Simplify.

SOLUTION:

$$\sqrt{-81} = \sqrt{-1 \cdot 9 \cdot 9}$$
$$= \sqrt{-1} \cdot \sqrt{9^2}$$
$$= 9i$$

SOLUTION:

$$\sqrt{-32} = \sqrt{-1 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2}$$

$$= \sqrt{-1} \cdot \sqrt{2^2} \cdot \sqrt{2^2} \cdot \sqrt{2}$$

$$= i \cdot 2 \cdot 2 \cdot \sqrt{2}$$

$$= 4i\sqrt{2}$$

$$3.(4i)(-3i)$$

SOLUTION:

$$(4i)(-3i) = -12i^2$$

= -12(-1)
= 12

4.
$$3\sqrt{-24} \cdot 2\sqrt{-18}$$

SOLUTION:

$$3\sqrt{-24} \cdot 2\sqrt{-18}$$

$$= 3 \cdot \sqrt{-1 \cdot 2 \cdot 2 \cdot 2 \cdot 3} \cdot 2 \cdot \sqrt{-1 \cdot 2 \cdot 3 \cdot 3}$$

$$= 3 \cdot i \cdot 2 \cdot \sqrt{2} \cdot \sqrt{3} \cdot 2 \cdot i \cdot \sqrt{2} \cdot 3$$

$$= 72 \cdot i^{2} \cdot \sqrt{3}$$

$$= 72 \cdot (-1) \cdot \sqrt{3}$$

$$= -72\sqrt{3}$$

SOLUTION:

$$i^{40} = (i^2)^{20}$$

$$= (-1)^{20}$$

$$= 1$$

6.
$$i^{63}$$

SOLUTION:

$$i^{63} = i^{62} \cdot i$$

$$= (i^2)^{31} \cdot i$$

$$= -1 \cdot i$$

$$= -i$$

Solve each equation.

7.
$$4x^2 + 32 = 0$$

$$4x^{2} + 32 = 0$$

$$4x^{2} = -32$$

$$x^{2} = -8$$

$$x = \pm \sqrt{-8}$$

$$x = \pm \sqrt{-1 \cdot 2 \cdot 2 \cdot 2}$$

$$x = \pm 2i\sqrt{2}$$

$$8. x^2 + 1 = 0$$

SOLUTION:

$$x^{2} + 1 = 0$$

$$x^{2} = -1$$

$$x = \pm \sqrt{-1}$$

$$x = \pm i\sqrt{1}$$

$$x = \pm i$$

Find the values of a and b that make each equation true.

9.
$$3a + (4b + 2)i = 9 - 6i$$

SOLUTION:

Set the real parts equal to each other.

$$3a = 9$$

$$a = 3$$

Set the imaginary parts equal to each other.

$$4b + 2 = -6$$

$$4b = -8$$

$$b = -2$$

10.
$$4b - 5 + (-a - 3)i = 7 - 8i$$

SOLUTION:

Set the real parts equal to each other.

$$4b - 5 = 7$$

$$4b = 12$$

$$b=3$$

Set the imaginary parts equal to each other.

$$-a-3=-8$$

$$-a = -5$$

$$a = 5$$

Simplify.

11.
$$(-1+5i)+(-2-3i)$$

SOLUTION:

$$(-1+5i)+(-2-3i)=(-1-2)+(5i-3i)$$

= -3+2i

12.
$$(7+4i) - (1+2i)$$

SOLUTION:

$$(7+4i)-(1+2i)=7+4i-1-2i$$

= 6+2i

13.
$$(6-8i)(9+2i)$$

SOLUTION:

