# 8th grade Math Team Summer Packet

## Before starting 8th grade math team you should be able to:

- Simplify integer expressions
- · Solve multi-step equations and inequalities
- Apply the Pythagorean Theorem and know the common Pythagorean Triples
- Write square roots in simplest radical form
- · Find the area of 2-D figures
- Find surface area and volume of 3-D geometric shapes
- + Graph linear equations from slope-intercept form and standard form
- Write the equation of a line in slope-intercept form, given a graph
- Graph the a line, given the equation in slope-intercept form
- \* Solve a system of linear equations by graphing, substitution, and elimination
- Convert from fractions to decimals to percents
- Convert repeating decimals to fractions
- Convert from base 10 to other bases and vice versa
- Attempt to work all the problems on the tournament tests in this packet
- \* memorize factorials up to 10 (timed quiz 1st week)
- + memorize all square roots up to 20 and cube roots up to 10 (timed quiz 1st week)
- memorize common fraction decimal percent equivalents (timed quiz 1st week)
- Chapters 1-3 Pre-Test (will be collected the first day- write final answers on test paper, but attach work that has been shown on separate paper. Failure to follow directions will result in a 0.)

Your assignment is to review all of the material in this packet over the summer and to complete all of the problems. These are concepts you should have learned in 7th grade math team class, so I will not be taking anytime in class to review these concepts. This entire packet will not be taken up for a grade, but you will be expected to know the material well that the worksheets cover. The final worksheet in the packet is a <a href="Pre-Test for Chapters 1-3">Pre-Test for Chapters 1-3</a> in the Algebra book. You will be turning that in the first day of school and I will use this to determine what concepts covered in those chapters that I will need to teach. The Pre-Test will be collected for a grade before you take the test, once you have a chance to correct any mistakes. You will then take the actual Chapters 1-3 Test that will count for a test grade.

All of the worksheets in this packet should be completed <u>WITHOUT</u> the aid of a calculator. Be sure to bring the completed Ch 1-3 Pre-Test to school the first day.

I look forward to meeting you in August.

Mb. Thurer

## Math Team Grade 8 - Things to Know

Be prepared to take a quiz on this material the First Week of school Write each as a percent, decimal, and fraction.

$$\frac{1}{2}$$
 = .5=50%

$$\frac{1}{3}$$
 = .3 $\frac{1}{3}$  %

$$\frac{2}{3} = .6\overline{6}$$
,  $= 66\overline{3}$  %

$$\frac{1}{5}$$
 =.2=20%

$$\frac{2}{5}$$
 = 4=40%

$$\frac{1}{6} = .1\overline{6} = 16\overline{3} \%$$

$$\frac{5}{6} = .83 = 83 \frac{1}{3} \%$$

$$\frac{1}{8}$$
 = .125=12  $\frac{1}{2}$  %  $\frac{3}{8}$  = .375=37  $\frac{1}{2}$  %

$$\frac{5}{8} = .625 = 62\frac{1}{2}\%$$

$$\frac{7}{8} = .875 = 87 \frac{1}{2} \%$$

$$\frac{1}{9} = .11$$
 = 11 9 %

$$\frac{2}{9} = .2\overline{2} = .22 \frac{2}{9} \%$$

$$\frac{4}{9} = .4\overline{4} = 44 \frac{4}{9} \%$$

$$\frac{1}{12} = .08\overline{3} \ 8\overline{3} \%$$

$$\frac{5}{12} = .41 \frac{2}{6} = 41 \frac{2}{3} \%$$

$$\frac{7}{12} = .58\overline{3} : 58\overline{3}$$

$$\frac{11}{12} = .91\overline{b} = .91\overline{3} \%$$

## Pythagorean Theorem : $a^2 + b^2 = c^2$

## Triples:

3, 4, 5

9,40,41

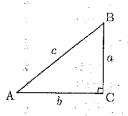
5, 12, 13

11, 60, 61

7, 24, 25

20, 21, 29

8, 15, 17



Polygons	# of sides	# of angles	# of vertices	# of diagonal s
triangle	3	3	3	0
quadrilateral	4	4	4	2
pentagon	5	5	5	5
hexagon	6	6	6	9
heptagon	7	7	7	14
octagon	8	8	8	20
nonagon	9	9	9	27
decagon	10	10	10	35
dodecagon	12 .	12	12	54
icosagon	20	20	20	170

