (1 set per pair) Choice 4: Hungry Ants: directions; paper to record (1 per pair)

Make copies of game directions available or simply post each sheet. Students may refer to the directions when in doubt about the rules of the game. Students may choose to play using only the Array Cards in Set A, which consists of multiplication pairs with products up to 50. Then when they feel comfortable, students may include Array Cards from Set B.

Choice 1: Array Game: Multiplication Pairs

Given the dimensions of an array, students are to find the total number of squares in the array; given the total, students are to find the dimensions. As they play, students write the multiplication pairs and relationships they know and don't know on a sheet of paper.

Choice 2: Array Game: Count and Compare

Students use multiplication relationships to find the sizes of students' array cards and then determine the largest.

Choice 3: Array Game: Small Array/Big Array

Students use their array cards to make "matches" between a large array and two or more smaller arrays. Each student should write their "matches" on a sheet of paper using mathematical statements.

Choice 4: Hungry Ants:

Students explore how to group other numbers of ants.

During Choice Time, circulate among the groups and observe students as they are involved with an activity, or use the time to meet with small groups of students who are having difficulty with a particular activity. Some things you might look for are the following:

- How are students making decisions about choosing an activity and organizing their time and materials?
- Are there too many or not enough activities going on at once?
- Are students keeping track of the choices they have completed?
- How are students figuring out the total number of squares in arrays? Are they counting one by one? Counting by groups? Do they know the multiplication pairs?
- Do some students need to spend more time counting by 2s, 3s, and 6s?

Are some students ready to add the next set of arrays (Set B) to their existing set?

How to Play Multiplication Pairs

Materials

- Set of array cards
- Paper and pencil

Players: 1, 2, or 3

How to Play

- 1. Spread out all the array cards in front of you. Some should be turned up, showing the dimensions. Others should be turned over to show the total.
- 2. Choose an array card and put your finger on it. (Don't pick it up until you say the answer.) If the dimensions are showing, you must give the total. If the total is showing, you must say the dimensions of the grid. The shape of the array will help you!

For example: Suppose you pick an array with total 36 showing. The dimensions could be 6×6 , or 9×4 , or 12×3 . You must decide which is right. The shape of the array is a good clue.

- 3. Turn the card over to check your answer. If your answer is correct, then pick up the card.
- 4. If you are playing with a partner, take turns choosing and identifying cards. Play until you have picked up all the cards.

While you are playing, make lists for yourself of "pairs that I know" and "pairs that I don't know yet." Keep these lists in your math folder.

How to Play Count and Compare

Materials: Set of array cards

Players: 2 or 3

How to Play

- 1. If you are playing with a partner, sit across from each other. If three people are playing, sit in a circle.
- 2. Deal out the array cards with the total sides face down. Players should all have the same number of cards. Set aside any that are left over.
- 3. Place your cards in a stack in front of you, with the total side face down.
- 4. Players take the top card from their stacks and place these cards side by side (total sides still face down).
- 5. Decide which array is largest. You can do this just by looking, or by skip counting by rows to find the total of each. Counting the squares by 1's is not allowed.
- 6. The player with the largest array takes the cards, after proving that it is the largest.
- 7. Sometimes arrays of the same size may be played in one turn—like this:





When this happens, the players decide together who will get the cards. Once a rule is decided, it cannot be changed until the game is over.

8. The game is over when time is up or one player runs out of cards.

How to Play Small Array/Big Array

Materials: Set of array cards

Players: 2

How to Play

- 1. Deal out 10 array cards to each player with the dimensions side up. Spread out the cards in front of you.
- 2. Spread out 6 more cards, dimensions side up, in the center of the table. Place the remaining cards in a deck in the center of the table.
- 3. The goal is to make a "match" by covering a big array with two or three smaller arrays. Players take turns.
- 4. From your smaller arrays, choose one that matches one dimension of a big array in the center of the table.
- 5. If none of your array cards matches, you can choose a card that matches a dimension of the big array from the center of the table. Or you can pick the top card from the deck and play it if you can.
- 6. If you use an array from the center of the table to cover another array, you can either replace it with a card from the deck, or discard one of your array cards. There should always be 6 cards in the middle.
- 7. When you cover a big array, you can collect the "match." While playing, keep a list of the dimensions of the large array and the smaller arrays:

 $7 \times 6 = 3 \times 6 + 4 \times 6$ 42 = 18 + 24

8. If you run out of cards, take 4 cards from the deck. The game is over when there are no more cards or no more matches can be made.

Hungry Ants

1. Figure out what would happen if 20 ants tried to group themselves into 1 line, 2 lines, 3 lines, and so on up to 10 lines. How many ants would be in each line?

Record your answers like this:

20 Hungry Ants

1	line of
2	lines of
3	lines of
4	lines of
5	lines of
6	lines of
7	lines of
8	lines of
9	lines of
0	lines of

2. Choose another number of ants and do the activity again.

I

Unit: Division Lesson # 6 Equal Sharing Equal Groups Common Core Standards	Grade Level/Course 4 th Grade 4th Grade Number and Use place value underst arithmetic. 6. Find whole-number qu divisors, using strategies between multiplication a rectangular arrays, and/or area models.	Duration: 60 min. Date: d Operations in Base Ten standing and properties of operations to perform multi-digit quotients and remainders with up to four-digit dividends and one-digit s based on place value, the properties of operations, and/or the relationship and division. Illustrate and explain the calculation by using equations,				
Materials/ Resources/ Lesson Preparation	Mathematical Tools: cc Media/Technology to b Division Module	e used to deepen le	earning: ST Math Whole Number Multiplication and			
Objectives	Content: Students will be able to a partitive (known number quotative (known number division using cubes or t Students will create mod problem type.	b demonstrate Language: b demonstrate Students compare the processes of equal sharing and equal groups in division and create examples of each b demonstrate problem type. c tiles. problem type.				
Depth of Knowledge Level	☐ Level 1: Recall ☑ Level 3: Strategic Thin	⊠ Level 2: nking ⊠Level 4:	Skill/Concept Extended Thinking			
Standards for Mathematical Practice I. Make sense of problems and persevere in solving them. Image: Pro						
Common Core Instructional Shifts in Mathematics	 ☑ Focus on the Standard ☑ Coherence within and ☑ Rigor (Balance of condition) 	ls across grade levels ceptual understandii	ng, procedural skill & fluency, and application of skills)			
Academic Vocabulary teacher provides simple explanation	KEY WORDS ESSENTIAL TO	UNDERSTANDING	WORDS WORTH KNOWING			

	ЭH.	Equal sharing						
		Equal groups						
	STU URE							
	EIG .							
Pr	·e-teaching							
Сог	nsideration	S Students should have concept of equal groups, meaning of conventional notation (4 x 6 to						
		designate 4 groups of 6)						
		Lesson Delivery						
In	structional	Check method(s) used in the lesson:						
	Methods	□ Modeling						
		⊠ Independent Practice □ Guided Inquiry ⊠ Reflection						
	Lesson	Prior Knowledge: Students should have concept of equal groups, meaning of conventional notation						
	Opening	(4 x 6 to designate 4 groups of 6)						
		Context, and Motivation:						
		Today's big idea is "Multiplication and division are different ways to look at the same problem						
		situation.'						
		rouns. Let's consider these two problems:						
		groups. Let's consider these two problems.						
		"I have 18 balloons for my party. After the party is over, I am going to divide them evenly between						
		my sister and me. How many balloons will each of us get?"						
mn		"I have 18 balloons for my party. After the party is over, I am going to tie them together in bunches						
ıtinu		of two to give to my friends. How many bunches can I make?"						
n Con		Using counters, represent each of these problem situations. How do they "look" different?						
essol		Each of these problems is a division situation—a quantity is broken up into equal groups. Although we begin with the same number of balloons, and the notation for each problem is the same $(18 \div 2 =$						
Γ		we begin with the same number of balloons, and the notation for each problem is the same $(18 \div 2 = 9)$ the problem situation is really quite different. In the first situation, you know the number of						
		groups—2. Your question is "How many balloons will be in each group?" In the second situation,						
		you know that you want 2 balloons in each group, and your question is, "How many groups will there						
		be?" In each case you divide the balloons into equal groups, but the results of your actions look						
		different.						
		In the first case, the balloons are passed out, one at a time to the two children, until they are all gone.						
		In the second case, the balloons are given in pairs to as many children as possible. We could say, "						
		Divide 18 into two groups. How many are in each group?" or "How many 2s are in 18?" We will call						
		the first problem type equal sharing, and the second problem type equal groups.						

			Differentiated Instruction:
		<u>Guided Practice</u> Now study these problems. Make a visual representation of each problem in your math journal, and determine if the problem situation is asking for equal sharing (known number of groups) or equal groups (known number in each group). Students are given choices of numbers to use for each problem, depending on their abilities.	English Learners: Using sentence frames Using visuals Working in pairs
A	Activities/1asks/ Strategies/1echnology/ Questioning/Engagement/Writing/Checking for Understanding	 Peter has 96 (54, 36) photos to place in his photo album. He can fit six photos on each page. How many pages will he need for all of his photos? Galen uses 120 (56, 32) ounces of toothpaste in 8 months. How many ounces of toothpaste did he use each month? Mara's dessert contained 425 (300, 125) calories. She ate five items, and each contained the same number of calories. How many calories are in each item? The elementary school just received 76 (63, 42) reams of paper to divide evenly among the teachers. Each teacher will receive 3 reams of paper. How many teachers work at the school? Monitor students as they work. Make note of student work that is representative of many students' thinking, and work that can push the thinking of the group forward. Strategically sequence student sharing to maximize the impact. A general rule is to begin with students who have the most concrete model, and proceed to those who use a more abstract representation of the problem. Call students together to debrief answers and depictions of problem situations. Focus on bringing out the concepts of equal sharing (known number of groups) and equal groups (known number in each group). Now ask students to work in pairs to create one word problem of each type. Write the problems on index cards. Gather the index cards and pass them out to different students. Students can act out each others' problems. 	Special Needs: Working in pairs Modifying numbers given Using sentence frames Accelerated Learners: Creativity in creating story problems of own interests and difficulty level
		Lesson Reflection	
Teacher Reflection Evidenced by Student Learning/ Outcomes		How do we know whether a division problem is asking for equal shares Why does it matter?	or equal groups?

Unit: I	Division	Grade Level/Course	Course Duration: 60 min.				
Lesson	n # 7	4 th Grade	Date:				
Fair	Shares	4th Crade Number and Operations in Base Ten					
Star	ndards	Use place value understanding and properties of operations to perform multi-digit					
		arithmetic.					
		6. Find whole-number quotients and remainders with up to four-digit dividends and one-digit					
		divisors, using strategies based on place value, the properties of operations, and/or the relation between multiplication and division. Illustrate and explain the calculation by using equations					
		rectangular arrays, and/o	or area models.				
Mat Res	terials/ ources/	Mathematical Tools: ci	ubes, counters, math	iournals, graph paper, calculators, box of 12 pencils			
Le	esson	Media/Technology to b	e used to deepen le	earning: ST Math Whole Number Multiplication and			
Prep	aration	Division Module					
Ohi	iectives	Content:		Language:			
0.01		Students will be able t	o apply	Students describe situations in which equal			
		partitioning (known nu	umber of groups)	sharing or equal groupings are more appropriate.			
		and sharing (known nu	umber in each				
		group) division to real life problem					
		situations.					
De	pth of	Level 1: Recall	🛛 Level 2:	Skill/Concept			
Knowle	edge Level	Level 3: Strategic Thinking 🛛 Level 4: Extended Thinking					
Stand	lards for	□ 1. Make sense of problems and persevere in solving them.					
Math	ematical	\square 2. Reason abstractly and quantitatively.					
Pr	actice	\Box 3. Construct viable arguments and critique the reasoning of others.					
		\boxtimes 4. Model with mathematics.					
		5. Use appropriate tools strategically					
		□ 6. Attend to precision.					
		7. Look for and make use of structure.					
		8. Look for and express regularity in repeated reasoning.					
Comn	non Core	Focus on the Standards					
Instr	ructional	Coherence within and across grade levels					
Shifts in Mathematics		Rigor (Balance of conceptual understanding, procedural skill & fluency, and application of skills)					
	sz	KEY WORDS ESSENTIAL TO	UNDERSTANDING	WORDS WORTH KNOWING			
r.	PRO	Equation					
- III	HER EXF						
ocał Tier	EACI						
ic V I &		D					
lem er I	S THE	Dozen		Раскаде			
Acat (Ti							
Ł	TUD IRE (IEAI						
	S. FIGU						

