

Practice with Examples

For use with pages 150–156

GOAL

Prove that two lines are parallel and use properties of parallel lines to solve problems

VOCABULARY

Postulate 16 Corresponding Angles Converse If two lines are cut by a transversal so that corresponding angles are congruent, then the lines are parallel.

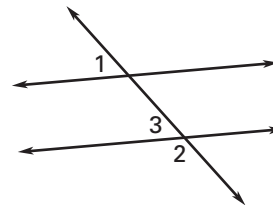
Theorem 3.8 Alternate Interior Angles Converse If two lines are cut by a transversal so that alternate interior angles are congruent, then the lines are parallel.

Theorem 3.9 Consecutive Interior Angles Converse If two lines are cut by a transversal so that consecutive interior angles are supplementary, then the lines are parallel.

Theorem 3.10 Alternate Exterior Angles Converse If two lines are cut by a transversal so that alternate exterior angles are congruent, then the lines are parallel.

EXAMPLE 1**Proving that Two Lines are Parallel**

Prove that lines j and k are parallel.

**SOLUTION**

Given: $m\angle 1 = 53^\circ$

$$m\angle 2 = 127^\circ$$

Prove: $j \parallel k$

Statements	Reasons
1. $m\angle 1 = 53^\circ$ $m\angle 2 = 127^\circ$	1. Given
2. $m\angle 3 + m\angle 2 = 180^\circ$	2. Linear Pair Postulate
3. $m\angle 3 + 127^\circ = 180^\circ$	3. Substitute.
4. $m\angle 3 = 53^\circ$	4. Subtract.
5. $\angle 3 \cong \angle 1$	5. Substitute.
6. $j \parallel k$	6. Corresponding Angles Converse

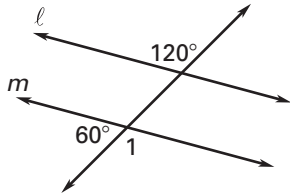
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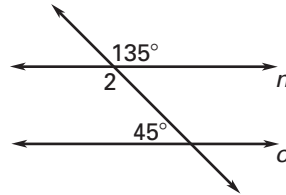
Exercises for Example 1

Prove the statement from the given information.

1. Prove: $l \parallel m$



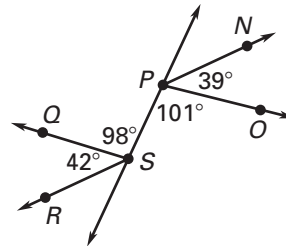
2. Prove: $n \parallel o$



EXAMPLE 2 Identifying Parallel Lines

Determine which rays are parallel.

- Is \vec{PN} parallel to \vec{SR} ?
- Is \vec{PO} parallel to \vec{SQ} ?



SOLUTION

a. Decide whether $\vec{PN} \parallel \vec{SR}$.

$$\begin{aligned} m\angle NPS &= 39^\circ + 101^\circ \\ &= 140^\circ \end{aligned}$$

$$\begin{aligned} m\angle RSP &= 42^\circ + 98^\circ \\ &= 140^\circ \end{aligned}$$

$\angle NPS$ and $\angle RSP$ are congruent alternate interior angles, so $\vec{PN} \parallel \vec{SR}$.

b. Decide whether $\vec{PO} \parallel \vec{SQ}$.

$$m\angle OPS = 101^\circ$$

$$m\angle PSQ = 98^\circ$$

$\angle OPS$ and $\angle PSQ$ are alternate interior angles, but they are not congruent, so $\vec{PO} \parallel \vec{SQ}$ are not parallel.

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Exercises for Example 2

Find the value of x that makes $a \parallel b$.