$$(6-8i)(9+2i)$$

$$= 6(9) + 6(2i) - 8i(9) - 8i(2i)$$

$$= 54 + 12i - 72i - 16i^{2}$$

$$= 54 + 12i - 72i - 16(-1)$$

$$= 54 + 12i - 72i + 16$$

$$= 70 - 60i$$

14.
$$(3+2i)(-2+4i)$$

$$(3+2i)(-2+4i)$$

$$= 3(-2) + 3(4i) + 2i(-2) + 2i(4i)$$

$$= -6 + 12i - 4i + 8i^{2}$$

$$= -6 + 12i - 4i + 8(-1)$$

$$= -6 + 12i - 4i - 8$$

$$= -14 + 8i$$

15.
$$\frac{3-i}{4+2i}$$

SOLUTION:

$$\frac{3-i}{4+2i} = \frac{3-i}{4+2i} \cdot \frac{4-2i}{4-2i}$$

$$= \frac{(3-i)(4-2i)}{(4+2i)(4-2i)}$$

$$= \frac{12-6i-4i+2i^2}{16-4i^2}$$

$$= \frac{12-6i-4i-2}{16-4(-1)}$$

$$= \frac{10-10i}{20}$$

$$= \frac{10(1-i)}{2\cdot 10}$$

$$= \frac{1-i}{2}$$

$$= \frac{1}{2} - \frac{1}{2}i$$

16.
$$\frac{2+i}{5+6i}$$

SOLUTION:

$$\frac{2+i}{5+6i} = \frac{2+i}{5+6i} \cdot \frac{5-6i}{5-6i}$$

$$= \frac{(2+i)(5-6i)}{(5+6i)(5-6i)}$$

$$= \frac{10-12i+5i-6i^2}{25-36i^2}$$

$$= \frac{10-12i+5i-6(-1)}{25-36(-1)}$$

$$= \frac{10-12i+5i+6}{25+36}$$

$$= \frac{16-7i}{61}$$

$$= \frac{16}{61} - \frac{7}{61}i$$

17. **ELECTRICITY** The current in one part of a series circuit is 5 - 3j amps. The current in another part of the circuit is 7 + 9j amps. Add these complex numbers to find the total current in the circuit.

SOLUTION:

Total current =
$$(5-3j)+(7+9j)$$

= $5-3j+7+9j$
= $12+6j$ amps

CCSS STRUCTURE Simplify.

SOLUTION:

$$\sqrt{-121} = \sqrt{-1 \cdot 11 \cdot 11}$$

$$= \sqrt{-1} \cdot \sqrt{11^2}$$

$$= 11i$$

SOLUTION:

$$\sqrt{-169} = \sqrt{-1 \cdot 13 \cdot 13}$$
$$= \sqrt{-1} \cdot \sqrt{13^2}$$
$$= 13i$$

$$\sqrt{-100} = \sqrt{-1 \cdot 10 \cdot 10}$$
$$= \sqrt{-1} \cdot \sqrt{10^2}$$
$$= 10i$$

21. $\sqrt{-81}$

SOLUTION:

$$\sqrt{-81} = \sqrt{-1 \cdot 9 \cdot 9}$$
$$= \sqrt{-1} \cdot \sqrt{9^2}$$
$$= 9i$$

22. (-3i)(-7i)(2i)

SOLUTION:

$$(-3i)(-7i)(2i) = (-3 \cdot -7 \cdot 2)(i \cdot i \cdot i)$$

= $(-3 \cdot -7 \cdot 2)(-1 \cdot i)$
= $-42i$

23. $4i(-6i)^2$

SOLUTION:

$$4i(-6i)^{2} = (4i)(36i^{2})$$
$$= (-144)(i)$$
$$= -144i$$

24. *i*¹¹

SOLUTION:

$$i^{11} = i^{10} \cdot i$$

$$= (i^2)^5 \cdot i$$

$$= -1 \cdot i$$

$$= -i$$

25. i^{25}

SOLUTION:

$$i^{25} = i^{24} \cdot i$$

$$= (i^2)^{12} \cdot i$$

$$= 1 \cdot i$$

$$= i$$

26.(10-7i)+(6+9i)

SOLUTION:

$$(10-7i)+(6+9i)=(10+6)+(-7i+9i)$$

= 16+2i

27. (-3+i)+(-4-i)