Pre-teaching			Students should have the concept of packages containing equal amounts.							
Соі	Considerations		12 is the same as one dozen.							
			Lesson Delivery							
In	structional	l	Check method(s) used in the lesson:							
Methods		☐ Modeling		Collaboration						
			🗌 Independent Practice 🛛 🖾 Guided Inquiry 🖂 Reflect		ction					
Lesson Continuum	Lesson Opening	Pr 12 Co sit To sit To or wo Sh Th Sh Th Sh Th Sh Th Sh Th Sh Th Sh Sh Th Sh Sh Sh Th Sh Sh Sh Sh Sh Sh Sh Sh Sh Sh Sh Sh Sh	 ior Knowledge: Students shoul is the same as one dozen. ontext and Motivation: oday's big idea is "Multiplication nution." oday we will investigate the big if der pencils, and we will need to a decide how many pencils that if now a box of pencils to the class. nat's right, one dozen." 1. How many packages woul 2. How many packages woul 3. How many packages woul 3. How many packages woul a. How many packages woul b. How many packages woul c. In deciding how many per passing out the pencils to a thinking about giving a ce student? c. How many pencils would received one pencil? How c. How many students may the solutions to these prob 	d have the concept of pack n and division are different idea by exploring a real lif order enough so that every might be? . "Pencils come in package d we have to order to give d we have to order to give bes, or independently to ey must write an equation to d it. They can use words o bes, graph paper, or calcul be available to them. Remi sing numbers in some way olication or division to sho ated into the work of some heils to order, are we think each student one-by-one, o rtain number of pencils to we need if each student or many packages of 12 is th the number of pencils need at is equal to that many pe be in one class? 20? 24? 30 altiplication to division to do lems?	cages conta t ways to lo e problem f yone in the es of 12. Wi e 2 pencils t e 4 pencils t e 6 pencils t complete for each r pictures ators. nd all y. w their e students. ing about or are we each aly hat? led and encils? 0? 36? express	 ining equal amounts. ok at the same problem for our class. It is time to class has six pencils. How can hat is another way to say 12? o each student in our class? Differentiated Instruction: English Learners: Using sentence frames Using counters Working in pairs or small groups Using sentence frames Using sentence frames Using counters Using sentence frames Using modified numbers of students 				

Activities/Tasks/ Strategies/Technology/ Questioning/Engagement/Writing/Checking for Understanding	 Monitor students as they work, and observe the following: What tools are students using to help them solve the problems? How do students keep track of the steps in each problem? Are students able to recognize a problem as a multiplication or division situation? How do students use multiplication or division notation to record their work? Do students deal with remainders sensibly as they answer the questions? Bring about a discussion of the various strategies used to solve this series of problems. Perhaps some students began with one strategy, then switched to another, as the problem got more complex. Perhaps some students noticed that six pencils is equal to one half dozen. In this scenario, it would be an easy stretch to also notice that two students could share one package of 12 pencils. Is there an even or odd number of students in the class? Does this affect the strategies used? Call attention to the types of tools students used to assist them in their work. Compare organizational results from using graph paper to lined or unlined paper. Ask those using cubes or counters to explain how these tools helped their thinking process. Look for students who utilized tally marks, or other methods to keep track of packages of pencils. Highlight students who created a function table or T-chart. Possible solution: 30 students need six pencils and we gave six pencils to each student in the class, we must have 30 students." 180 + 6 = 30. If we divide the pencils into groups of 12, we would see that 180 pencils is equal to 15 dozen. 180 ÷ 12 = 15 Quick write: How could you show the following story using either multiplication or division? "I bought a box of treats for my dog. The box contained 24 treats. I give my dog a treat 3 times a day. How many days will the box of treats last?" 	Accelerated Learners: Using invented algorithms Finding multiple solution strategies Investigating different sized classes, and varying numbers of pencils for each student
Teacher	Lesson Reflection	
Reflection Evidenced by Student Learning/ Outcomes	How does the mathematics change with different numbers of students in Is it easier with 20 students or 24? With 30 or 36? What quantity of pencils is easier to work with? How does our thinking change as we give each student more pencils? Is it easier with 4 pencils or with 6?	the class?

Unit: I Lesson U Rem	Division 1 # 8 Using nainders	Grade Level/Course 4 th Grade	Duration: 60 min. Date:					
Comn Star	non Core ndards	 4th Grade Number and Use place value unders arithmetic. 6. Find whole-number q divisors, using strategies between multiplication a rectangular arrays, and/or 	th Grade Number and Operations in Base Ten Use place value understanding and properties of operations to perform multi-digit arithmetic. b. Find whole-number quotients and remainders with up to four-digit dividends and one-digit livisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, ectangular arrays, and/or area models.					
Ma Rese Lo Prep	terials/ ources/ esson paration	Mathematical Tools: cubes, counters, math journals, graph paper, calculators, array cardsMedia/Technology to be used to deepen learning: ST Math Whole Number Multiplication andDivision ModuleSupplementary Materials: Arrays and Shares, TERC						
Obj	jectives	Content: Students will be able to most appropriate use of division problem situation	cent:Language:ents will be able to determine the t appropriate use of the remainder in sion problem situations.Language: Students will explain how they dealt with the leftovers in a division problem situation.					
Depth of Level 1: Recall Level 2: Skill/Concept Knowledge Level Level 3: Strategic Thinking Level 4: Extended The strategic Thinking				Skill/Concept Extended Thinking				
Standards for Mathematical Practice		 □ 1. Make sense of problems and persevere in solving them. □ 2. Reason abstractly and quantitatively. □ 3. Construct viable arguments and critique the reasoning of others. □ 4. Model with mathematics. □ 5. Use appropriate tools strategically □ 6. Attend to precision. □ 7. Look for and make use of structure. □ 8. Look for and express regularity in repeated reasoning. 						
Comn Instr Sh Matl	non Core ructional lifts in hematics	 ☑ Focus on the Standards ☑ Coherence within and across grade levels ☑ Pigor (Balance of concentual understanding, proceedural skill & fluoney, and application of skille) 						
Vocabulary & Tier III)	TEACHER PROVIDES SIMPLE EXPLANATION	KEY WORDS ESSENTIAL TO	UNDERSTANDING	WORDS WORTH KNOWING				
Academic (Tier II &	STUDENTS FIGURE OUT THE MEANING	Remainder						
Pre-teaching Students should have knowledge of arrays and equal groups.				d equal groups.				

Lesson Delivery							
Instructional Mothodo		Check method(s) used in the lesson:					
Methods		🖾 Modeling	Guided Practice	🔀 Collaboration			
		Independent Practice	🛛 Guided Inquiry	Reflection			
	Lesson Opening	Prior Knowledge: Students should have knowledge of arrays and equal groups. Context and Motivation: Today's big idea is "How the remainder is explained depends on the problem situation. Today we will investigate the big idea through real life situations you may encounter. Let's look at our array cards. Find the cards that show 36 squares." Write $36 \div 4$ on the board. "Here is a division problem. How do you read this? Which array would help you solve it?" Can you think of a problem situation that you could write as $36 \div 4$?" Students may think of a division problem that involves sharing ("There are 36 marbles being shared by four friends. How many marbles will each friend get?") and division problems that involve grouping or measuring ("There are 36 marbles. I'm going to put four marbles in each bag. How many bags will I need?"). Chart several student responses as they are given.					
		Ν	Iodeling	Differentiated Instruction	1:		
Lesson Continuum	Activities/Tasks/ Strategies/Technology/ Questioning/Engagement/Writing/Checking for Understanding	Introduce the formal division si "This division notation is read a 36 ÷ 4. The total that is being d number, whereas when we use first." "How would you use your calcu keys would you use? Which nu Give students a minute to explo	gn 4 $\overline{)36}$ as thirty-six divided by four, ivided shows up here as the s the \div the total being divided alator to solve this problem? mber would you put in first?	just like second comes Which m share Special Needs:	11		
		their strategies and solutions. <u>Guid</u> "What is another way we can d your arrays for ideas. What is a that involves dividing 36?" Allow students a few minutes w problems that start with the tota instructions:	ded Inquiry ivide 36 into equal groups? I nother problem situation we vorking in pairs to generate d 1 of 36. Give the following	Look at can use division	11		
		 Write down each proble 36 children who are go races. How many child: Write down the division and ÷. Give the solution to each As students are working, monit students are comfortable creating understand the correspondence written notation. Help students asked. 36 ÷ 9 can be read as "30 situation, or "how many 9s are 	em situation. (For example, ' ing to divide up into 6 teams ren will be on each team?") n notation for that problem u ch problem using both) or their progress, observing v ng division problems, and wh between the problem situation to read the notation correctly 6 divided into 9 groups" in a in 36?" in a partitioning situation	"There are a for relayAccelerated Learners: Using invented algorithm Finding multiple solution strategies Using creativity to exprese and ÷.and ÷.Using creativity to exprese the remainders in each situationwhether hether they on and the y when sharing ation.Image: Comparison of the second s	ns n ess		

	nology/ for Understanding	Ask some students to present their problems. Others can demonstrate how to express the problems using standard notation, or how they reached their solutions. Write 36 ÷ 5 on the board. Ask students to look at the problem. "What is a situation where we might have 36 divided by 5?" List student responses on the board. Then use students' situations to illustrate the problem. Discuss with the students how you would find the solution to 36 ÷ 5, and what would happen with the extra. Students may wish to express this extra as a fraction, a decimal, a remainder, or leftover amount. "Now we are going to solve a set of division problems where you cannot divide the total evenly. Your task is to decide what to do with the leftovers. Write down your reasoning and a solution for each problem. You may use any of your mathematical tools to help you." Give students the following problems to solve in pairs or small				
	rech king	groups:				
	gies/ Chec	1. There are 36 people who are taking a trip in some small vans. Each van holds 8 people. How many vans will they need?				
	rate; ing/	2. Eight people are going to share 36 crackers equally. How				
	s/ St Writ	3. Eight people are going to share 36 balloons equally. How				
	[ask ent/	many balloons will each people get?				
	ies/_ igem	4. 36 students are going to see a movie together. Each row holds 8 people. How many rows will they fill up?				
	Activit ning/Enga	5. Eight friends raised \$36 by washing people's cars. They want to share the money equally. How much money should each person get?				
	Questio	Math Meeting				
	0	Gather the students together to discuss their solutions to the division problems. Invite some students to share their solution strategies and				
		how they expressed the remainder. Possible solutions: (Van problem) "There are 4 full vans with 4 people				
		left. You would need 5 vans to take all the people."				
		(Cracker problem) "Each person will get 4 crackers. Keep 4 crackers for another day." Or "Each person will get 4 ¹ / ₂ crackers."				
		(Theater problem) "32 people will fit in 4 rows. 4 people will have to sit in the fifth row." Or "You fill up 4 rows and half of another row."				
Lesson Reflection						
Teacher Reflection Evidenced by Student Learning/ Outcomes		How is the remainder expressed differently in each of these problem situations? How does the situation determine what you can do with the remainder?				
Unit: I	Division	Grade Level/Course	Duration: 60 min			
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Lesson	1 # 9	4 th Grade Date:				
More Rem	e Using					
Comn	ion Core	4th Grade Number and Operations in Base Ten				
Star	ndards	Use place value unders	tanding and prope	rties of operations to perform multi-digit		
		arithmetic.				
		6. Find whole-number qu	uotients and remain	ders with up to four-digit dividends and one-digit		
		between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.				
Mat	terials/	Mathematical Tools: cu	ibes, counters, math	journals, graph paper, calculators, array cards		
Res	ources/	Media/Technology to b	e used to deepen le	earning: ST Math Whole Number Multiplication and		
	esson	Division Module				
Prep	aration	school library.	als : A Remainder o	<i>f One</i> , by Pinczes, E.; Check out book from your		
Obi	ectives	Content:		Language:		
3		Students will be able to a	determine the	Students will explain how they dealt with the		
		most appropriate use of t	the remainder in	leftovers in a division problem situation.		
		division problem situation	ons.			
Depth of		Level 1: Recall Z Level 2: Skill/Concept				
Knowle	edge Level	⊠ Level 3: Strategic Thinking ⊠Level 4: Extended Thinking				
Stand	lards for	⊠ 1. Make sense of problems and persevere in solving them.				
Math Pr	ematical actice	2. Reason abstractly and quantitatively.				
110	actice	☐ 3. Construct viable arguments and critique the reasoning of others.				
		⊠ 4. Model with mathematics.				
		☐ 5. Use appropriate tools strategically				
		☐ 6. Attend to precision.				
		☐ 7. Look for and make use of structure.				
		8. Look for and express regularity in repeated reasoning.				
Comn	non Core	Secus on the Standards				
Instructional Shifts in		Coherence within and across grade levels				
Mathematics		🖾 Rigor (Balance of conceptual understanding, procedural skill & fluency, and application of skills)				
	IPLE	KEY WORDS ESSENTIAL TO	UNDERSTANDING	WORDS WORTH KNOWING		
, c		Ouotient				
mi		Solution				
ade abı	ANA	Expression				
Ac: 70c:	ER PI					
	ACHE					
	TE/					