## Exponents

02=0	1 <sup>2</sup> =1	2 <sup>2</sup> =4	3 ² =9	4 <sup>2</sup> =16	5 <sup>2</sup> = 25	6 <sup>2</sup> =36
$7^2 = 49$	8 <sup>2</sup> = 64	9 <sup>2</sup> = 81	$10^2 = 100$	11 <sup>2</sup> =121	$12^2 = 144$	13 <sup>2</sup> =169
14 <sup>2</sup> = 196	15 <sup>2</sup> = 225	16 <sup>2</sup> =256	17² = 289	18 <sup>2</sup> =324	19 <sup>2</sup> = 361	20 <sup>2</sup> = 400
21 <sup>2</sup> =441	25 <sup>2</sup> = 625	30 <sup>2</sup> = 900	35 <sup>2</sup> = 1225	40 <sup>2</sup> =1600	45 <sup>2</sup> = 2025	55 <sup>2</sup> = 3025
$65^2 = 4225$	$1^3 = 1$	$2^3 = 8$	$3^3 = 27$	$4^3 = 64$	$5^3 = 125$	6³ = 216
$7^3 = 343$	$8^3 = 512$	9³ = 729	10 <sup>3</sup> = 1000	$11^3 = 1331$	$12^3 = 1728$	20³ = 8000

## Square Roots and Cube Roots

$$\sqrt{4} = 2$$

$$\sqrt{9} = 3$$

$$\sqrt{16} = 4$$

$$\sqrt{25} = 5$$

$$\sqrt{49} = 7$$

$$\sqrt{64} = 8$$

$$9 \quad \sqrt{100} = 10 \quad \sqrt{121} = 11$$

$$\sqrt{144} = 12$$

$$\sqrt{169} = 13$$
  $\sqrt{196} = 14$ 

$$\sqrt{225} = 15$$

$$\sqrt{256} = 16$$

$$\sqrt{289} = 17$$

$$\sqrt{324} = 18$$

$$\sqrt{361} = 19$$

$$\sqrt{400} = 20 \sqrt{1} = 1$$

$$\sqrt[3]{27} = 3$$

$$\sqrt[3]{343} = 7$$
  $\sqrt[3]{512} = 8$ 

$$\sqrt[3]{1000} = 10$$

## Formulas

Circle: circumference = 
$$2\pi r$$
 or  $\pi d$ 

Circle: circumference = 
$$2\pi r$$
 or  $\pi d$  area =  $\pi r^2 \pi$  = 3.14 or 22/7

Triangle: area = 
$$\frac{1}{2}$$
 bh

Square: 
$$area = s^2$$

perimeter 4s

Rectangle: area = lw

perimeter = 21 + 2w

Trapezoid: area =  $\frac{1}{2}$  h(b<sub>1</sub> + b<sub>2</sub>)

Parallelogram: area = bh

Cube



Sphere

surface area = 6s²

Volume = 4/3πr³

Surface Area =  $4\pi r^2$ 

Cone surface (



Volume =  $1/3 \pi r^2 h$ 

area = πrs.+πr²

Volume = πr2h

Surface Area =  $2\pi r^2 + 2\pi rh$ 

Rectangular solid

surface .

volume = lwh

Cylinder

area = 2!w + 2wh + 21h

Interest = prt (Interest = principal x rate x time)

Distance = rt (distance = rate x time)

Percent of change = change/original

Prime Numbers between 1 and 150: 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97, 101, 103, 107, 109, 113, 127, 131, 137, 139, 149

## Factorials

$$5! = 120$$

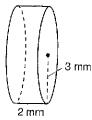
$$91 = 362.880$$

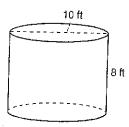
$$n! = 1 \times 2 \times 3 \times ... \times n$$

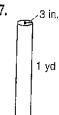
## In Exercises 1–14, use 3.14 for $\pi$ .