SOLUTION:

$$(-3+i)+(-4-i)=(-3-4)+(i-i)$$

= -7

28. (12 + 5i) - (9 - 2i)

SOLUTION:

$$(12+5i)-(9-2i)=12+5i-9+2i$$

= 3+7i

29. (11 - 8i) - (2 - 8i)

$$(11-8i)-(2-8i)=11-8i-2+8i$$

= 9

$$30.(1+2i)(1-2i)$$

SOLUTION:

$$(1+2i)(1-2i) = 1(1) + 1(-2i) + 2i(1) + 2i(-2i)$$

$$= 1 - 2i + 2i - 4i^{2}$$

$$= 1 - 2i + 2i - 4(-1)$$

$$= 1 + 4$$

$$= 5$$

31.
$$(3+5i)(5-3i)$$

SOLUTION:

$$(3+5i)(5-3i) = 3(5)+3(-3i)+5i(5)+5i(-3i)$$

$$= 15-9i+25i-15i^{2}$$

$$= 15-9i+25i+15$$

$$= 30+16i$$

32.
$$(4-i)(6-6i)$$

SOLUTION:

$$(4-i)(6-6i) = 4(6) + 4(-6i) - i(6) - i(-6i)$$

$$= 24 - 24i - 6i + 6i^{2}$$

$$= 24 - 24i - 6i - 6$$

$$= 18 - 30i$$

33.
$$\frac{2i}{1+i}$$

SOLUTION:

$$\frac{2i}{1+i} = \frac{2i}{1+i} \cdot \frac{1-i}{1-i}$$

$$= \frac{2i(1-i)}{(1+i)(1-i)}$$

$$= \frac{2i-2i^2}{1-i^2}$$

$$= \frac{2i+2}{1+1}$$

$$= \frac{2i+2}{2}$$

$$= 1+i$$

34.
$$\frac{5}{2+4i}$$

SOLUTION:

$$\frac{5}{2+4i} = \frac{5}{2+4i} \cdot \frac{2-4i}{2-4i}$$

$$= \frac{5(2-4i)}{(2+4i)(2-4i)}$$

$$= \frac{10-20i}{4-16i^2}$$

$$= \frac{10-20i}{4+16}$$

$$= \frac{10-20i}{20}$$

$$= \frac{1}{2} - i$$

35.
$$\frac{5+i}{3i}$$

$$\frac{5+i}{3i} = \frac{5+i}{3i} \cdot \frac{3i}{3i}$$

$$= \frac{3i(5+i)}{9i^2}$$

$$= \frac{15i+3i^2}{9i^2}$$

$$= \frac{15i+3(-1)}{9(-1)}$$

$$= \frac{15i-3}{-9}$$

$$= \frac{1}{3} - \frac{5}{3}i$$

Solve each equation.

36.
$$4x^2 + 4 = 0$$

SOLUTION:

$$4x^{2} + 4 = 0$$

$$4x^{2} = -4$$

$$x^{2} = -1$$

$$x = \pm \sqrt{-1}$$

$$x = \pm i$$

37.
$$3x^2 + 48 = 0$$

SOLUTION:

$$3x^{2} + 48 = 0$$

$$3x^{2} = -48$$

$$x^{2} = -16$$

$$x = \pm \sqrt{-16}$$

$$x = \pm 4i$$

38.
$$2x^2 + 50 = 0$$

SOLUTION:

$$2x^{2} + 50 = 0$$

$$2x^{2} = -50$$

$$x^{2} = -25$$

$$x = \pm \sqrt{-25}$$

$$x = \pm 5i$$

39.
$$2x^2 + 10 = 0$$

SOLUTION:

$$2x^{2} + 10 = 0$$

$$2x^{2} = -10$$

$$x^{2} = -5$$

$$x = \pm \sqrt{-5}$$

$$x = \pm i\sqrt{5}$$

40.
$$6x^2 + 108 = 0$$

SOLUTION:

$$6x^{2} + 108 = 0$$

$$6x^{2} = -108$$

$$x^{2} = -18$$

$$x = \pm \sqrt{-18}$$

$$x = \pm 3i\sqrt{2}$$

41.
$$8x^2 + 128 = 0$$

$$8x^{2} + 128 = 0$$

$$8x^{2} = -128$$

$$x^{2} = -16$$

$$x = \pm \sqrt{-16}$$

$$x = \pm 4i$$

Find the values of x and y that make each equation true.