	S THE		
	STUD URE		
Pr Coi	e-teaching nsideration	Students should have knowledge of equal groups and formal	division notation.
		Lesson Delivery	
In	structional Mothoda	Check method(s) used in the lesson:	
	Methods	☐ Modeling	Collaboration
		☐ Independent Practice ⊠ Guided Inquiry	Reflection
	Lesson	Prior Knowledge: Students should have knowledge of equal g	roups and formal division notation.
	Opening	Context and Motivation: Today's big idea is "How the remainder is explained depends	s on the problem situation. We are going
		to start today's lesson by reading a story about a very smart b	bug, and how he solved a problem with
		remainders."	
		Read, A Remainder of One.	
		<u>Guided Inquiry</u> "Voctorday we investigated many problem situations that app	Differentiated Instruction:
		solved by dividing 36 by 8. However, in each situation, the re-	emainder English Learners:
		had a different meaning. We are going to continue this type o	f
		investigation today. We will be looking at the same problem with different questions and different solutions "	situation
	ng	Chart the division expressions, the questions, and the solution	ns for Special Needs:
	erstandi	each of the following problems:	
		taken. She has 79 postcards that she wants to place into an all	bum. She
m	unc	can place seven postcards on each page. How many pages wi	ll she
inui	nolc for	need for all the postcards to fit? What is the division expression we will use to solve this prob	lem?
Ont	cch cing	$(79 \div 7)$	Accelerated Learners:
on (les/T	What is the question? (How many pages will she need?)	
esse	itegi ig/C	What is the solution? (12 pages) Mrs. Ross plans to divide her 79 postcards equally among sev	ven
Τ	Stre	children. She will keep the extras. How many postcards will l	Mrs.
	sks/ nt/W	Ross keep? What is the division expression we will use to solve this prob	Jam2
	s/Ta mer	$(79 \div 7)$	
	vitie gage	What is the question? (How many postcards will Mrs. Ross k	eep?)
	Activ /Eng	What is the solution? (2 postcards) Mrs. Ross put her postcards on display at the local library for	79 days
	 ning	How many full weeks is that?	
	stio	What is the division expression we will use to solve this prob $(79 \div 7)$	lem?
	Que	What is the question? (How many full weeks is that?)	
		What is the solution? (11 weeks)	
		"Hmmm! How could we have three such different answers to	each of
		these problems when the division expression is the same each	n time?
		I alk with your elbow partner about what you think is the reas the different answers."	son for

Activities/Tasks/ Strategies/Technology/ Questioning/Engagement/Writing/Checking for Understanding	 "Now we are going to solve several problem situations. I want you to think very carefully about what the question is for each problem, and how you should best express the solution for that problem. We will have a discussion after you have finished, and I want you all to be prepared to defend your answers. You may use any of your mathematical tools that you think would help your thinking." 1. Mrs. Webster wants to buy 68 postcards. They come in packages of 6. How many packages does Mrs. Webster need to buy? 2. Mr. Seng has \$71 to buy postcards. Each package costs \$6. How much money does he have left after buying as many packages as he can? 3. Suzanne is placing postcards into a scrapbook. She places three postcards on each page. On which page will she place postcard number 95? As students are working, circulate through the classroom, taking notes on strategies you see students using. Select students that are using strategies that are representational of many other students' work, and students that are using innovative strategies that will push others forward in their thinking. Sequence students in a way that each student's work builds upon the previous student's work. (i.e., look for students that have drawn a picture, and another that has made a table using the same numbers.)
	Lesson Reflection
Teacher Reflection Evidenced by Student Learning/ Outcomes	How is the remainder expressed differently in each of these problem situations? How does the situation determine what you can do with the remainder?

Unit: D	Division	Grade Level/Course	Duration: 60 min			
Lesson	# 10 Activities	4 th Grade	Date:			
Comm	ion Core	4th Grade Operations and Algebraic Thinking				
Stan	ıdards	Gain familiarity with factors and multiples.				
		4. Find all factor pairs for a whole number in the range $1-100$. Recognize that a whole number is a				
		multiple of each of its factors. Determine whether a given whole number in the range $1-100$ is a multiple of a given one-digit number. Determine whether a given whole number in the range 1				
		100 is prime or composite.				
		4th Grade Number and	l Operations in Ba	se Ten		
		Use place value unders	tanding and prope	rties of operations to perform multi-digit		
		6. Find whole-number q	uotients and remain	ders with up to four-digit dividends and one-digit		
		divisors, using strategies	based on place value	ue, the properties of operations, and/or the relationship		
		between multiplication a	ind division. Illustra	te and explain the calculation by using equations,		
		lectangular arrays, and/c	area models.			
Mat	erials/					
Reso	ources/	Textbook: 4" Grade Ho Mathematical Tools: at	ughton Mifflin Inte	rvention Activities		
Prepa	aration	Media/Technology to b	e used to deepen le	earning: ST Math Whole Number Multiplication and		
		Division Module				
		Supplementary Materi p. 298C. Chapter 15 Ma	als: Menu Activities	s; Houghton Mifflin Chapter 14 Math Centers,		
		p. 2960, Chapter 19 Wa	th centers p. 524c			
Objectives		Content:	a la a dia ini a a	Language:		
		problems using visual ar	nd numerically	division games		
		strategies.				
Denth of Level 1: Recall I level 2: Skill/Concent		Skill/Concept				
Knowledge Level A: Extended Thinking			Extended Thinking			
Stand	ards for	\square 1. Make sense of problems and persevere in solving them.				
Mathe	ematical	\square 2. Reason abstractly and quantitatively.				
Pra	actice	☐ 3. Construct viable arguments and critique the reasoning of others.				
		\boxtimes 4. Model with mathematics.				
		\square 5. Use appropriate tools strategically				
		\square 6 Attend to precision				
		\square 7 Look for and make use of structure				
		\sim 7. Look for and avarass regularity in repeated reasoning				
Comm	on Coro	Constant express regularity in repeated reasoning.				
Instru	uctional	□ rocus on the Standards				
Shifts in		☐ Coherence within and across grade levels				
Math		Rigor (Balance of con	ceptual understandi	ig, procedural skill & fluency, and application of skills)		
	DES	KEY WORDS ESSENTIAL TO	UNDERSTANDING			
mic	ANA					
ade abı	ER PI EXPL					
Ac Voc	ACHI PLE I					
-	JIM SIM					

	STUDENTS GURE OUT THE					
Pre-teaching Consideration		s Students should be able to relate multiplication and division as inversion also be able to interpret a division expression and form equal grouping	se operations. Students should ngs.			
		Lesson Delivery				
In	structional Methods	Check method(s) used in the lesson:				
	wiethous	☑ Modeling □ Guided Practice ☑ Collai	boration			
		Independent Practice Guided Inquiry Reflect	ction			
	Lesson Opening	Prior Knowledge: Students should be able to relate multiplication and division as inverse perations. Students should also be able to interpret a division expression and form equal groupings. Context and Motivation: To the Teacher: The following activities are provided so that students have independent poportunities to practice multiplication and division, while the teacher has the opportunity to meet with students who are struggling.				
		Students work on the Menu Activities, while the teacher works with	Differentiated Instruction:			
	chnology/ ng for Understanding	small group of students. Students could choose from Menu Activities 1-4, however teach students new activities.	English Learners:			
ontinuum		The following are Menu Activities : The Game of Leftovers In students math journals students should keep a record of Menu Activities that they complete.	Special Needs:			
Lesson Co ities/Tasks/ Strategies/Te agement/Writing/Checki	vities/Tasks/ Strategies/T gagement/Writing/Check	Intervention Activities from Houghton Mifflin Strategic Intervention Book: Inverse Operations: NS 24-28; NS 41 Remainders: NS 40, NS 42 Benchmark Intervention Book: Remainders: pp. 30, 57-58, 60 Problem Solving: p. 31	Accelerated Learners:			
	Acti Questioning/En	English Learners Resources Book : Using Language and Solving Word Problems pp. 103-106 (for Beginning and Early Intermediate English Language Learners) Can be either Teacher Directed or students can listen to the CD and complete the activities in small groups or pairs.				
Т	aachar	Call students together to debrief the Menu Activities Session				
Teacher Reflection Evidenced by Student Learning/ Outcomes		Ask students: What challenges did you find while working? Is there a learning pair who wants to share how well they worked togeth Which activities did you complete? How did the activity help you?	ner? Why?			

The Game of Leftovers

You need: A partner One die 15 Color Tiles One cup to hold the tiles Six paper plates or 3-inch paper squares ("plates")

- 1. Take turns. On your turn, roll the die, take that number of paper plates or squares, and divide the tiles among them. Keep any leftover tiles.
- 2. Both players record the math sentence that describes what happened.

For example: $15 \div 4 = 3$ R3

In front of each sentence write the initial of the person who rolled the die.

- 3. Return the tiles on the plates to the cup before the next player takes a turn.
- 4. Play until all the tiles are gone. Then figure your scores by counting how many tiles each of you has. The winner is the player with the most leftovers. Add your scores to make sure that they total the 15 tiles you started with.
- 5. When you finish a game, look at each of your sentences with a remainder of zero (R0). Write on the class chart each sentence with R0 that isn't already posted.

Starting Menu Activities

If you set up your choices at stations, list the materials students will find at each station. Students can keep track of their choices on their own choice lists.

Choice 1: Array Game: Multiplication Pairs: directions; Array Cards, Sets A and B (1 set per pair) Choice 2: Array Game: Count and Compare: directions; Array Cards, Sets A and B (1 per pair) Choice 3: Array Game: Small Array/Big Array: directions; Array Cards, Sets A and B (I set per pair) Choice 4: Hungry Ants: directions; paper to record (1 per pair) Choice 5: The Game of Leftovers Choice 6: Mystery Numbers

Make copies of game directions available or simply post each sheet. Students may refer to the directions when in doubt about the rules of the game. Students may choose to play using only the Array Cards in Set A, which consists of multiplication pairs with products up to 50. Then when they feel comfortable, students may include Array Cards from Set B.

Choice 1: Array Game: Multiplication Pairs

Given the dimensions of an array, students are to find the total number of squares in the array; given the total, students are to find the dimensions. As they play, students write the multiplication pairs and relationships they know and don't know on a sheet of paper.

Choice 2: Array Game: Count and Compare

Students use multiplication relationships to find the sizes of students' array cards and then determine the largest.

Choice 3: Array Game: Small Array/Big Array

Students use their array cards to make "matches" between a large array and two or more smaller arrays. Each student should write their "matches" on a sheet of paper using mathematical statements.

Choice 4: Hungry Ants:

Students explore how to group other numbers of ants.

Choice 5: The Game of Leftovers

Students explore how to work with the leftovers in a division problem.

Choice 6: Mystery Numbers

Students use number strategies and their knowledge of prime and composite to find the mystery number. They could use scratch paper or graph paper to find a solution.

During Choice Time, circulate among the groups and observe students as they are involved with an activity, or use the time to meet with small groups of students who are having difficulty with a particular activity. Some things you might look for are the following:

- How are students making decisions about choosing an activity and organizing their time and materials?
- Are there too many or not enough activities going on at once?

- Are students keeping track of the choices they have completed?
- How are students figuring out the total number of squares in arrays? Are they counting one by one? Counting by groups? Do they know the multiplication pairs?
- Do some students need to spend more time counting by 2s, 3s, and 6s?
- Are some students ready to add the next set of arrays (Set B) to their existing set?

