

Graph the function and identify intervals on which the function is increasing, decreasing or constant.

30)  $f(x) = |x+1| + |x-1| - 3$

33)  $g(x) = 3 - (x-1)^2$

Use your calculator to find all local maxima and minima and the values of  $x$  where they occur.

43)  $h(x) = -x^3 + 2x - 3$

45)  $f(x) = x^2 \sqrt{x+4}$

State whether the function is odd, even, or neither. Support graphically and confirm algebraically.

A)  $f(x) = 4x^2$

Graphically: Even Function  
Algebraically:  $f(1) = 4(1)^2 = 4$   
 $f(-1) = 4(-1)^2 = 4$

B)  $f(x) = 3x^3$

Graphically: Odd Function  
Algebraically:  $f(1) = 3(1)^3 = 3$   
 $f(-1) = 3(-1)^3 = -3$

C)  $f(x) = \sqrt{x^4 + 1}$  → Even

$f(1) = \sqrt{1^4 + 1} = \sqrt{2}$

$f(-1) = \sqrt{(-1)^4 + 1} = \sqrt{2}$

D)  $f(x) = 4x + x^3$   $f(x) = -f(-x)$

$f(1) = 4(1) + 1^3 = 5$

$f(-1) = 4(-1) + (-1)^3 = -5$

E)  $f(x) = 4x + x^2$

$f(1) = 5$

$f(-1) = 4(-1) + (-1)^2 = -3$

Neither Even or Odd

Don't forget to make sure that what appears to be a vertical asymptote is not actually a hole

Find all horizontal and vertical asymptotes

A)  $f(x) = \frac{x+1}{x}$

VA: Set denominator = 0

$x=0$  VA

HA:  $f(x) = \frac{|x+1|}{|x|} \quad y=1$

If the powers are the same use the leading coefficients

C)  $f(x) = \frac{-3x^2 + 1}{x^2 - 1}$

VA:  $x^2 - 1 = 0 \quad x^2 = 1 \quad x = \pm 1$

HA:  $y = -3$

B)  $f(x) = 2^x$

$f(x) = 2^x$

exponential

HA: x-axis  
 $y=0$

VA: None



HA: Denominator

has the higher power

D)  $f(x) = \frac{3x-9}{x^2-9}$

VA:  $x^2 - 9 = 0 \quad x^2 = 9$

$x = 3 \quad x = -3$   
Hole      VA

$y=0$

E)  $f(x) = \frac{3x^3 + 3}{x^2 + 1}$

$f(x) = \frac{3x^3 + 3}{x^2 + 1}$

HA: Numerator power is bigger: **NO HA**

VA:  $x^2 + 1 \neq 0$   
No VA

F)  $f(x) = \frac{x+5}{x^3 - 27}$

$f(x) = \frac{x+5}{x^3 - 27}$

HA: **y=0**

VA:  $x^3 - 27 = 0$   
 $x=3$

Determine if each function is continuous. If the function is not continuous, find the x-axis location of each discontinuity and classify each discontinuity as infinite or removable. Also find any horizontal asymptotes.

A)  $f(x) = \frac{3x^2 + 15x}{x + 5}$

B)  $f(x) = \frac{x^2 + 3x}{x + 2}$

C)  $f(x) = \frac{9x + 6}{x^2 - 4}$

D)  $f(x) = \frac{9x + 18}{x^2 - 4}$

E)  $f(x) = \frac{x - 5}{x^2 - 4x - 5}$