42.
$$9 + 12i = 3x + 4yi$$

SOLUTION:

Set the real parts equal to each other.

$$9 = 3x$$

$$3 = x$$

Set the imaginary parts equal to each other.

$$12 = 4y$$

$$3 = y$$

43.
$$x + 1 + 2yi = 3 - 6i$$

SOLUTION:

Set the real parts equal to each other.

$$x+1=3$$

$$x = 3 - 1$$

$$x = 2$$

Set the imaginary parts equal to each other.

$$2y = -6$$

$$y = -3$$

44.
$$2x + 7 + (3 - y)i = -4 + 6i$$

SOLUTION:

Set the real parts equal to each other.

$$2x + 7 = -4$$

$$2x + 7 - 7 = -4 - 7$$

$$2x = -11$$

$$x = -\frac{11}{2}$$

Set the imaginary parts equal to each other.

$$3 - y = 6$$

$$y = -3$$

$$45.5 + y + (3x - 7)i = 9 - 3i$$

SOLUTION:

Set the real parts equal to each other.

$$5 + y = 9$$

$$v = 4$$

Set the imaginary parts equal to each other.

$$3x - 7 = -3$$

$$3x-7+7=-3+7$$

$$3x = 4$$

$$x = \frac{4}{3}$$

$$46. a + 3b + (3a - b)i = 6 + 6i$$

SOLUTION:

Set the real parts equal to each other.

$$a+3b=6\rightarrow (1)$$

Set the imaginary parts equal to each other.

$$3a-b=6 \rightarrow (2)$$

Multiply the second equation by 3 and add the resulting equation to (1).

$$a + 3b = 6$$

$$9a - 3b = 18$$
 (+)

$$10a = 24$$

$$a = \frac{24}{10}$$

$$a = \frac{12}{5}$$

Substitute $a = \frac{12}{5}$ in (1).

$$\frac{12}{5} + 3b = 6$$

$$\frac{12+15b}{5}=6$$

$$\frac{12+15b}{5} \cdot 5 = 6 \cdot 5$$

$$12 + 15b = 30$$

$$15b = 18$$

$$b = \frac{18}{15}$$

$$b = \frac{6}{5}$$

47.
$$(2a-4b)i + a + 5b = 15 + 58i$$

SOLUTION:

Set the real parts equal to each other.

$$a + 5b = 15 \rightarrow (1)$$

Set the imaginary parts equal to each other.

$$2a - 4b = 58 \rightarrow (2)$$

Multiply the first equation by 2 and subtract the second equation from the resulting equation.

$$2a + 10b = 30$$

$$2a - 4b = 58$$
 (-)

$$14b = -28$$

$$b = -2$$

Substitute b = -2 in (1).

$$a+5(-2)=15$$

$$a - 10 = 15$$

$$a = 25$$

Simplify.

48.
$$\sqrt{-10} \cdot \sqrt{-24}$$

SOLUTION:

$$\sqrt{-10} \cdot \sqrt{-24} = \sqrt{-1 \cdot 2 \cdot 5} \cdot \sqrt{-2 \cdot 2 \cdot 2 \cdot 3}$$

$$= \sqrt{-1} \cdot \sqrt{2} \cdot \sqrt{5} \cdot \sqrt{-1} \cdot 2 \cdot \sqrt{2} \cdot \sqrt{3}$$

$$= i \cdot 2 \cdot \sqrt{15} \cdot i \cdot 2$$

$$= -4\sqrt{15}$$

49.
$$4i\left(\frac{1}{2}i\right)^2(-2i)^2$$

$$4i\left(\frac{1}{2}i\right)^{2}(-2i)^{2} = 4i\left(\frac{1}{2}\right)^{2}i^{2}(-2)^{2}i^{2}$$
$$= 4i\left(\frac{1}{4}\right)(-1)(4)(-1)$$
$$= 4i$$