Unit: I	Division	Grade Level/Course	Duration: 60 min	•		
Lesson	n # 11	4 th Grade Date:				
Pri	ime &					
Con	mbers					
Comn	non Core	4th Grade Operations and Algebraic Thinking				
Star	ndards	Gain familiarity with f	actors and multipl	es.		
		4. Find all factor pairs for	or a whole number i	n the range 1–100. Recognize that a whole number is a		
		multiple of each of its fa	ctors. Determine w	hether a given whole number in the range $1-100$ is a		
		100 is prime or composi	te	mine whether a given whole number in the range 1–		
		100 is prime of composi				
Mat	terials/	Mathematical Tools: g	graphing paper, cour	nters 20 per pair, or cubes		
Rese	ources/	Media/Technology to b	e used to deepen lo	earning: ST Math Whole Number Multiplication and		
Le Prop	esson	Division Module				
Obj	ectives	Content:		Language:		
- ~ j		Students will be able to	analyze given	The students, given a counting number less than 100,		
		whole numbers to prove	numbers are	will be able to express if it is a prime number or a		
		either prime or composit	te.	composite number and why.		
De	pth of	Level 1: Recall	Level 2:	Skill/Concept		
Knowle	edge Level	☐ Level 3: Strategic Thinking ☐ Level 4: Extended Thinking				
Stand	lards for	☐ 1. Make sense of problems and persevere in solving them.				
Math	ematical	\square 2 P osson abstractly and quantitatively				
Pra	actice					
		5. Construct viable arguments and critique the reasoning of others.				
		⊠ 4. Model with mathematics.				
		□ 5. Use appropriate tools strategically				
		6. Attend to precision.				
		7. Look for and make use of structure.				
		🔀 8. Look for and express regularity in repeated reasoning.				
Comn	non Core	Secus on the Standards				
Instr Sh	uctional ifts in	Coherence within and across grade levels				
Math	nematics	Rigor (Balance of conceptual understanding, procedural skill & fluency, and application of skills)				
	_	KEY WORDS ESSENTIAL TO	UNDERSTANDING	WORDS WORTH KNOWING		
	DES					
>		Factor				
lar. II)	R PR XPL/	Multiple				
bul r Il		Composite number				
oca Tie	TEA					
c V &						
mi · II	IRE	Whole number				
ade Tier	IIGL	Counting number				
Ac: (J	TSF					
Ì	DEN					
	STU					
Academic Voca (Tier II & Tie	STUDENTS FIGURE TEA OUT THE MEANING SIMP	Whole number Counting number				



					Differentiated Instruction:
Define coun numbers are counting nu Review "Fa	ting numbers for 1, 2, 3, 4, Te mbers to define ctor" with studen	English Learners: Students use manipulatives Students work with a partner.			
Each dyad o Ask the stud more rows a	or triad of studen lents to take 6 cc and with the sam	ts will need 20 ounters and arra e number of co	counters. inge the 6 co unters in eac	unters in 2 or h row.	Teacher provides sentence frames for class discussions Use of visuals
000	or 00 00				Special Needs: Use of visuals. Students use manipulatives
Ask the stud more rows v should notic O O O O O	lents to take 5 cc with the same nu we that it cannot b	partner. Is a prime number divisible by two? Connection to real or natural life.			
Ask the students to take 9 counters and arrange the 9 counters in 2 or more rows with the same number of counters in each row. 0.00					
00000000					Accelerated Learners: Houghton Mifflin, Enrichment 14.3- Charting Primes and Composites.
Using their counters, ask the students to complete the following information for each number listed. Do the first four with them.					
Number	Drawing of counters arranged in rows	What are its factors?	Prime Number	Composite Number	
5	••	1, 5			
	•••	1 2 2 (
0	•••	1, 2, 3, 6			
7		1 7		+	

1, 7,

• ••••

What do they notice about 6 and 8?

1, 2, 4, 8

Ask students what they notice about the number 5 and 6.

Give students time to discuss this with a learning partner. Chart their

What can they conjecture about prime and composite numbers

7

8

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responses.

Guiding Questions:

so far?

83

	Math Meeting Direct students to complete their charts up to 20. Bring them together for a Math Meeting. Ask students to put an x in the box under Prime Number if the number has two factors and even rows, and an x in the box under Composite Number if the number has uneven rows and more than two factors. Then ask students to revise their conjectures. Students should conjecture that: The prime numbers will be those numbers for which 2 or more rows with the same number of counters in each row cannot be formed. The composite numbers are those numbers for which 2 or more rows with the same number of counters in each row can be formed. Now create a t chart with yes and no. Show students a set of numbers one at a time and ask them where to put it. Allow students to place the number in the chart and tell why they placed it there: 35, 28, 40, 25, 37, 57, 33, 75, 68 "This is a prime number because" YES NO			
Tarah	Lesson Reflection			
Reflection Evidenced by Studen Learning/ Outcomes	How are prime and composite numbers related to the daisy and the lily? Draw a bridge map of students' responses. What are some other conjectures can you make about the big idea "Rules of divisibility are related to prime and composite numbers"? Chart any new conjectures. i.e., prime numbers will signal when there are no more ways to divide. Can you think of any new examples? Bring some number examples for tomorrow. In your math journals do a quick write of what you learned, what questions you have.			

4th Grade Division Unit

Name_____ Collect data about prime and composite numbers.

	Drawing of	Factors	Prime	Composite
	counters		Number	Number
5	00			
5	000	1,5	Х	
	000			X
6	000	1, 2, 3, 6		
7				
8				
U				
q				
U				
10				
10				
11				
11				
10				
12				
10				
13				
14				
15				
16				
17				
18				
19				
20				

PRIME AND COMPOSITE NUMBERS CONCEPT TEST

Name	Score	
Determine if the number	er in the [] is prime or composite.	
1. [43]	Proof:	
2. [24]	Proof:	
3. [11]	Proof:	
4. [30]	Proof:	
5. [21]	Proof:	
PRI	ME AND COMPOSITE NUMBERS CONCEPT TEST	
Name	Score	
Determine if the number Prime Comp	er in the [] is prime or composite.	
1. [43]	Proof:	
2. [24]	Proof:	
3. [11]	Proof:	
4. [30]	Proof:	
5. [21]	Proof:	

Unit: I	Division	Grade Level/Course	Duration: 60 min			
Lesson	n # 12	4 th Grade Date:				
Comn	or Trees	4th Grade Operations and Algebraic Thinking				
Star	ndards	Gain familiarity with factors and multiples.				
		4. Find all factor pairs for a whole number in the range $1-100$. Recognize that a whole number is a multiple of each of its factors. Determine whether a given whole number is the range $1-100$ is				
	multiple of each of its factors. Determine whether a given whole number in the range $1-1$ multiple of a given one-digit number. Determine whether a given whole number in the ra					
		100 is prime or composite.				
Mat	terials/	Mathematical Tools:				
Res	ources/	Media/Technology to b	e used to deepen l	earning: ST Math Whole Number Multiplication and		
Le	esson	Division Module; Nation	hal Library of Virtu	al Manipulatives Website:		
rrep		http://pbskids.org/cyber	chase/videos/#!/seas	sons-1-8/4 Icky's Factor ;		
		http://www.geneyang.c	om/factoring/			
Obj	ectives	Content:		Language:		
		Students will be able to	analyze a given	The students will explain the pathways of their factor		
		composite number to fin	d its prime	trees.		
De	pth of	Level 1: Recall Z: Skill/Concept				
KIIUWI	euge Level	☐ Level 3: Strategic Thinking ☐Level 4: Extended Thinking				
Stand	lards for	⊠ 1. Make sense of problems and persevere in solving them.				
Math Pr	actice	2. Reason abstractly and quantitatively.				
		3. Construct viable arguments and critique the reasoning of others.				
		⊠ 4. Model with mathematics.				
		□ 5. Use appropriate tools strategically				
		☐ 6. Attend to precision.				
		7. Look for and make use of structure.				
		⊠ 8. Look for and express regularity in repeated reasoning.				
Comm	non Core	Focus on the Standard	ls t			
Instr	uctional	\boxtimes Coherence within and across grade levels				
Sn Math	itts in iematics	Rigor (Balance of conceptual understanding, procedural skill & fluency, and application of skills)				
	s N	KEY WORDS ESSENTIAL TO	UNDERSTANDING	WORDS WORTH KNOWING		
	VIDE					
nry (PRO	Prime Factor				
c Vocabula & Tier III	E EX					
	TEAC					
	о Ш					
emi r II	GUR NIN					
ade Tie	'S FIC MEA					
AC DA	ENT THE I					

Pre-teaching Considerations		Students should be able to identify the factors of a number				
Constact attons		Lesson Delivery				
Inst	tructional	Check method(s) used in the lesson:				
Methods		Modeling Guided Practice Collaboration				
		\square Independent Prestice \square Cuided Inquiry \square Deflection				
Lesson Continuum	Lesson Opening	Prior Knowledge: Students should be able to identify the factors of a number. Context and Motivation: Yesterday we compared prime numbers to a simple flower like the lily and composite numbers to a daisy. Yesterday we compared prime number and composite numbers they thought of to share with the class. Create a quick chart of their ideas. Daisy-Composite Tuly-Prime 72 71 Tell students we are going to construct – factor trees to find the prime and composite numbers of a number. A factor tree is a number tool you can use to find solutions to problems with fractions and to find solutions using algebra. When we study the traits of numbers we are study number theory. Number Theory helps us do more difficult mathematics. Before we draw factor trees lets create a Number Theory page in our journals. Talk students through the creation of this page. Fold the paper in half lengthwise. Fold both sides toward the centerfold. Fold the paper in half. See teacher's model in the lesson addendum. Direct Instruction Today's big idea is "A number is the product of its prime factors." The tree is constructed for a particular number. If a leaf is prime number, then it can be underlined as it is a prime factor. Leaves that are not prime numbers can be broken down in the same way as the original number, util all the leaves are prime numbers. Think back to the daisy and the lily. A daisy leaf can be broken down into its related factors. If you cannot break the number into factors it becomes a lily—a prime number. You are finished when you have only prime member. You are finished when you have only prime				



Lesson Reflection		
Teacher		
Reflection		
Evidenced		
by Student		
Learning/		
Outcomes		

Factors	Multiples
Factors of 24	Multiples of 24
Prime Numbers	Composite Numbers
Examples of Prime Numbers	Examples of composite Numbers

A number that is the product of 2 factors (like style counting)	The first five multiples of 24 are: 24,48,72,96,120	A composite number has 3 or more factors. 8=1×8 8=2×4 All even numbers are composite because 2 is a factor of all	15 14 27 20 24
divides a whole number that remainder. One of two whole numbers that multiply together to form a product.	Factors of 24 are 1,213,4,6,8,12,	has only 2 factors: has only 2 factors: and product ~ 7=1×7 factor factor	6 2 3

Unit: Division Lesson # 13	Grade Level/Course	Duration: 60 min.		
Multiplication	4 Glade	Date:		
Common Core	4th Grade Operations and Algebraic Thinking			
Standards	Gain familiarity with factors and multiples. 4. Find all factor pairs for a whole number in the range $1-100$. Recognize that a whole number is a			
	multiple of each of its fac	ctors. Determine wl	hether a given whole number in the range 1–100 is a	
	multiple of a given one-d 100 is prime or composit	ligit number. Deteri e.	nine whether a given whole number in the range $1-$	
	4th Grade Number and	Operations in Ba	se Ten	
	arithmetic.	anding and prope	rues of operations to perform multi-digit	
	6. Find whole-number qu divisors, using strategies	otients and remain based on place values	ders with up to four-digit dividends and one-digit ue, the properties of operations, and/or the relationship to and explain the calculation by using equations	
	rectangular arrays, and/or	r area models.	te and explain the calculation by using equations,	
Materials/	Mathematical Tools: co	lored pencils and	plain white paper	
Resources/ Lesson	Media/Technology to be Division Module	e used to deepen le	earning: ST Math Whole Number Multiplication and	
Preparation	Supplementary Materia	als: Properties slide	s or power point; teacher model of journal page	
Objectives	Content:	lagariba	Language:	
	relationships between fac	ctors and	numbers in the form of conjectures.	
	multiples.			
Depth of Knowledge Lovel	Level 1: Recall 🛛 Level 2: Skill/Concept			
Knowledge Level	☐ Level 3: Strategic Thinking ☐Level 4: Extended Thinking			
Standards for Mathematical	1. Make sense of pro	blems and perseve	ere in solving them.	
Practice	2. Reason abstractly	and quantitative		
	\square 3. Construct viable a	arguments and cri	tique the reasoning of others.	
	\Box 5. Use appropriate to	nols strategically		
	6. Attend to precisio	n.		
	7. Look for and mak	e use of structure.		
	🛛 8. Look for and exp	ress regularity in r	epeated reasoning.	
Common Core Instructional Shifts inImage: Second seco				
Mathematics	Rigor (Balance of conc	eptual understandi	ng, procedural skill & fluency, and application of skills)	
y /IDES NN	KEY WORDS ESSENTIAL TO	UNDERSTANDING	WORDS WORTH KNOWING	
lemic bular & T PROV PROV IPLE	Divisible Factors		Conjectures	
Acad /ocal ier II HER SIM	Multiples			
TEAC	Digits			