- 1. Find the volume of a cylinder with a radius of 2 meters and a height of 4 meters.
- 3. Find the volume of a cylinder with a diameter of 16 inches and a height of 4 inches.
- 2. Find the volume of a cylinder with a base area of  $625\pi$  in.<sup>2</sup> and a height of 25 inches.
- 4. Find the volume of a cylinder with a circumference of  $25\pi$  and a height of 7.5 cm. (Hint: Use the circumference to find the radius.)

In Exercises 5-8, find the volume of the cylinder.

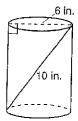




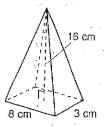


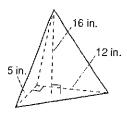
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8.

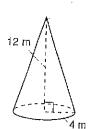


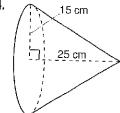
in Exercises 1-4, find the volume of the solid. Use 3.14 for  $\pi\,.$  Round your results to one decimal place.





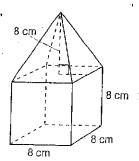
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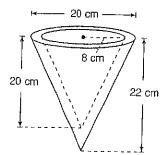


In Exercises 7-9, find the volume of the solid. Use 3.14 for  $\pi\,.$  Round your result to one decimal place.

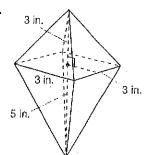
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8.

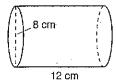


9.

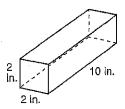


In Exercises 1–6, find the surface area of the right prism or right cylinder. Use 3.14 for  $\pi$  . Round your results to one decimal place.

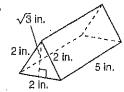
1.



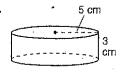
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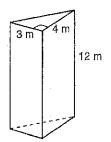
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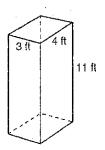
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5.



6.



## Repeating Decimals Worksheet

Directions: Convert each decimal to a fraction.

1. o. <del>c</del>	2. 2. <del>c</del>	3. c.54	·4. , -6.2
5. 0.45	6. <u> </u>	.7. 0.46	87, 6
9	10. 0.583	11. . 285714	12
13. 0.2	14. 0.7	15.	16.
17.	18	0.4	20.
21. 7.83	22. 0.083	232.06	24. 0.72

Example: 
$$\frac{10 \, n}{9} = 1.66$$
 $\frac{9 \, n}{9} = 1.5$ 
 $\frac{15}{9} = \frac{15}{9}$ 
 $\frac{15}{9} = \frac{15}{9} = \frac{15}{9}$ 

This is why the method Mrs. Collay Shaved you works

 $\frac{15}{9} = \frac{15}{90} = \frac{15}{6}$ 

Note: if 2 digits repeat, X by 100; 3- X by 1000, etc.
This step removes the repeating part of the decimal

## Changing Bases Worksheet

Change each base 10 numeral to base 2.

1, 54

2.384

3, 10

4.516

5.40

Change each base 10 numeral to base 4.

6.38

7.2049

8. 12

9, 564

10.388

Change each base 10 numeral to base 5.

11. 488

12. 15

13, 5017

14, 283

15.5000

Change each base 10 numeral to base 8.