50. *i*⁴¹

SOLUTION:

$$i^{41} = i^{40} \cdot i$$

$$= (i^2)^{20} \cdot i$$

$$= 1 \cdot i$$

$$= i$$

51.(4-6i)+(4+6i)

SOLUTION:

$$(4-6i) + (4+6i) = 4+4-6i+-6i$$

= 8

52. (8-5i)-(7+i)

SOLUTION:

$$(8-5i) - (7+i) = 8-5i-7-i$$

= 1-6i

53. (-6-i)(3-3i)

SOLUTION:

$$(-6-i)(3-3i) = -6(3) - 6(-3i) - i(3) - i(-3i)$$
$$= -18 + 18i - 3i - 3$$
$$= -21 + 15i$$

54.
$$\frac{(5+i)^2}{3-i}$$

SOLUTION:

$$\frac{(5+i)^2}{3-i} = \frac{(5+i)^2}{3-i} \cdot \frac{3+i}{3+i}$$

$$= \frac{(5+i)^2(3+i)}{(3-i)(3+i)}$$

$$= \frac{(25-1+10i)(3+i)}{9+1}$$

$$= \frac{(24+10i)(3+i)}{10}$$

$$= \frac{72+30i+24i+10i^2}{10}$$

$$= \frac{72+30i+24i-10}{10}$$

$$= \frac{62+54i}{10}$$

$$= \frac{31}{5} + \frac{27}{5}i$$

55.
$$\frac{6-i}{2-3i}$$

$$\frac{6-i}{2-3i} = \frac{6-i}{2-3i} \cdot \frac{2+3i}{2+3i}$$

$$= \frac{(6-i)(2+3i)}{(2-3i)(2+3i)}$$

$$= \frac{12+18i-2i-3i^2}{4+9}$$

$$= \frac{12+18i-2i+3}{13}$$

$$= \frac{15+16i}{13}$$

$$= \frac{15}{13} + \frac{16}{13}i$$

56.
$$(-4+6i)(2-i)(3+7i)$$

SOLUTION:

$$(-4+6i)(2-i)(3+7i)$$

$$= (-4(2)-4(-i)+6i(2)+6i(-i))(3+7i)$$

$$= (-8+4i+12i+6)(3+7i)$$

$$= (-2+16i)(3+7i)$$

$$= -2(3)-2(7i)+16i(3)+16i(7i)$$

$$= -6-14i+48i-112$$

$$= -118+34i$$

57.
$$(1+i)(2+3i)(4-3i)$$

SOLUTION:

$$(1+i)(2+3i)(4-3i)$$

$$= (1(2)+1(3i)+i(2)+i(3i))(4-3i)$$

$$= (2+3i+2i-3)(4-3i)$$

$$= (-1+5i)(4-3i)$$

$$= -1(4)-1(-3i)+5i(4)+5i(-3i)$$

$$= -4+3i+20i+15$$

$$= 11+23i$$

$$58. \ \frac{4-i\sqrt{2}}{4+i\sqrt{2}}$$

SOLUTION:

$$\begin{split} \frac{4-i\sqrt{2}}{4+i\sqrt{2}} &= \frac{4-i\sqrt{2}}{4+i\sqrt{2}} \cdot \frac{4-i\sqrt{2}}{4-i\sqrt{2}} \\ &= \frac{\left(4-i\sqrt{2}\right)\left(4-i\sqrt{2}\right)}{\left(4+i\sqrt{2}\right)\left(4-i\sqrt{2}\right)} \\ &= \frac{\left(16-2-8i\sqrt{2}\right)}{16+2} \\ &= \frac{14-8i\sqrt{2}}{18} \\ &= \frac{7}{9} - \frac{4i\sqrt{2}}{9} \end{split}$$