	STUDENTS FIGURE OUT THE MEANING			
Pre- Cons	-teaching ideration	Students should have knowledge of n	mber patterns and mu	iltiplication facts.
		Les	on Delivery	
Inst	ructional	Check method(s) used in the less	1:	
IVI	lethous	□ Modeling	Guided Practice	Collaboration
		Independent Practice	Guided Inquiry	Reflection
Lesson Continuum	Activities/Tasks/ Strategies/Technology/ Questioning/Engagement/Writing/Checking for Understanding	Prior Knowledge: Students should hav Context and Motivation: "Multiplication properties demonstrate How can you prove that the properties You have learned that there are five properties You have learned that there are five properties Think-Pair-Share Take a brief inventory of student know students slides or pictures of sets and H "I will show a series of slides that sho relationships are." <u>Concept Atta</u> Show students a slide of a set of 6 spice a set of 6 cars and ask them and a set of 4 dump trucks. In t write the expressions that go with the 4, 4 x 6. Students should conjecture th matter the order of factors. Ask them in numbers and operations. They should addition and subtraction. In their journals have them record the ORDER of the numbers does not ch problem of the product of a multipli Does it work with all numbers?	knowledge of number relationships between of multiplication help perties that help make revealed of the properties we students infer what relationships between nment ers. And 8 bee about the number of w eir learning dyads ask ets of pictures. 6 x 8, 8 t the products are the st their conjectures work educe that it is limited commutative Property: nge the sum of an ad ation problem.	r patterns and multiplication facts. a numbers. with division? e solving multiplication and division s of multiplication. You will show at their relationship is. n numbers. Try to deduce what the Differentiated Instruction: English Learners: Houghton Mifflin: <i>English Learners Resource</i> : p. 70 Using sentence frames Using pictorials Working in pairs or small groups Special Needs: Working in pairs or small groups Using journals Using sentence frames





In their learning dyads ask them to write the expressions that go with the sets of pictures. Students should conjecture that the products are the same as the factor, if factor multiplied by one. Ask them if their conjectures work for all numbers and operations. For example; $4 \times 1 = 4$ or $1 \times 4 = 4$ so, $4 \times 1 = 1 \times 4$ Just like each of us has our own identity, a number has its own

Just like each of us has our own identity, a number has its own identity as well. We are all unique in that every person has their own identity, which is themselves, a number has its own identity as well, itself.

In their journals have them record Multiplicative Identity Property: **The product of any number and one is that number.**

Ask students what the inverse would be: $4 \div 1 = 4$ or $4 \div 4 = 1$

Six pickle jars, but no pickles:



In their learning dyads ask them to write the expressions that go with the sets of pictures. Students should conjecture that any number multiplied by zero equals zero.

In their journals have them record The Zero Property: The product of zero and any number is zero. Examples: $6 \times 0 = 0$: $0 \times 6 = 0$

When students have completed taking notes for their journal ask them to teach each other (reciprocal teaching).

	Activities/Tasks/ Strategies/Technology/ Questioning/Engagement/Writing/Checking for Understanding	 Practicing the Properties: Which property of multiplication is shown? (5 × 6) × 3 = 5 × (6 × 3) Which property of multiplication is shown? 9 × 8 = 8 × 9 Which property of multiplication is shown? 0 = 9 × 0 Which property of multiplication is shown? 1 × 5 = 5 Which equation shows the commutative property of multiplication? a. 8 × (1 - 0) = 8 × 1 - 8 × 0 b. 7 × 8 = 8 × 7 c. 5 × (3 + 9) = 5 × 3 + 5 × 9 d. 8 + 8 + 8 + 8 = 5 × 8 Which property of multiplication is shown? 6 × 5 + 2 × 5 = (6 + 2) × 5 Which property of multiplication is shown? 4 × 0 = 0 Reflection: How can you use the properties of multiplication to help with division? The Commutative and Associative Properties help make your multiplication accurate. The properties offer different ways to solve the same problem, often in an easier way. By allowing for different opportunities to solve the problem, it is easier to check your work and find a correct product.	
		Lesson Reflection	
Т	eacher		
R	eflection		
Ev	idenced		
by	Student		
L	earning/		
0	utcomes		

Unit: Division	Grade Level/Course Duration: 60	min.		
Lesson # 14	4 th Grade Date:	Date:		
Divisibility				
Kules	4th Crade Operations and Algebraic	Thinking		
Standards	Gain familiarity with factors and m	Itiples.		
~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~	4. Find all factor pairs for a whole num	ber in the range 1–100. Recognize that a whole number is a		
	multiple of each of its factors. Determi	ne whether a given whole number in the range 1–100 is a		
	multiple of a given one-digit number. I	Determine whether a given whole number in the range 1–		
	100 is prime or composite.	n Daga Tan		
	Use place value understanding and r	roperties of operations to perform multi-digit		
	arithmetic.	- operations of operations to be recent manual media		
	6. Find whole-number quotients and re	mainders with up to four-digit dividends and one-digit		
	divisors, using strategies based on plac	e value, the properties of operations, and/or the relationship		
	between multiplication and division. If	ustrate and explain the calculation by using equations,		
	rectangular arrays, and/or area moders.			
Materials/	Mathematical Tools: index cards, col	ored pencils and plain white paper		
Resources/	Media/Technology to be used to deep	en learning: ST Math Whole Number Multiplication and		
Lesson	Division Module Supplementary Materials: Teacher m	adel of journal page. Write the following numbers on index		
i reparation	cards 6025, 1230, 723, 846, 3421, 680.	975. 2963		
Objectives	Content:	Language:		
	Students will be able to use divisibility	d form of conjectures and record them in their math		
	Tutes to find factors related to a divider	journals.		
Depth of	Level 1: Recall 🛛 Level 2: Skill/Concept			
Knowledge Level Level 3: Strategic Thinking Level 4: Extended Thinking		el 4: Extended Thinking		
Standards for	☐ 1. Make sense of problems and pe	rsevere in solving them.		
Mathematical	2. Reason abstractly and quantita	tively.		
Practice	\square 3. Construct viable arguments an	d critique the reasoning of others.		
	\boxtimes 4 Model with methometics	a critique die reasoning of others.		
	5. Use enprenriete tools strategie	. 11		
	\square 5. Use appropriate tools strategically			
	\Box 0. Attend to precision.	tura		
	\boxtimes 8 Look for and express regularit	v in reneated reasoning		
Common Core	E Focus on the Standards			
Instructional	\square Focus on the Standards			
Shifts in Mathematics	\boxtimes Concrete within and across grade levels \boxtimes Digor (Balance of concentual understanding precedural skill & fluency, and application of skills)			
Wrathematics		words words words words words		
mic ular ER	ZINET WORDS ESSENTIAL TO UNDERSTAND			
abt Achi MPL	Divisibility	Conjectures		
Aca /oc Prc SII	Digits			
 ✓ 				

	HE	Factors
		Multiples
	ST	
Pr	e-teaching	Students should have knowledge of number patterns and multiplication facts
Сог	nsideratior	IS I
		Lesson Delivery
In	structiona	I Check method(s) used in the lesson:
	Methods	☐ Modeling ☐ Guided Practice ☐ Collaboration
		☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐
		Prior Knowledge: Students should have knowledge of number patterns and multiplication facts
		Context and Motivation:
		Rules of divisibility are tools to solve division problems. (The Rules of Divisibility are listed in
		HM Lesson 14.2. Only teach the rules that you think are useful to your students. It will be difficult to
		teach all of the rules. 4 th grade usually focuses on 2, 3, 5, 9, and 10) Tell students: Vesterday we explored how the multiplication properties are related to division
		Today we will investigate rules of divisibility and practice how to use them as a tool to solve
		division problems. Rules of divisibility are number patterns that can be used to estimate the
		factor related to the dividend and divisor. Let's define divisibility.
		$5\overline{)1245}$ $5\overline{)3671}$
		Randomly choose student groups to share out their solutions. Ask them what they noticed about the
		quotients of the two problems. (one number could be divided evenly and the other had remainders.) Give students the definition of divisibility: be able to be divided with no remainder.
		"Have you ever wished that you could tell if an example would divide out evenly or have a
Е		remainder before you divide?" Tall students: "Suppose I told you I am a math magician and can do this. I'll prove this to you
nnu	ning	by simply looking at some numbers and then telling you if they will divide evenly by 5."
Conti	Ope	Write the following numbers on cards: 6025, 1230, 723, 846, 3421, 680, 975, 2963. Ask students to randomly choose a card and respond ves or not to its divisibility. (You are also modeling the
00 (uossa	language for students. You may want to place a sentence frame next to the T-chart so students
Less	Γ	Have students look at all the numbers in the Yes column. Tell them to look for similarities in the
		numbers. If necessary, use guiding clues such as "focus on the digit in the ones place" or underline
		the last digit in the yes column. After someone has discovered the pattern, formulate a rule and write it on the board. If a number ends in the digits 0 or 5, it will always be evenly divisible by 5
		NO: 2421, 722, 846, 2062
		Divisible by 5
		Yes No











Divisibility Rules

I'm 御湿 and I'll be your friend, as long as an even #'s on the end. 曲③ will work for me, you see, if the sum is divisible by 3. The 翻到 won't be such a chore, if the last 2 are divisible by 4. The 🖽 is my biggest hero, he has to end in 5 or 0. The 邸③ will always go into me, as long as so does 2 and 3. 🕮 will go into me just fine, if the sum is divisible by 9. I'm 🖽 and this you should know, I always end in a big fat O!

risible 5	870 542
not div	12,551 685
ble by 5	12,040 278
divisi	817 14,095

isible 2	81	10,256
not div	10,147	558
ble by 2	94	5,790
divisi	15,289	1,023

isible 3	10,035 678	
not div	2,005 82	
ble by 3	12,021 345	
divisi	152 3,016	
visible 9	82	11,256
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not div	95	5,790
ble by 9	15,289	1,024
divisi	10,148	558

Unit: Division	Grade Level/Course	Duration: 60 min	
Lesson # 15	4 th Grade Date:		
Menu Activities			
Common Core	4th Grade Operations	and Algebraic Thi	nking
Standards	Gain familiarity with f	actors and multiple	es.
	4. Find all factor pairs for a whole number in the range 1–100. Recognize that a whole number is a		
	multiple of each of its fa	ctors. Determine wi	hether a given whole number in the range $1-100$ is a mine whether a given whole number in the range $1-100$
	100 is prime or composite.		
	4th Grade Number and	l Operations in Ba	se Ten
	Use place value unders	tanding and prope	rties of operations to perform multi-digit
	6. Find whole-number q	uotients and remain	ders with up to four-digit dividends and one-digit
	divisors, using strategies	based on place val	ue, the properties of operations, and/or the relationship
	between multiplication a	nd division. Illustra	te and explain the calculation by using equations,
	rectangular arrays, and/c	n area moders.	
Materials/			
Resources/	Textbook: 4 th Grade Ho Mathematical Tools: co	ughton Mittlin Inte	rvention Activities
Preparation	Media/Technology to b	e used to deepen le	earning: ST Math Whole Number Multiplication and
-	Division Module		
	Supplementary Materials : Menu Activities, Houghton Mifflin Chapter 14 Math Centers, p. 208C. Chapter 15 Math Centers p. 224C.		
		centers p. 52 te	
Objectives	Content:		Language:
	using a variety of strateg	ties.	division games.
Depth of Knowledge Level	Level 1: Recall 🛛 Level 2: Skill/Concept		
Level 3: Strategic Thinking Level 4: Extended Thinking			Extended Thinking
Standards for Mathematical	≥ 1. Make sense of problems and persevere in solving them.		
Practice	2. Reason abstractly and quantitatively.		
	□ 3. Construct viable arguments and critique the reasoning of others.		
	🛛 4. Model with math	ematics.	
	🗌 5. Use appropriate t	ools strategically	
	6. Attend to precision	on.	
	☐ 7. Look for and make use of structure.		
	⊠ 8. Look for and express regularity in repeated reasoning.		
Common Core	Socus on the Standards		
Instructional Shifts in	Coherence within and across grade levels		
Mathematics	Rigor (Balance of conceptual understanding, procedural skill & fluency, and application of skills)		
, si O	KEY WORDS ESSENTIAL TO	UNDERSTANDING	WORDS WORTH KNOWING
ic Iry VIDE VATIC			
dem bula L & _ PRO PLAN	Review previous vocabul	arv	
Aca oca er I HER E EX	rection providus vocadur		