18 247

17, 317

18. 56

19.27

20, 687

Example change 31 to base 2

Mrs. Colley may have shown you adofterent method to do these. I don't care what method you use

# How Did the Light Dress Up Hor the Costune Party?

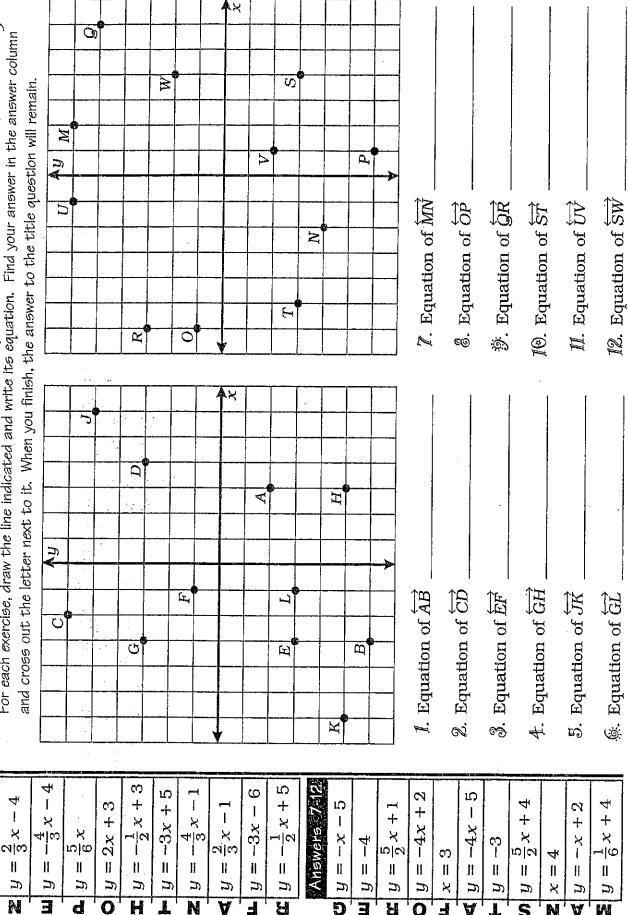
Answers 1-6

S

Ц

2

For each exercise, draw the line indicated and write its equation. Find your answer in the answer column



work to all (m =



# What Vid the Teacher Do With Ogar's Cheese Report?

answer. When you finish, the remaining letters will tell you the answer to the title question. Solve each system of equations by graphing. Cross out the letters above each correct

 $\frac{1}{3}\chi + 2$ 

11

Z

[]

J

-x + 4

II

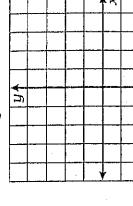
7

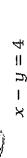
 $y = \frac{3}{2}x - 1$ 

7

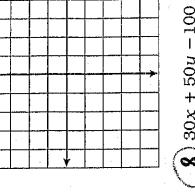


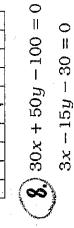
4/3x + y = 0





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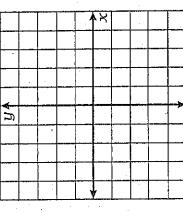
20x + 80y = 0

-8x - 3y = 12

**6.** 7x - 5y = 20

(5) -3x + 4y =

(7) - x - 4y = 12



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(4,3)

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Systems of Linear Equation Solving Systems by Graphi	

1.	How many integ a. 7	gers satisfy both 3-x≤ 2 and b. infinitely many		d. 6
2.	What is 243 expre a. 11110011	essed as a binary number b. 101		d. 11101110
3.	What is the slope	of the line passing throug	gh (2,3) and (	-3,2) ?
	a. 5	b. 1	c. $\frac{1}{5}$	d1
4.	A recipe for 12 cu	$\frac{1}{1}$ cups	s of sugar. H	low many cups of sugar should
	be used if 20 cup	cakes are being made v	vith this same	e recipe?
	a. $2\frac{1}{2}$	b. $2\frac{1}{4}$	c. $2\frac{3}{4}$	d. 2
5.	Find the greatest a. 504a³b⁴	common factor 24 a²b, 5 b. 18ab	66a³b4, and 7 c. 12ab²	
6.	23.5% were straw	perry, 12.5% were peach, many Jolly Ranchers we	20% were a	
7.	Lilli and Nora trave boat from its starti		n 8 miles sou	th in their boat. How far is the
	a. 48 miles		c. 14 miles	d. 2 miles
8.	Solve for x. $\frac{5}{8}x = \frac{1}{8}$	<del>7</del> .		
	a. $-\frac{15}{28}$	b. $\frac{15}{28}$	c. $\frac{28}{15}$	d. $\frac{-28}{15}$
9.	$3\sqrt{\sqrt{2}}60$ a. $2^3$			
	a. 2 <sup>3</sup>	b. 2 <sup>5</sup>	c. 24	d. 20