59.
$$\frac{2-i\sqrt{3}}{2+i\sqrt{3}}$$

SOLUTION:

$$\frac{2-i\sqrt{3}}{2+i\sqrt{3}} = \frac{2-i\sqrt{3}}{2+i\sqrt{3}} \cdot \frac{2-i\sqrt{3}}{2-i\sqrt{3}}$$

$$= \frac{(2-i\sqrt{3})(2-i\sqrt{3})}{(2+i\sqrt{3})(2-i\sqrt{3})}$$

$$= \frac{(4-3-4i\sqrt{3})}{4+3}$$

$$= \frac{1-4i\sqrt{3}}{7}$$

$$= \frac{1}{7} - \frac{4i\sqrt{3}}{7}$$

60. **ELECTRICITY** The impedance in one part of a series circuit is 7 + 8j ohms, and the impedance in another part of the circuit is 13 - 4j ohms. Add these complex numbers to find the total impedance in the circuit.

Total impedance =
$$7 + 8j + 13 - 4j$$

= $20 + 4j$ ohms

ELECTRICITY Use the formula $V = C \cdot I$.

61. The current in a circuit is 3 + 6i amps, and the impedance is 5-i ohms. What is the voltage?

SOLUTION:

We know that voltage can be calculated by

 $V = C \cdot I$

V = Voltage

C = current

I = impedance

$$V = (3+6j)(5-j)$$

$$=15-3j+30j+6$$

$$=21+27j$$

Therefore, the voltage is 21+27j Volts.

62. The voltage in a circuit is 20 - 12i volts, and the impedance is 6 - 4i ohms. What is the current?

SOLUTION:

We know that voltage can be calculated by

 $V = C \cdot I$

V = Voltage

C = current

I = impedance

$$20-12i = I(6-4i)$$

$$I = \frac{20 - 12j}{6 - 4j}$$

$$I = \frac{20 - 12j}{6 - 4j}$$

$$= \frac{20 - 12j}{6 - 4j} \cdot \frac{6 + 4j}{6 + 4j}$$

$$= \frac{(20 - 12j)(6 + 4j)}{(6 - 4j)(6 + 4j)}$$

$$= \frac{120 + 80j - 72j + 48}{36 + 16}$$

$$= \frac{168 + 8j}{52}$$

$$= \frac{42}{13} + \frac{2}{13}j$$

Therefore, the current is $\frac{42}{13} + \frac{2}{13}j$ Amps.

63. Find the sum of $ix^2 - (4+5i)x + 7$ and $3x^2 + (2+6i)$

SOLUTION:

$$ix^{2} - (4+5i)x + 7 + 3x^{2} + (2+6i)x - 8i$$

$$= (3+i)x^{2} - 5ix - 4x + 2x + 6ix + 7 - 8i$$

$$= (3+i)x^{2} + ix - 2x + 7 - 8i$$

$$= (3+i)x^{2} + (-2+i)x + 7 - 8i$$

64. Simplify $[(2+i)x^2 - ix + 5 + i] - [(-3+4i)x^2 + (5-4i)x^2 +$ 5i)x - 61.

SOLUTION:

$$[(2+i)x^{2} - ix + 5 + i] - [(-3+4i)x^{2} + (5-5i)x - 6]$$

$$= [(2+i)x^{2} - ix + 5 + i] - (-3+4i)x^{2} - (5-5i)x + 6$$

$$= 2x^{2} + ix^{2} - ix + 5 + i + 3x^{2} - 4ix^{2} - 5x + 5ix + 6$$

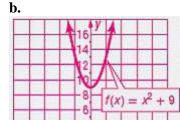
$$= 5x^{2} - 3ix^{2} + i - 5x + 4ix + 11$$