	STUDENTS FIGURE OUT THE			
Pr Cor	e-teaching Isideration	Students should be able to relate multiplication and division as inverse operations. Students should also be able to interpret a division expression and form equal groupings.		
		Lesson Daliyony		
In	structional	Check method(s) used in the lesson:		
	Methods	⊠ Modeling □ Guided Practice ⊠ Collaboration		
		☐ Independent Practice ☐ Guided Inquiry ☐ Reflection		
	Lesson Opening	rior Knowledge: Students should be able to relate multiplication and division as inverse perations. Students should also be able to interpret a division expression and form equal groupings. Sontext and Motivation: To the Teacher: The following activities are provided so that students have independent portunities to practice multiplication and division, and so that the teacher has opportunity to meet with students who are struggling.		
	standing	Students work on the Menu Activities, while teacher works with small group of students. Students could choose from Menu Activities 1-4, however teach students new activities. English Learners: The following are Menu Activities: Houghton Mifflin Chapter 14 Math Centers, p. 298C, Chapter 15 Math Centers p. 224C English Learners		
Lesson Continuum	asks/ Strategies/Technology/ ent/Writing/Checking for Unde	In students math journals students should keep a record of Menu Activities that they complete. Intervention Activities from Houghton Mifflin Strategic Intervention Book: Properties: NS 19-20 Problem Solving: NS 29-31, NS 39 Multiplying by 10s: NS 32 Divisibility Rules: NS 37-38 Factors: NS 45		
Benchmark Intervention Book: Properties and Divisibility Rules: pp. 28-29 Multiples of Ten: p. 59 Model Division: p. 61-70 English Learners Resources Book: Using Language and Solving Word Problems pp. 107-114 (for Beginning and Early Intermediate English Language Learners) Can be either Teacher Directed or students can listen to the CD and complete the activities in small groups or pairs.				

		Closing/Debrief
		Call students together to debrief the Menu Activities Session. Ask students: What challenges did you find while working? Is there a learning pair who wants to share how well they worked together? Why? Which activities did you complete? How did the activity help you?
	•	Lesson Reflection
T Re Ev by Le Ou	Teacher eflection videnced Student earning/ utcomes	





a hi



Unit: I	Division	Grade Level/Course	Duration: 60 min		
Lesson	n # 16	4 th Grade Date:			
Dividi	ng Larger				
Nu	mbers				
Comm	10n Core	4th Grade Operations and Algebraic Thinking			
Star	ndards	Gain familiarity with factors and multiples.			
		4. Find all factor pairs for a whole number in the range $1-100$. Recognize that a whole number multiple of each of its factors. Determine whether a given whole number in the range $1-100$ is			
		multiple of a given one-	digit number Deter	nine whether a given whole number in the range 1–	
		100 is prime or composi	te.		
		4th Grade Number and	d Operations in Ba	se Ten	
		Use place value unders	tanding and prope	rties of operations to perform multi-digit	
		arithmetic.			
		6. Find whole-number q	uotients and remain	ders with up to four-digit dividends and one-digit	
		aivisors, using strategies	s based on place val	te and explain the colculation by using equations.	
		rectangular arrays and/c	or area models	te and explain the calculation by using equations,	
		rootungulur ultu jo, ultu c			
Mat	terials/	Mathematical Tools: i	ndex cards, adding i	nachine tape or sentence strips, calculators, 300	
Reso	ources/	charts, math journals			
Le	esson	Media/Technology to b	e used to deepen le	earning: ST Math Whole Number Multiplication and	
Prep	aration	Division Module Supplementary Materi	als Packages and	Fround TEPC	
		Supplementary Water	ais. 1 uchages and	iroups, TERC	
Obj	ectives	s Content: Language:			
		Students will use multip	les of 10, 100, and	Students will explain how using multiples of 10 help	
		1,000 to solve division p	problems based on	them to apply division in problem situations using	
larger numbers. larger numbers.			larger numbers.		
De	pth of	Level 1: Recall	E Level 2:	Skill/Concept	
Knowledge Level X Level 3: Strategic Thinking			Extended Thinking		
La Level 3. Su augre 1 minking Elevel 4. Extended 1 minking					
Stand Moth	ards for	\boxtimes 1. Make sense of problems and persevere in solving them.			
Practice		2. Reason abstractly and quantitatively.			
		3. Construct viable	arguments and cri	tique the reasoning of others.	
		⊠ 4. Model with mathematics.			
		☐ 5. Use appropriate tools strategically			
		6. Attend to precision.			
		☐ 7. Look for and make use of structure.			
		⊠ 8. Look for and express regularity in repeated reasoning.			
Common Core		Focus on the Standards			
Instructional Shifts in Mathematics		\boxtimes Coherence within and across grade levels			
		\boxtimes Concrete within and across grade levels \boxtimes Digor (Balance of concentual understanding presedural skill & further and employed a skills)			
		Kigor (Balance of conceptual understanding, procedural skill & fluency, and application of skills)			
J DES TION		KET WORDS ESSENTIAL TO	UNDERSTANDING		
mic Ilar	ANA	Multiples			
Acader ocabu cher Pro		*			
	TEA				

	STUDENTS URE OUT THE		
Pre-teaching		Students should know various strategies for modeling division.	
CUI	151001 2010	Lesson Delivery	
In	structiona	Check method(s) used in the lesson:	
	Methods	☐ Modeling ☐ Guided Practice ☐ Collaboration	
		☐ Independent Practice ⊠ Guided Inquiry ⊠ Reflection	
	 Prior Knowledge: Students should know various strategies for modeling division. Context and Motivation: Today's big idea is "Division is used to solve problems in daily life." "Today we will encounter some real life problems using larger numbers that can be solved by using division. We will think about all the strategies we have been using, and think about ways to apply those strategies to larger numbers." Just as we can skip count by 3s, 5s, or 6s, and find the multiples of those numbers, we can also 		
	pening	We can use tools like cubes, a 300 chart, or a calculator to help us skip count by larger numbers. Let's make a list of the multiples of 30.	
		Chart the multiples of 30 on the board, as students call them out. (30, 60, 90, 120) Then ask students to continue the list on their own. After a few minutes, call students together to discuss strategies for finding the multiples of 30.	
ntinum		Some students might use a calculator and push the following sequence of buttons: $30 + = =$. Others might push the buttons: $30 + 30 + 30$ Some might mark the multiples on a 300 chart. Some might use a T-chart and list the multiples. Discuss these various strategies, and how they are related.	
Lesson Co Lesson C		Count around the class by 30s, and ask each student to write their number in their journal, so they don't forget it. Also add these numbers to your list on the board. Ask students about the patterns they see in the multiples of 30. If no one mentions the relationship to the multiples of 3, make sure that this is brought up.	
		"Now we are going to predict my height, using the multiples of 30. How tall do you think I am, using an index card to measure, and counting by 30s?"	
		Give students a moment to think, then take predictions.	
		Find a spot on the wall where you can stand comfortably, and there is a clear path from the floor to the top of your head. Have students help to measure your height, using a strip of adding machine tape, or several sentence strips taped together. Tape the strip to the wall vertically. Start with the student who has the number 30, then proceed with 60, 90, 120, etc. Mark off the height of one index card (horizontally) starting from the floor and have the student write his/her number in the space. When the numbers reach knee height, stop to revise predictions.	
"Hmm, we are now at (180). Let's read the multiples so far. What is the pattern? What think? Could your prediction still be accurate? Would you like to revise your prediction number do you think will be on the card that is as high as the top of my head?"			

		Revise predictions at regular intervals (waist-height, shoulder- height, etc.) "What is a possible number we could have for my final height? Could it be 584? Why not? Let's think about which estimates are possible, and which ones don't fit the pattern? That's right, it has to be a multiple of 30."	
		Continue adding numbers until you reach the end of the adding machine tape (the top of your head). (The final product will resemble a measuring tape, with multiples of 30 written in the spaces between lines.) Celebrate the closest prediction.	
		"Our final number is (630). How many multiples of 30 is that? How can we find out, without counting all the numbers? Write x 30 = on the board. How many 30s are there in 630?"	
		Give students time to devise strategies for solving the problem, then share out. Compare solutions.	
		Guided Inquiry	Differentiated Instruction:
		"Now you and your partner will have a chance to build your own multiple towers that are as tall as you are. Choose a number to skip count, using numbers from this list: 15, 18, 20, 24, 32, 36, 40, 45, 55, 60, 64, 70, 72, 75, or 82. You can use any of your mathematical tools to help you build your list of multiples. When you have listed at least 12 multiples, you may begin to build your towers. Take turns cutting a	English Learners: Working with partners Using hands-on materials
nology/ for Understanding	strip of adding machine tape as tall as the other one. You may lie down on the floor or stand up to the wall. Then take one index card, and carefully mark off the width of one card all the way from one end of the adding machine tape to the other end. In the spaces between the lines, start listing your multiples. Predict what number you might end with."	Special Needs: Select from appropriate multiples Working with partners Using hands-on materials	
	es/Tasks/ Strategies/Tec gement/Writing/Checkin	 Circulate around the classroom as students work, lending assistance as necessary. Document the various multiples chosen, and the accuracy of multiples listed. Ask pairs to check their work before proceeding to the towers. In addition, observe the following: How are students using mathematical tools to assist their work? Are students recognizing and using number patterns to build 	Accelerated Learners: Select from more complex multiples Answer more advanced questions
	Activiti ning/Engag	 their multiple towers? What strategies are students using to practice difficult number combinations? Where are students getting stuck? How are they getting past. 	
	Question	these difficult areas?	