10. A rectangle with dimensions 225 by 196 has the same area as a square. What is the perimeter of the square?

a. 210

b. 421

c. 116

d. 840

		hletes competing in the t medal be awarded?	rack finals. Ir	how mo	any ways can the gold
	504	•	c. 362,880	d. 3	
		% raise each year for thre raises if his starting salary			
a. S	\$20,736	b. \$1,600	c. \$17,280	d. \$ 2,00	00
13.x @ y = a. 7		y² and x # y = 3y + 4x. b. 841	Find [4 @ (3 c. 784		
14.If the a	verage of	n numbers is <mark>n, the thei</mark> r s	um is:		·
a.	$\frac{n}{2}$	b. n <sup>2</sup>	c. 2n	d.n	
and Bo	iiley togeth	an orchard. Bailey owns er own 70% of the orcha b. 50 acres	rd, how man	y acres c	does Grace own?
a s	5% of what 520	b. 32.5		5 d	. 155
		wing has the largest valu b. 2x[(9-6)-3]	· ·	(9-6)]-3	d. (2x-9)-(6-3)
2.	% of 14% o	•	, mo.o		00
ay 4 5	1.58	b4508	c. 4.508	d045	08
19. What is	the quotie	nt when 0.48 is divided b	9 0.016°		•
a. (	).3	b. 3	c. 30	d. 300	
**	ck of eight ack of qua	quarters measures exact	ly one inch, l	now mar	ny inches high would a
		b. 12.5 inches	с. 38	inches	d. 96 inches
21.How m	any eighth	s are in 5.75 ?			
- a; 2	23	b. 46	c. 120	(	d. 63
p-		<del>-</del>			

- 22. What is the average of  $\frac{1}{4}$  and  $\frac{1}{6}$  ?
  - a.  $\frac{5}{12}$  b.  $\frac{1}{5}$

- c.  $\frac{1}{10}$  d.  $\frac{5}{24}$
- 23. If the area of a square is 1024, what is the perimeter of the square?
  - a. 128
- b. 32

- c. 256
- d. 64
- 24. In a school of 910 students, the ratio of boys to girls is 5:2. How many more boys than girls are in the school?
  - a. 650
- b. 260

- c. 390
- d. 455

- 25.  $(\frac{1}{3} \frac{1}{4}) (\frac{1}{6} \frac{1}{12})$ 
  - a.  $\frac{1}{12}$ 
    - b. 0