$$= (5-3i)x^{2} + (-5+4i)x + i + 11$$

- 65. MULTIPLE REPRESENTATIONS In this problem, you will explore quadratic equations that have complex roots. Use a graphing calculator.
 - a. Algebraic Write a quadratic equation in standard form with 3i and -3i as its roots.
 - b. Graphical Graph the quadratic equation found in part a by graphing its related function.
 - c. Algebraic Write a quadratic equation in standard form with 2 + i and 2 - i as its roots.
 - d. Graphical Graph the related function of the quadratic equation you found in part c. Use the graph to find the roots if possible. Explain.
 - e. Analytical How do you know when a quadratic equation will have only complex solutions?

SOLUTION:

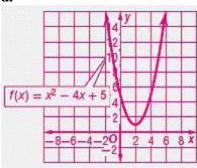
a. Sample answer: $x^2 + 9 = 0$



c. Sample answer: $x^2 - 4x + 5 = 0$

2 4

d.



- **e.** Sample answer: A quadratic equation will have only complex solutions when the graph of the related function has no *x*-intercepts.
- 66. **CCSS CRITIQUE** Joe and Sue are simplifying (2*i*) (3*i*)(4*i*). Is either of them correct? Explain your reasoning.

SOLUTION:

Sue;
$$i^3 = -i$$
, not -1 .

67. **CHALLENGE** Simplify $(1 + 2i)^3$.

SOLUTION:

$$(1+2i)^{3} = (1+2i)(1+2i)(1+2i)$$

$$= (1-4+4i)(1+2i)$$

$$= (-3+4i)(1+2i)$$

$$= -3-6i+4i-8$$

$$= -11-2i$$

68. **REASONING** Determine whether the following statement is *always*, *sometimes*, or *never* true. Explain your reasoning.

Every complex number has both a real part and an imaginary part.

SOLUTION:

Sample answer: Always. The value of 5 can be represented by 5 + 0i, and the value of 3i can be represented by 0 + 3i.

69. **OPEN ENDED** Write two complex numbers with a product of 20.

SOLUTION:

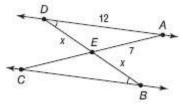
Sample answer: (4 + 2i)(4 - 2i)

 WRITING IN MATH Explain how complex numbers are related to quadratic equations.

SOLUTION:

Some quadratic equations have complex solutions and cannot be solved using only the real numbers.

71. **EXTENDED RESPONSE** Refer to the figure to answer the following.



- **a.** Name two congruent triangles with vertices in correct order.
- **b.** Explain why the triangles are congruent.
- **c.** What is the length of \overline{EC} ? Explain your procedure.

SOLUTION:

- a. $\triangle CBE \cong \triangle ADE$
- **b.** $\angle AED \cong \angle CEB$ (Vertical angles)

 $\overline{DE} \cong \overline{BE}$ (Both have length x.) $\angle ADE \cong \angle CBE$ (Given)

Consecutive angles and the included side are all congruent, so the triangles are congruent by the ASA Property.

c. $\overline{EC} \cong \overline{EA}$ by CPCTC (corresponding parts of congruent triangles are congruent.) EA = 7, so EC = 7.

72.
$$(3+6)^2$$
 =

$$\mathbf{A} \ 2 \times 3 + 2 \times 6$$

B 9^2

$$C 3^2 + 6^2$$

D
$$3^2 \times 6^2$$

SOLUTION:

$$(3+6)^2=9^2$$

So, the correct option is B.

73. **SAT/ACT** A store charges \$49 for a pair of pants. This price is 40% more than the amount it costs the store to buy the pants. After a sale, any employee is allowed to purchase any remaining pairs of pants at 30% off the store's cost.

How much would it cost an employee to purchase the pants after the sale?

F \$10.50

G \$12.50

H \$13.72

J \$24.50

K \$35.00

SOLUTION:

Let *x* be the original amount of the pants.