	Reflection: As students complete their towers, give them these reflective questions to answer about their multiple towers: • What number did you use to build your multiple tower? • Did your tower include 100, or any multiples of 100 (200, 300, etc.)? • If you kept building your tower until it reached the next multiple of 100, how many numbers would be in your tower? • What patterns do you notice in your tower? • What patterns do you notice in your tower? • Call students together to share their results. Closing questions: • How can you express the final number on your multiple tower and the multiple you are counting by as a division expression? What will the solution tell you? (how many multiples were used to build your tower) • How did this activity help us with multiplication and division
	 How did this activity help us with multiplication and division of larger numbers?
I	Lesson Reflection
Teacher Reflection Evidenced by Student Learning/ Outcomes	

Unit: Division	Grade Level/Course	Duration: 60 min		
Lesson # 17	4 th Grade	Date:		
Using Patterns				
Common Core	4th Grade Operations	and Algebraic This	nking	
Stanuarus	4 Find all factor pairs for a whole number in the range 1, 100. Decognize that a whole number is a			
	multiple of each of its fa	ctors Determine w	hether a given whole number in the range $1-100$ is a	
	multiple of a given one-	digit number. Deter	mine whether a given whole number in the range 1–	
	100 is prime or composi	te.	6	
	4th Grade Number and	l Operations in Ba	se Ten	
	Use place value unders	tanding and prope	rties of operations to perform multi-digit	
	arithmetic.		dans with we to found init dividends and one disit	
	divisors using strategies	based on place value	ue the properties of operations, and/or the relationship	
	between multiplication a	nd division. Illustra	te and explain the calculation by using equations.	
	rectangular arrays, and/c	r area models		
Materials/	Mathematical Tools: to	ols of students' cho	ice: have available counters, tiles, blocks	
Resources/	Media/Technology to b	e used to deepen le	earning: S1 Math Whole Number Multiplication and	
Prenaration	Supplementary Materi	als [.] Math Story exc	ernts: How Much How Many How Far How Heavy	
reputation	How Long, How Tall is	1000?; Great Estim	ations (Lesson slides will be provided)	
	Math Journal pages prov	rided.		
			-	
Objectives	Content: Students will be able to a	usa basia division	Language:	
	facts and patterns of zero	as to divide	explain the process they used to solve a division	
	mentally and solve divis	ion problems with	problem.	
	larger numbers.			
Depth of Level 1: Recall Level 2: Skill/Concept		Skill/Concept		
Kilowicuge Level	Level 🔀 Level 3: Strategic Thinking 🗌 Level 4: Extended Thinking			
Standards for	⊠ 1. Make sense of problems and persevere in solving them.			
Mathematical	2. Reason abstractly and quantitatively.			
Practice	— · · · · · · · · · · · · · · · · · ·	arguments and cri	tique the reasoning of others	
	5. Construct viable arguments and critique the reasoning of others.			
	🖂 4. Model with math	ematics.		
	🔲 5. Use appropriate t	ools strategically		
	6. Attend to precision	on.		
	7. Look for and ma	ke use of structure		
	\boxtimes 8 Look for and express regularity in repeated reasoning			
	o. Look for and express regularity in repeated reasoning.			
Common Core Instructional	Focus on the Standard	15		
Shifts in	Coherence within and across grade levels			
Mathematics	Rigor (Balance of con	ceptual understandi	ng, procedural skill & fluency, and application of skills)	
) DES	KEY WORDS ESSENTIAL TO	UNDERSTANDING	WORDS WORTH KNOWING	
mic lar ovir				
der bu PR(APL	Divisor			
Dividend				
A V.	Quotient			

	UDENTS KE OUT THE					
	STI					
Pr Coi	Pre-teaching Considerations Students should have knowledge of division by grouping or algorithm, multiplication and division facts, and understanding of place value.					
Ŧ		Lesson Delivery				
In	structional Methods	Check method(s) used in the lesson: $\Box = \Box = \Box = \Box = \Box = \Box$				
Prior Knowledge: Students should have knowledge of division by grouping or algorithmultiplication and division facts, and understanding of place value. Context and Motivation: Start with making estimation pictures. Ask students to estimate using numbers with quantity they see. Each photo will increase the amount of to be estimated. For each students to divide among their table groups; i.e. We see 80 cherries. If we division go ourselves we will each receive Ask students how they found the quot 80 - 10; 70 - 10; 60 - 10; 50 - 10; 40 - 10; 30 - 10; 20 divided by 6 and there were or other groups may estimate more and divide by four. Compare strategies and for patterns of use of zero. $120 \div 4 \longrightarrow 100 \div 4 = 25$ $20 \div 4 = 5$ $25 \pm 5 = 30$		multiplication and division facts, and understanding of place value. Context and Motivation: Start with making estimation pictures. Ask students to estimate using numbers with zeros the quantity they see. Each photo will increase the amount of to be estimated. For each picture ask students to divide among their table groups; i.e. We see 80 cherries. If we divide them among ourselves we will each receive Ask students how they found the quotient. 80 - 10; 70 - 10; 60 - 10; 50 - 10; 40 - 10; 30 - 10; 20 divided by 6 and there were 2 left over. Or other groups may estimate more and divide by four. Compare strategies and focus on the patterns of use of zero. $120 \div 4 \longrightarrow 100 \div 4 = 25$ $20 \div 4 = 5$ $25 + 5 = 30$				
	white Board Discussion on Patterns of Zero					
Lesson Continuum	White Board Discussion on Patterns of Zero White board discussions should move at a good pace. For today's exercises tell students they do not have to write the number sentences—they only need to write their answer and be prepared to justified have to write the number sentences—they only need to write their answer and be prepared to justified to the sentences and the prepared to justified to the sentences					
	$ \begin{array}{c} 480 \div 8 = 60 \\ 4,800 \div 8 =? \end{array} $					

Show students the following sequence of problems. Ask students to discuss their thinking with a learning partner. When they know their answers have them record it on a white board. At a signal ask students to hold up their boards so that you could see their thinking. Ask students to retell their reasoning for writing 30 and 300. $21 \div 7 = 3$

 $21 \div 7 = 3$ $210 \div 7 = ?$ $2,100 \div 7 = ?$

Now mix up the discussion and check for precision. 4,500 \div 9 =? Write the following problems for students to solve. 3,200 \div 4 = n 420 \div 6 = d 1,400 \div k = 700

 $m \div 5 = 90$ Discuss the use of variables.

Problem Solving with Larger Numbers

Ask students to write an expression for the problem and then solve it. These are journal problems. The class may not work out all the problems. What problems are not completed, students may do for homework.

The Delmar family collected pennies. When the jar was full, Mrs. Delmar gave the pennies to her three sons. They counted 1,500 pennies and shared them equally. How many pennies did each boy get? (500 dimes each)



Sela has 6 times as many coins now as she had 4 months ago. If Sela has 240 coins now, how many coins did she have 4 months ago? (40 coins)

What about 1000 french fries? Even if you loved french fries, 1000 would be too much for one person. You could share them. A single serving has about 40 fries. How many friends would 1000 french fries feed? (25)

Chip collected 289 dimes. Sue collected 191 dimes. They divided all their dimes into 8 stacks. If each stack had an equal number of dimes, how many dimes were in each stack? *(60 dimes)*

Robby sees a rare 1937 penny. The cost is \$210. If he saves \$3 every week, will Robby have enough money to buy the coin after one year? (*No, It will take him 70 weeks to save the money* $(210 \div \div 3 = 70)$). There are only 52 weeks in a year.)

Differentiated Instruction:

English Learners:

Houghton Mifflin: Universal Access p.207B Using pictorials Working in pairs or small groups Teacher prompts

Special Needs:

Houghton Mifflin: *Reteach* 12.4

Working in pairs or small groups Using journals Teacher prompts

Accelerated Learners:

Houghton Mifflin: *Chapter Challenges and Investigations:* Chapter 12, p. 71 Students explore the inverse of the associative and commutative properties.

		Math Meeting
		Ask a few students to share their solutions with the class. Make sure students are using academic language with coherence. Provide prompts for students if necessary. How did noticing the patterns of zeros help you solve the division problems?
	I	Lesson Reflection
T Ro Ev by Lo O	Feacher eflection videnced Student earning/ utcomes	

The Delmar family collected pennies. When the jar was full, Mrs. Delmar gave the pennies to her three sons. They counted 1,500 pennies and shared them equally. How many pennics did each boy get?	Sela has 6 times as many coins now as she had 4 months ago. If Sela has 240 coins now, how many coins did she have 4 months ago?
What about 1000 french fries? Even if you loved fried, 1000 would be too much for one person. You could share them. A single serving has about 40 fries. How many friends would 1000 french fries feed?	Chip collected 289 dimes. Sue collected 191 dimes. They divided all their dimes into 8 stacks. If each stack had an equal number of dimes, how many dimes were in each stack?

Problem Solving with Division and Patterns of Zero	Robby sees a rare 1937 penny. The cost is \$210. If he saves \$3 every week, will Robby have enough money to buy the coin after one year?

Unit: I	Division	Grade Level/Course	Duration: 60 min			
Lesson	# 18	4 th Grade	Date:			
Find	ling an					
Comm	erage	4th Grade Onerations	and Algebraic Thi	nking		
Star	idards	Gain familiarity with factors and multiples.				
		4. Find all factor pairs for	or a whole number i	n the range 1–100. Recognize that a whole number is a		
		multiple of each of its fa	ctors. Determine w	nether a given whole number in the range 1–100 is a		
		multiple of a given one-	dıgıt number. Deter	mine whether a given whole number in the range 1–		
		4th Grade Number and	le. I Onerations in Ba	se Ten		
		Use place value unders	tanding and prope	rties of operations to perform multi-digit		
		arithmetic.	arithmetic.			
		6. Find whole-number quotients and remainders with up to four-digit dividends and one-digit				
		between multiplication a	and division Illustra	te and explain the calculation by using equations		
		rectangular arrays, and/o	or area models.	the und explain the culculation by using equations,		
Mat	erials/	Mathamatical Taolar of	laulatora math iou	mala		
Keso	ources/	Mathematical 1001s: ca Media/Technology to h	e used to deepen le	earning: ST Math Whole Number Multiplication and		
Prep	aration	Division Module	e used to deepen R	an mig. 91 Multi whole Multipleation and		
Obj	ectives	Content:	wara and for larger	Language: Studente will evolvin how to find on everyon wing		
		numbers	verages for larger	larger numbers		
		numbers.		larger numbers.		
Dej	pth of	Level 1: Recall	🛛 Level 2:	Skill/Concept		
Knowle	edge Level	🛛 Level 3: Strategic Thi	inking Level 4: Extended Thinking			
Stand	ards for	1. Make sense of pro	oblems and persev	ere in solving them.		
Mathe	ematical	$1 \square 2$. Reason abstractly and quantitatively.				
Pra	actice	☐ 3. Construct viable	arguments and cri	tique the reasoning of others.		
		X 4. Model with math	ematics.	-1		
		\Box 5 Use appropriate t	ools strategically			
		\Box 6. Attend to precisi	n			
		\Box 7 Look for and mat	/n. ke use of structure			
		\boxtimes 8 Look for and exp	ress regularity in r	reneated reasoning		
Comm	Como	Ecours on the Standard		cpcatcu reasoning.		
Instru	uctional		12			
Shi	ifts in	Coherence within and	across grade levels			
Math	ematics	Rigor (Balance of con	ceptual understandi	ng, procedural skill & fluency, and application of skills)		
y	DES	KEY WORDS ESSENTIAL TO	UNDERSTANDING	WORDS WORTH KNOWING		
mic lar		Average				
idei Ibu	R PR					
Aca oca	CHEI LE E)					
↓ ►	TEA					

	STUDENTS FIGURE OUT THE				
Pr Coi	e-teaching nsideration	s Students should know addit strategies.	know addition of multiple addends. They should have several efficient division		
			Lesson Delivery		
In	structional Motheda	Check method(s) used in t	he lesson:		
	vietnoas	☐ Modeling	Guided Practice	Collaboration	
		Independent Practice	🛛 Guided Inquiry	⊠ Reflection	
ontinuum	Lesson Opening	Prior Knowledge: Students sh Context and Motivation: Today's big idea is "Division i "Today we will investigate som numbers." At Moorpark Elementary Scho number of students: 24, 25, 20, However, the students must be students will enter the theater i Take a few minutes to think ab number of students in each gro Ask students to share their stra from the class of 24, and add a the numbers and divide by four Mathematicians use many diffe considered typical out of a list develop different strategies to b	ould know addition of mult s used to solve problems in the e situations in which we will ol, there are four fourth grade and 23. The fourth grade st evenly divided in order to b n each group? out this problem. How can we up? tegies. Some may move 2 st Il three to the class of 20, to the class of 20, to the class how these strategies event words to mean the aver- of numbers. This may be the determine the mean of a gro	iple addends and division strategies. daily life." ill need to find the average of some larger de classes. They have the following udents have been invited to a play. be admitted to the theater. How many we be sure that there are exactly the same udents from the class of 25, and 1 student make 23 in each class. Some may add all tes would lead to the same solution. rage, or the one number that can be e mean, median, or mode. Today, we will up of numbers.	
Lesson C		Guided Inquiry 'A zookeeper has to know how much food to order for each of his animals. He kept a chart of the food the elephants ate each day for a week. Now he needs to know the average number of pounds eaten each day. Look at this table, and answer the questions related to the nformation." Food eaten per day in pounds Male elephant Female elephant Monday 135 pounds 125 pounds Tuesday 125 pounds 130 pounds Wednesday 120 pounds 120 pounds Friday 130 pounds 125 pounds		h of his day for a ds eaten ed to the elephant nds nds nds nds nds nds	