- c.  $\frac{1}{6}$
- d. 6

## <u>Tie Breakers</u>

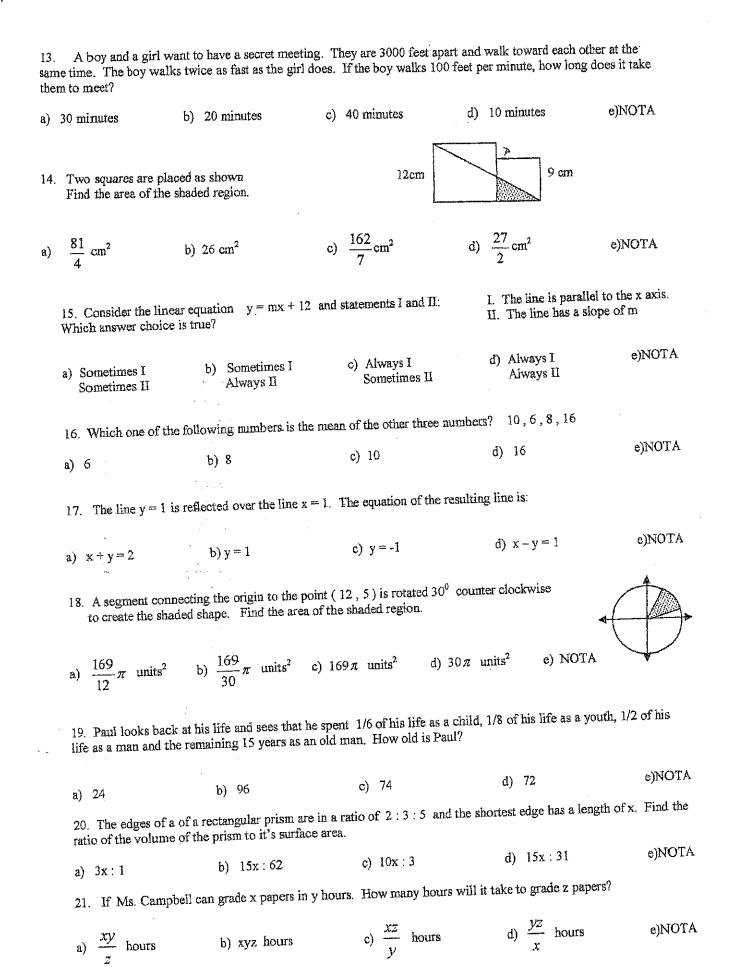
T1. 
$$\frac{1}{10} + \frac{1}{5} + \frac{1}{10} + \frac{1}{5} + \frac{1}{10} + \frac{1}{5} + \frac{1}{10} + \frac{1}{5} =$$

- T2. (10% of 20) minus (20% of 10)
- T3. Sally drove 238 miles in 4 hours and 15 minutes. What was her average speed in miles per hour?

## 2008 Hoover HS Math Tournament Pre-Algebra Written Test

1. If r > 1 which one of the following must also be true?

a) $r+1=2$	b) $r-1=0$	c) $r+1>2$	d) r = 2	e)NOTA
2. Evaluate the	e following: 44 - 33 ÷ 11 -	1 × 2		
a) 27	b) 2	c) 40	d) 39	e)NOTA
3. If $a = b$ and	b = 2c, find $a + b + c$ when	c = 6	•	
a) 18	b) 24	c) 30	d) 36	e)NOTA
4. Solve: 2(2	(x-2(2+2)) = 8x			
a) 4	b) 2	c) -2	d) 8	e)NOTA
5. A circle with	center at the origin passes th	rough the point (3,4). W	hat is the diameter of the cir	rcle?
a) 7 units	b) 10 units	c) 5 units	d) 12 units	e)NOTA
6 Which guadr	ant does the graph of $y = -3$	e = 3 NOT page through?	)	
a) I	b) II	ė) III	d) IV	e)NOTA
4) 1 <sub>k.</sub>	oy u	<i>v)</i> III.		
7. The following	ng equation has two answers.	What is the sum of the ans	swers? $(a+2)(a-2)=$	21
a) 4	b) 10	c) 7	d) 0	e)NOTA
8. Find the tota	l number of triangles in the d	rawing		•
** ** ** **				
a) 7	b) 9	c) 4	d) 8	e)NOTA
t t N		0.41	1100	
Ą.	ter a building has a single lett	*		
a) 36 <sub>[</sub>	b) 326	c) 3026	d) 26000	e) NOTA
# 10 FF 3 d	Programme and the street control			
10. Find the sur	rface area of a cube that has a	volume of cm .		
a) $\frac{8}{3}$ cm <sup>2</sup>	b) 6 cm <sup>2</sup>	c) $\frac{1}{3}$ cm <sup>2</sup>	d) $\frac{8}{27}$ cm <sup>2</sup>	e)NOTA
12 How many in	teger solutions does the equat	ion have? $ 2x-4  < 2$		,
	osor sommons aces me equal	100 mayor  2x -4  < 2	· -	<i>-</i> -
a) 6	b) 3	c) 2	d) 1	e)NOTA