\$49 = 40%x + x

\$49 = 0.4x + x

\$49 = 1.4x

x = \$35

 $\$35 \cdot \frac{30}{100} = \10.50

\$35 - \$10.50 = \$24.50

So, the correct option is J.

74. What are the values of *x* and *y* when (5 + 4i) - (x + yi) = (-1 - 3i)?

A
$$x = 6, y = 7$$

B
$$x = 4, y = i$$

$$C x = 6, y = i$$

D
$$x = 4, y = 7$$

SOLUTION:

Set the real parts equal to each other.

$$5 - x = -1$$

$$x = 6$$

Set the imaginary parts equal to each other.

$$4 - y = -3$$

$$y = 7$$

So, the correct option is A.

Solve each equation by factoring.

75.
$$2x^2 + 7x = 15$$

SOLUTION:

Write the equation with right side equal to zero.

$$2x^2 + 7x - 15 = 0$$

Find factors of 2(-15) = -30 whose sum is 7.

$$10(-3) = -30$$
 and $10 + (-3) = 7$

$$2x^2 + 10x - 3x - 15 = 0$$

$$2x(x+5)-3(x+5)=0$$

$$(x+5)(2x-3)=0$$

$$\Rightarrow x+5=0$$
 or $2x-3=0$

$$\Rightarrow$$
 $x = -5$ or $x = \frac{3}{2}$

Therefore, the roots are -5 and $\frac{3}{2}$.

76.
$$4x^2 - 12 = 22x$$

SOLUTION:

Write the equation with right side equal to zero.

$$4x^2 - 22x - 12 = 0$$

Find factors of 4(-12) = -48 whose sum is -22.

$$-24(2) = -48$$
 and $2 + (-24) = -22$

$$4x^2 - 24x + 2x - 12 = 0$$

$$4x(x-6)+2(x-6)=0$$

$$(x-6)(4x+2)=0$$

$$\Rightarrow x-6=0 \text{ or } 4x+2=0$$

$$\Rightarrow x = 6$$
 or $x = -\frac{1}{2}$

Therefore, the roots are $-\frac{1}{2}$ and 6.

77
$$6x^2 = 5x + 4$$

SOLUTION:

Write the equation with right side equal to zero.

$$6x^2 - 5x - 4 = 0$$

Find factors of 6(-4) = -24 whose sum is -5.

$$-8(3) = -24$$
 and $3+(-8) = -5$

$$6x^2 - 8x + 3x - 4 = 0$$

$$2x(3x-4)+1(3x-4)=0$$

$$(2x+1)(3x-4)=0$$

$$\Rightarrow$$
 2x + 1 = 0 or 3x - 4 = 0

$$\Rightarrow x = -\frac{1}{2}$$
 or $x = \frac{4}{3}$

Therefore, the roots are
$$-\frac{1}{2}$$
 and $\frac{4}{3}$.

Determine whether each trinomial is a perfect square trinomial. Write yes or no.

78.
$$x^2 - 12x + 36$$

SOLUTION:

 $x^2-12x+36$ can be written as $(x-6)^2$.

So, $x^2 - 12x + 36$ is a perfect square trinomial. The answer is "yes".

79.
$$x^2 + 8x - 16$$

SOLUTION:

We cannot write the given trinomial as the perfect square format. So, the answer is "no".

80.
$$x^2 - 14x - 49$$

SOLUTION:

We cannot write the given trinomial as the perfect square format. So, the answer is "no".

81.
$$x^2 + x + 0.25$$

SOLUTION:

 $x^{2} + x + 0.25$ can be written as $(x + 0.5)^{2}$.

So, $x^2 + x + 0.25$ is a perfect square trinomial. The answer is "yes".

82.
$$x^2 + 5x + 6.25$$

SOLUTION:

 $x^{2} + 5x + 6.25$ can be written as $(x + 2.5)^{2}$.

So, $x^2 + 5x + 6.25$ is a perfect square trinomial. The answer is "yes".