		Differentiated Instruction:
	 What was the average amount of food eaten by the male elephant each day? How much greater was the average amount of food eaten by the male elephant than the female elephant? 	English Learners: Working with partners Using hands-on materials
	"Work together in pairs to find the answer to each question. Keep track of your work in your math journals. What strategies might you try?"	Special Needs:
lerstanding	Circulate among the students and notice how they attack the problems. Do they know how to determine an average in the traditional manner? Do they use innovative methods? Call students together to share their strategies. Look for connections between their methods.	Working with partners Using hands-on materials
inology/ for Unc	"Now let's work on a problem where we know the average, but we don't know one of the addends."	
ategies/Tech ng/Checking	There are three tigers at the zoo. One weighs 259 pounds. Another weighs 326 pounds. Their average weight is 294 pounds. How can we determine the weight of the third tiger?	Accelerated Learners: Answer more advanced questions
ks/ Str /Writii	Allow students to work a few minutes, then review strategies.	
ities/Tas] agement	"Sometimes when we are asked to find averages, the results are not reasonable. Let's look at this problem:"	
Activ ing/Eng	The aquarium has 310 fish, 60 sea animals, and 20 sea birds. What is the average number of each type of sea creature?	
Question	Allow students to work a few minutes, then ask, "Why would the average in this case not be reasonable? There are many more fish than either of the other kinds of sea creatures. If the numbers are too different, the average doesn't make sense."	
	Review the following reflective questions with your students.	
	Reflection: • What are some situations where we might want to determine an average?	
	How can we make sure everyone has an equal share?What is an efficient strategy to determine an average?	
	Lesson Reflection	
Teacher		
Reflectio		
by Stude	t	
Learning	/s	

Unit: I	Division	Grade Level/Course	Duration: 60 min			
L L	Jnit	4 th Grade	Date:			
Asse	essment			-19		
Stan	ion Core idards	 4th Grade Operations : Gain familiarity with fa 4. Find all factor pairs for multiple of each of its fa multiple of a given one-of- 100 is prime or composi 4th Grade Number and Use place value unders arithmetic. 6. Find whole-number q divisors, using strategies between multiplication a rectangular arrays, and/or 	 Grade Operations and Algebraic Thinking familiarity with factors and multiples. and all factor pairs for a whole number in the range 1–100. Recognize that a whole number is a ple of each of its factors. Determine whether a given whole number in the range 1–100 is a ple of a given one-digit number. Determine whether a given whole number in the range 1–s prime or composite. Grade Number and Operations in Base Ten place value understanding and properties of operations to perform multi-digit metic. and whole-number quotients and remainders with up to four-digit dividends and one-digit ors, using strategies based on place value, the properties of operations, and/or the relationship een multiplication and division. Illustrate and explain the calculation by using equations, ngular arrays, and/or area models. 			
Mat Reso Le Prep	terials/ ources/ esson aration	Mathematical Tools: P Supplementary Materi	erformance-Based T als: End of Unit Di	Fask visionTest		
Obj	ectives	Content:Language:Students will apply division concepts and skills through solving problems in the unit test.Students will create and record a situation to fit a given division expression and solve for the expression.				
Dej Knowle	pth of edge Level	Image: Second				
Stand Matho Pra	ards for ematical actice	 1. Make sense of pro 2. Reason abstractly 3. Construct viable 4. Model with math 5. Use appropriate t 6. Attend to precision 7. Look for and main 8. Look for and exp 	sense of problems and persevere in solving them. n abstractly and quantitatively. ruct viable arguments and critique the reasoning of others. with mathematics. propriate tools strategically I to precision. for and make use of structure. for and express regularity in repeated reasoning.			
Comm Instru Shi Math	non Core uctional ifts in ematics	 ☑ Focus on the Standard ☑ Coherence within and ☑ Rigor (Balance of con 	ls across grade levels ceptual understandi	ng, procedural skill & fluency, and application of skills)		
Academic Vocabulary	TEACHER PROVIDES SIMPLE EXPLANATION	KEY WORDS ESSENTIAL TO No new vocabulary	UNDERSTANDING	WORDS WORTH KNOWING		

	STUDENTS URE OUT THE							
	FIG							
Pr	e-teaching	Final unit a	ssessment—	Students show	uld have gain	ed all necess	ary sk	ills.
Cor	nsideration	15		Losso	n Dolivory			
In	structional	Check me	thod(s) used	in the lessor	n:			
	Methods	🗌 Modeli	nσ		Guided Prac	tice 🗌	Colla	horation
					Cuided Incu		Doflor	otion
	Losson				Julucu Iliqu		KUIIU	
	Opening	Context and	euge: Motivation					
		Tell students: nothing on the take a copy of Math Task: St division probl "Think of a si Write a story	"Today you e written test the math tas rudents shoul em they wrot tuation descr problem and	are going to s that you have k." d work alone te. ibing the follo then solve it.	show how mu e not already on this probl owing proble As you solve	ch you have learned. Whe em. They wr m: 287 ÷ 14 e the problem	learne en you ite a s =	ed about division. There is finish the End of Unit Test, ituation that reflects the rd each step of your work so
		someone look	ing at your w	ork would ur	nderstand you	ir thinking."		
		Students will	take the End	of Unit Divis	ion Test.			Differentiated Instruction:
unnu	derstanding	Upon complet performance t "Think of a s Write the stor record each st would underst	tion of the wr ask: ituation descr y problem an ep of your we cand your thin	itten test, stu ribing the foll d then solve ork so someo hking."	dents will con lowing proble it. As you sol ne looking at	mplete the em 297 ÷ 14 ve the proble your work	= . em,	English Learners: Have students draw a situation that describes the problem. Have manipulatives available for students.
ntiı	Un.	Scoring Rubri	c:					
Co	for		4	3	2	1		Special Needs:
Lesson	sgies/Techi /Checking	Creates appropriate problem situation	A creative problem situation	Adequate The problem fits the situation	Somewhat Problem rambles or is hard to follow	The problem is nonsensical	-	Have students draw a situation that describes the problem.
	s/ Strate Writing	Records Steps	Detailed description of all steps	All steps are listed in sequence	3 steps listed, or out of sequence	1 or 2 steps listed		available for students.
	ivities/Task ngagement/	Deals with remainders	The precise use of the remainder, with explanation	Remainder used correctly without explanation	Remainder is listed as R	Remainder is not mentioned, ignored		Accelerated Learners:
	Aci estioning/E	Uses efficient strategies	More than one strategy is evident	Uses one strategy completely	False start or incomplete strategies	Counting, drawing relied upon to solve		activities after they finish the performance task.
	Que							

	Lesson Reflection
Teacher	
Reflection	
Evidenced	
by Student	
Learning/	
Outcomes	

Fourth Grade End of Unit Division Test

Name _____

Work each problem in the space provided.

Circle the correct answer for each problem

1.	Ms. Cortez is passing out bookmarks to a group of students in her class. She has a total of 80 bookmarks, and there are 6 students in the group. If she gives each student the same number of bookmarks, how many bookmarks will she have left over?	 A truck driver drives 2800 miles each week. How much does the truck driver drive each day, if he drives the same number of miles each day? A 280 miles
A 1		B 400 miles
B 2		C 700 miles
C 4		D 1400 miles
D 5		
3.	Isabella has 6 times as many pennies as she had 4 months ago. If Isabella has 420 pennies now, how many pennies did she have 4 months ago?	4. A long roller coaster car hold 6 people across each row of seats. The roller coaster car can seat 132 people. How many rows of seats does the roller coaster car have?
A 70		A 20
B 88		B 21
C 90		C 22
D 109		D 23

Name	_
Name	_

5. 126 ÷ 3 =	 What is the first digit in the quotient of 735 ÷ 5?
A 40	A 1
B 42	В 4
C 42 R 1	C 5
D 43	D 7
7. Ms. Ling is organizing 192 science magazine articles she has saved over the years. She has 8 folders. How many articles should she put in each folder so that each folder holds the	 8. There are 224 students in a school marching band. The students march in 8 rows of equal size. How many students are in each row?
same number of articles?	A 24
A 8	B 28
B 18	C 36
C 22	D 42
D 24	
 Yolanda read a 304-page book in 8 days. She read the same number of pages each day. How many pages did she read each day/ 	10. A variety show at the fairgrounds has 5 equal rows of seats. If 150 people can watch the show at one time, how many seats are in each row?
A 28	A 25
B 38	В 30
C 48	C 50
D 2432	D 75

 11. Mr. Simpson divided his class of 25 students into groups of equal size. How many groups did he create? A 2 	12. Colleen has 34 T-shirts. She puts the same number of T-shirts in each of her bags. If she does not have any T-shirts left over, how many bags does she have?
В 4	A 2
C 5	В 3
D 12	C 4
	D 5
13. What type of number is 9?	14. Which number is evenly divisible by 5?
A prime	A 32
B composite	B 54
C mixed	C 71
D even	D 80
15. Which of these is another way to write	16. What are all the factors of 36?
	A 1,36
A 12 X 4 X 2	B 1, 3, 4, 9, 12, 36
B 4 x 8 x 6	
C 3 X 2 X 6	U 1, b, 3b
	D 1, 2, 3, 4, 6, 9, 12, 18, 36
57470	

17. Kevin wants to list the factors of 12.	18. Which statement is true?
His list includes 1. 2, 6, and 12. What	
factors is he missing?	A The only factors of 12 are 1 and 12.
A 3,9	B The only factors of 13 are 1 and 13.
В 8, 4	C The only factors of 14 are 1 and 14.
C 3.4	D The only factors of 15 are 1 and 15.
D 5 7	
19. Which is a prime number?	20. Which is a prime number?
Δ 2	Δ 1Δ
· -	
	B 21
B 4	B 21
	B 21
B 4 C 6	B 21 C 33
B 4 C 6	B 21 C 33
B 4 C 6 D 8	B 21 C 33 D 47
B 4 C 6 D 8	B 21 C 33 D 47

When you finish the test, go back and check your work, then begin working on the Performance-based Assessment.

Teacher's Answer Key

Fourth Grade End of Unit Division Test

- 1. B 2 2. B 400 3. A 70 4. C 22 5. B 42 6. A 1 7. D 24 8. B 28 9. B 38 10. B 30 11. C 5 12. A 2 13. B composite 14. D 80 15. D 3 X 4 X 6 16. D 1, 2, 3, 4, 6, 9, 12, 18, 36 17. C 3, 4 18. B The only factors of 13 are 1 and 13. 19. A 2
- 20. D 47

4th Grade--Division

Final Performance Task

Name:

Think of a situation describing the following problem:

$287 \div 14 =$

Write a story problem and then solve it. As you solve the problem, record each step of your work so someone looking at your work would understand your thinking

Rubric for Mathematics Performance Task

	4	3	2	1
	Exemplary	Adequate	Somewhat	Minimal
Creates	A creative	The problem	Problem	The problem is
appropriate	problem	fits the	rambles or is	nonsensical
problem	situation	situation	hard to follow	
situation				
Records all	Detailed	All steps are	3 steps listed,	1 or 2 steps
steps	description of	listed in	or out of	listed
	all steps	sequence	sequence	
Deals with	The precise	Remainder	Remainder is	Remainder is
remainders	use of the	used correctly	listed as R	not
appropriately	remainder,	without		mentioned,
	with	explanation		ignored
	explanation			
Uses efficient	More than one	Uses one	False start or	Counting,
strategies	strategy is	strategy	incomplete	drawing relied
	evident	completely	strategies	upon to solve

Name:

Menu Activities after Lesson 4

- □ Choice 1: Array Game: Multiplication Pairs
- □ Choice 2: Array Game: Count and Compare
- □ Choice 3: Array Game: Small Array/Big Array
- □ Choice 4: Hungry Ants

Menu Activities after Lesson 9

Games

- □ Choice 5: The Game of Leftovers
- □ Choice 6: Mystery Numbers
- □ Choice 7: Remainder Face Off, p.133

Chapter 7 Math Centers

- □ Choice 8: Know Your Nines
- □ Choice 9: Roomy Dimensions
- □ Choice 10: What's My Fact

Chapter 13 Math Centers

- □ Choice 11: Remainders Rule
- □ Choice 12: Bits and Pieces
- □ Choice 13: Dividend Rolls

Menu Activities after Lesson 14

Chapter 14 Math Centers

- □ Choice 14: Division Day
- □ Choice 15: Division Puzzles
- □ Choice 17: Flowers Factors

Chapter 15 Math Centers

- Choice 18: Prime Time
- □ Choice 16: Divide and Score
- Choice 19: Making Trees

SAUSD Common Core 4th Grade Division Unit