23. Sou	up and salad cost \$12. f you bought three so	Salad and a sand ups and three sala	wich cost ds and thre	\$13. Soup an se sandwiches	nd a sandwich s?	cost \$11.	What would the total
a) \$54		\$108	c)			\$18	e)NOTA
24. W	nich of the quadrants	of the coordinate p	lane does	not contain a	n answer to t	he function:	$f(x) = \frac{2}{x-3} - 4$
a) I		II	c)		d)	IV	e)NOTA
25. The	e Braille alphabet use:	s a series of six do	ts that are	either raised	or recessed to	form each	symbol.
Six dots	s are always used and	form a rectangle a	is shown.	• Using	this informat	ion, how m	any different symbols
can be f	formed?					4	
a) 12	b)	24	c)	48	d)	64	e)NOTA
TB1 % TB2 :: TB3 %	Find the sum of the The 4 <sup>th</sup> root of a run Find the sum of the	mber is ½. Find t unique, positive, i	he number	tors of 81.			

## Chapters 1-3

# Show all work neatly and numbered on your own sheet of paper. Write final answers in the blanks provided.

Simplify.

1. 
$$\frac{30 \div 5 - 2}{2(5 - 3)}$$

2. 
$$\frac{-30}{-\frac{1}{2}}$$

3. 
$$56 \div 8 - 6 \div 2$$

$$4...9 - 1.02 + .54$$

5. 
$$-7(-5r-1) + 2(4-3r)$$

6. 
$$|3-1|-|1-3|$$

# Evaluate each expression if r = -2, $s = \left| -3 \right|$ , $t = \frac{1}{3}$ , and y = 6.

7. 
$$-4r(t + v)$$

$$8. \quad \frac{st + 4\nu}{r - 3}$$

# Solve each equation. If it is an identity or has no solution, say so.

9. 
$$|a| = 8$$

10. 
$$|b| = -6$$

11. 
$$15 - (5 - n) = 1$$

12. 
$$100 - d = 0$$

13. 
$$-12j = -84$$

$$12.100 - 4 - 0$$

14. 
$$4 + \frac{5}{2}(g - 3) = 24$$

15. 
$$-5(2h-1)-8=7$$

16. 
$$\frac{2}{5}x+16=0$$

17. 
$$-2(3-b) = 2b \pm 6$$

15. \_\_\_\_\_

18. 
$$3(2m-\frac{1}{3})=2(3m-\frac{1}{2})$$

|--|

19. 
$$\frac{5}{6}(7x-15) = 4x+4$$

10	14
19,	11



Solve each equation. You MUST define each unknown quantity, write an equation and solve it. Doing them in a chart is encouraged, but optional. Write the final answer(s) only on the blank provided and include the correct units of measure (label).

- 20. Six times a number, decreased by five, is -14. Find the number.
- 21. The longest side of a triangle is 8 cm longer than the shortest side and 5 cm longer than the third side. If the perimeter is 56 cm, find the lengths of all 3 sides.
- 22. The numbers of fish in Rick and Lisa's aquarium are consecutive integers. When they each had three less fish, together they had 15 fish. How many fish does each have now if Lisa has more fish?
- 23. When Kate worked 10 h overtime she earned \$8 more than one third the amount she earns for 40 h of work at her usual rate. If her overtime rate is \$2.40 more per hour that her usual rate, find her overtime rate (the amount of money she makes for each overtime hour).
- 24. Twin Cinema I seats 150 more people that Twin Cinema II. If the cinemas seat 1250 people altogether, find the number of seats in Cinema II.
- 25. Zach's last test score was 30 points less than twice his first score. What was his first score if the sum of the two scores is 150?

# BONUS QUESTION (5pts cotra)

On the first of three tests, Katie scored 72 points. On the third test, her score was 1 point more than on the second test. Her average on the three tests was 83. What were her scores on the second and third tests?

20.	,	15	)
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21.		(60
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23.	•	_(5	
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24	5)	ļ
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25.

